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► **To cite this version:**

James Angthopo, Ignacio Ferreras, Joseph Silk. A detailed look at the stellar populations in green valley galaxies. *Monthly Notices of the Royal Astronomical Society*, 2020, 495, pp.2720-2737. 10.1093/mnras/staa1276 . insu-03748070

HAL Id: insu-03748070

<https://insu.hal.science/insu-03748070>

Submitted on 9 Aug 2022

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A detailed look at the stellar populations in green valley galaxies

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Accepted 2020 May 4. Received 2020 March 29; in original form 2019 August 28

ABSTRACT

The green valley (GV) represents an important transitional state from actively star-forming galaxies to passively evolving systems. Its traditional definition, based on colour, rests on a number of assumptions that can be subjected to non-trivial systematics. In Angthopo, Ferreras & Silk (2019), we proposed a new definition of the GV based on the 4000 Å break strength. In this paper, we explore in detail the properties of the underlying stellar populations by use of ~230 thousand high-quality spectra from the Sloan Digital Sky Survey (SDSS), contrasting our results with a traditional approach via dust-corrected colours. We explore high-quality stacked SDSS spectra, and find a population trend that suggests a substantial difference between low- and high-mass galaxies, with the former featuring younger populations with star formation quenching, and the latter showing older (post-quenching) populations that include rejuvenation events. Subtle but measurable differences are found between a colour-based approach and our definition, especially as our selection of GV galaxies produces a cleaner ‘stratification’ of the GV, with more homogeneous population properties within sections of the GV. Our definition based on 4000 Å break strength gives a clean representation of the transition to quiescence, easily measurable in the upcoming and future spectroscopic surveys.

Key words: galaxies: evolution – galaxies: formation – galaxies: interactions – galaxies: stellar content.

1 INTRODUCTION

Our understanding of galaxy formation and evolution has greatly advanced over the past decades, especially thanks to high-quality all-sky galaxy surveys. However, challenges lie ahead, due to the complex mixture of physical processes, the different time-scales involved, and the inherent degeneracies in the interpretation of the observations. To tackle these hurdles, we have to combine numerical hydrodynamical simulations based on physical equations, with large galaxy surveys, where the large data sets allow us to carefully select samples, control systematics, and follow a general statistical approach. These surveys often combine photometric and spectroscopic data, enabling the discovery of fundamental relations such as a conspicuous bimodality (see e.g. Strateva et al. 2001). The bimodal behaviour represents a clear divide regarding star formation activity (or stellar population age) with a strong dependence with stellar mass and cosmic age (see e.g. Bell et al. 2004). This bimodality can be shown on various diagrams spanned by parameters such

as the colour–magnitude (Graves, Faber & Schiavon 2009), star formation rate (SFR)–mass (Schiminovich et al. 2007; Cibinel et al. 2013), UVJ bicolour diagram (Williams et al. 2009), or colour–mass (Schawinski et al. 2014; Bremer et al. 2018), to name a few. The two contrasting galaxy populations have been termed the red sequence (hereafter RS), and the blue cloud (hereafter BC) in colour–mass diagrams. Inherent to this bimodal nature is the region separating BC from RS, commonly known as the green valley (GV; Salim 2014).

By construction, the GV can be considered a region overlapping a number of possible evolutionary pathways between BC and RS, and various scenarios have been postulated to understand the observed distribution of galaxies (Faber et al. 2007). It is generally accepted that galaxies on the GV are undergoing quenching of their star formation activity (roughly ‘ascending’ on a colour versus stellar mass diagram, where the colour index increases upwards), or undergoing rejuvenation events (Thomas et al. 2010) from recent infall of gas – therefore tracing a ‘descending’ track on this diagram. Multiple survey-based studies have been carried out to assess the properties of GV galaxies. Martin et al. (2007) combined NUV and optical fluxes to define and study the GV, finding a significant increase

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in the fraction of AGN, with respect to BC or RS galaxies. The connection of AGN activity with quenching was further supported by the transition phases found in the population analysis of SDSS early-type galaxies made by Schawinski et al. (2007). However, a morphological analysis of GV galaxies revealed a complex mixture (Schawinski et al. 2014), leading to a scenario where, at least, two channels are present, with short quenching time-scales (~ 100 Myr) being involved in the evolution of early-type galaxies, and longer time-scales ($\sim 2\text{--}3$ Gyr) in late-type systems (see also Smethurst et al. 2015; Nogueira-Cavalcante et al. 2018). Phillipps et al. (2019) use MAGPHYS to extract star formation histories from GAMA GV galaxies to derive transition times $\sim 2\text{--}4$ Gyr, with no specific signal that the quenching takes place faster than an otherwise decaying rate. Moreover, the transition processes appear to affect mostly the disc component, favouring secular disc fading (Bremer et al. 2018), and environment unsurprisingly affecting the appearance of the GV (Coenda, Martínez & Muriel 2018). It is worth mentioning here that the presence of merger-like morphologies is not favoured in GV galaxies (Mendez et al. 2011). Also note that the GV transition times appear to proceed faster at high redshift, following the standard downsizing scenario (see e.g. Gonçalves et al. 2012 for a study at $z \sim 0.8$).

Regarding intrinsic colour distributions, it is found that GV galaxies present blue outer regions, so that the recent star formation responsible for their being GV galaxies may be caused by rejuvenation events from the infall of gas clouds or gas-rich smaller galaxies (Thilker et al. 2010; Salim & Rich 2010; Fang et al. 2012). Alternatively, one can consider the quenching of star formation moving outwards from the centre due to gas depletion (Kelvin et al. 2018).

On the theoretical side, state-of-the-art numerical simulations of galaxy formation such as EAGLE are able to quantify quenching time-scales (Wright et al. 2019) and the physical processes associated with quenching (Gabor et al. 2010). Through these simulations, they find that the quenching time-scale is dependent on galaxy mass and environment. The simulations suggest that low-mass galaxies, $M_* < 10^{9.6} M_\odot$, feature quenching time-scales $\gtrsim 3$ Gyr, and intermediate-mass galaxies, $10^{9.7} M_\odot < M_* < 10^{10.3} M_\odot$, have the longest quenching time-scales, whereas the most massive galaxies, $M_* > 10^{10.3} M_\odot$, are estimated to have the shortest quenching time-scales, $\tau \lesssim 2$ Gyr. Moreover, quenching is faster in satellites, with respect to centrals (however, see Trayford et al. 2016). Note though, that alternative selection methods, such as using submillimetre fluxes, give rise to different morphologies of the same region (e.g. ‘green mountain’, Eales et al. 2018), reflecting the complexity of the interpretation of this transition region, and the potential biases caused by the specific details of the selection.

The wide range of time-scales found suggests a mixture of evolutionary channels. At low mass, quenching may be mostly due to ram pressure stripping or stellar feedback, depending on whether the galaxies are satellites or centrals. Intermediate-mass galaxies, with the highest quenching time-scales, are thought to undergo radio-mode AGN and/or stellar feedback. Finally, at the massive end, major mergers that include strong AGN activity seem to be the main cause of quenching (Hopkins et al. 2006). Moreover, halo mass may also provide a valid mode of quenching in galaxies hosted by haloes above a critical mass $M_{\text{crit}} \sim 10^{12} M_\odot$ (Gabor et al. 2010). However, to further complicate our attempt at understanding the nature of GV galaxies, they are also likely to move from RS to GV or even into the BC. This can occur through events such as wet mergers, where a quiescent gas-poor galaxy merges with a star-forming gas-rich galaxy, so that the surplus of gas causes

rejuvenation (Thomas et al. 2010). Events such as accretion of gas may also cause rejuvenation.

Due to the importance of the GV as a transition phase that can constrain the underlying physical processes, it is essential that we find an effective and robust definition of the GV, that is easily implemented in theoretical models of galaxy formation. Although many intriguing results have been observed using the colour-based definition of the GV, they may suffer from systematics caused by the adopted dust correction. The standard procedure (see e.g. Brinchmann et al. 2004) compares a number of photometric and spectroscopic observables with a set of population synthesis models where a dust prescription is applied, assuming an extinction law fixed to constraints from Milky Way stars (Cardelli, Clayton & Mathis 1989) or from starburst galaxies (Calzetti et al. 2000). This method appears to work quite well (Angho et al. 2019); however, the results may be prone to uncontrolled systematics, especially given the observed correlation between the parameters that describe the *effective attenuation* by dust in star-forming galaxies (see e.g. Kriek & Conroy 2013; Narayanan et al. 2018; Salim, Boquien & Lee 2018; Tress et al. 2018).

This paper focuses on an analysis of the new selection of GV galaxies using the 4000 Å break strength, as proposed by Angho et al. (2019, hereafter A19). The 4000 Å break is a highly sensitive age indicator defined over a relatively narrow spectral region (250 Å using the definition of Balogh et al. 1999), to avoid a large effect from dust, but wide enough to be measured with relatively low-S/N spectra, including low spectral resolution, as, e.g., with slitless grism data (Hathi et al. 2009) or medium band filters (Hernán-Caballero et al. 2013). Therefore, the break can be accurately measured at moderately low-spectral resolution, opening its use to present and future medium spectral resolution surveys that use slitless grism spectroscopy, such as PEARS (Ferreras et al. 2009); FIGS (Pirzkal et al. 2017); Euclid (Laureijs et al. 2011); WFIRST (Spergel et al. 2015); or imaging surveys that use medium-band passbands, such as ALHAMBRA (Aparicio Villegas et al. 2010); SHARDS (Pérez-González et al. 2013); JPAS (Benitez et al. 2014). The definition of the GV with the 4000 Å break is expected to provide a more direct representation of the age distribution, with substantially weaker contamination from dust.

Hereafter, we refer to the GV selection via the 4000 Å strength as ‘D4k sel’. We include a comparative study with a colour-based selection, via $^{0.1}(g-r)$ – hereafter defined as ‘ $^{0.1}(g-r)$ sel’. Note the colour is K -corrected to $z = 0.1$ that represents the typical redshift of our SDSS-based sample. Section 2 outlines the survey used, as well as the creation of the spectral stacks used in the analysis of GV galaxies. Section 3 explores the stacks by use of line strengths and simple stellar population (SSP) models. Section 4 analyses the properties of GV galaxies using spectral fitting of composite populations. In Section 5 we discuss the main results, and Section 6 finishes with a summary.

2 SAMPLE SELECTION

2.1 Spectroscopic data

This paper continues the work presented in A19, based on a sample of spectroscopic data from the classic Sloan Digital Sky Survey (SDSS, York et al. 2000). We select the sample and retrieve the spectra from Data Release 14 (Abolfathi et al. 2018). SDSS is a full-sky survey that includes spectroscopic observations of galaxies with Petrosian r -band magnitude in the range $14.5 < r_{\text{AB}} < 17.7$. Our selection criteria identify targets with relatively high signal-to-

noise ratio, $\text{snMedian}_r > 10$. We stack the spectra within carefully defined regions on the plane that defines GV galaxies (see below).

Our GV is defined on a plane spanned by a stellar population parameter (i.e. either the 4000 Å break strength or a more standard broad-band colour) along with velocity dispersion (σ), as measured in the SDSS fibre. σ is preferred with respect to stellar mass, as it is directly measurable in good-quality spectra, being free of the systematics associated with stellar mass estimates (such as the derivation of the total flux, or the model-dependent constraint of the stellar mass-to-light ratio). Furthermore, velocity dispersion is the observable that more strongly correlates with stellar population properties (see e.g. Bernardi et al. 2003; Ferreras et al. 2019). The use of spectra with the imposed threshold in S/N guarantees a robust estimate of σ . Our sample is constrained in redshift between $z = 0.05$ and 0.1 (median 0.077 ± 0.013), resulting in $\sim 228\,000$ galaxies with high-quality spectra. We bin the sample according to velocity dispersion from $\sigma = 70$ to 250 km s^{-1} , with bin spacing of 30 km s^{-1} .

The SDSS spectra cover the wavelength range 3800–9200 Å, with variable resolution, from $R = 1500$ at $\lambda = 3800 \text{ Å}$, increasing to $R = 2500$ at $\lambda = 9000 \text{ Å}$ (Smee et al. 2013). The spectra are dereddened with respect to foreground extinction, adopting the standard Milky Way dust law (Cardelli et al. 1989). The correction required was determined by the extinction parameter A_g , quoted in the SDSS catalogues, evaluated in the g band. Once the foreground dust correction is applied, the spectra are brought to the rest frame, and the individual estimates of the 4000 Å break are measured, adopting the following definition (Balogh et al. 1999):

$$D_n(4000) = \frac{\langle \Phi^R \rangle}{\langle \Phi^B \rangle}, \text{ where } \langle \Phi^i \rangle \equiv \frac{1}{(\lambda_2^i - \lambda_1^i)} \int_{\lambda_1^i}^{\lambda_2^i} \Phi(\lambda) d\lambda \quad (1)$$

and $(\lambda_1^B, \lambda_2^B, \lambda_1^R, \lambda_2^R) = (3850, 3950, 4000, 4100) \text{ Å}$. Note that our definition contrasts with the traditional approach, originally defined by Bruzual (1983) that integrate $\Phi(\nu)$ in wavelength space. We believe our definition has an easier interpretation, as the flux ratio between two spectral intervals that straddle the 4000 Å break. These two definitions can be compared via a rescaling with a constant factor of ~ 1.08 between the old and the new definition, irrespective of the properties of the underlying populations.

In this paper, as well as in A19, we contrast the newly defined GV with the traditional one based on colours from broad-band photometry. We adopt $^{0.1}(g-r)$ as the reference colour, i.e. all galaxies are measured at a fiducial redshift $z = 0.1$. The colours are taken from the flux ratios as measured within the 3 arcsec fibres of the SDSS classic spectrograph – to be consistent with the analysis of the observed spectra – and the K -correction needed to bring them to the fiducial redshift is measured directly from the spectra, following the standard approach (see e.g. Hogg et al. 2002), adopting a vanilla-standard cosmology ($\Omega_m = 0.3$; $\Omega_\Lambda = 0.7$, $H = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$). As reference, our K -correction in $(g-r)$ stays below 0.14 mag (below 0.085 mag in 90 per cent of the sample), and the median correction applied is $+0.04 \pm 0.03$ mag. The colour is also corrected for *intrinsic* dust absorption, following the dust parameters of Kauffmann et al. (2003) and adopting the Calzetti et al. (2000) attenuation law. Note we use A_V as baseline for the correction, where we find, at $z = 0.1$, $A_g^{0.1} = 1.16 A_V^{0.1}$ and $A_r^{0.1} = 0.88 A_V^{0.1}$. We refer the reader to fig. 2 in A19 for a comparison between dust-corrected and uncorrected colours on the selection plane. Note the classic SDSS 3 arcsec diameter fibres map the central region of galaxies, ~ 3 – 5 kpc. However, the interpretations of our results are robust (see Appendix C for an analysis of aperture effects).

2.2 GV definition

We give here a brief description of the selection of GV galaxies, as proposed by A19, and refer interested readers to that paper for more details. Each galaxy is identified by two parameters: velocity dispersion (σ) and an indicator of stellar age (hereafter π), choosing either the 4000 Å break strength, $D_n(4000)$, or the dust-corrected colour, $^{0.1}(g-r)$. In addition, the sample is cross-matched with the JHU/MPA catalogue (Kauffmann et al. 2003) from which we retrieve the BPT classification of nebular emission lines (Baldwin, Phillips & Terlevich 1981). This enabled us to split the sample into unclassified/quiescent (BPT = -1), star-forming (BPT = 1, 2), composite (BPT = 3), Seyfert (BPT = 4), and LINER (BPT = 5) galaxies. We do not consider here those spectra classified as composite (BPT = 3), for a cleaner classification of the three regions. Moreover, the definition of the GV, as shown below, only relies on quiescent and star-forming galaxies. In each velocity dispersion bin, we fit separately the distribution of star-forming (SF) and quiescent (Q) galaxies adopting a Gaussian distribution with respect to π , namely:

$$\mathcal{P}_k(\pi; \sigma) \equiv \frac{1}{s_k(\sigma)\sqrt{2\pi}} e^{-\frac{1}{2} \left[\frac{\pi - \mu_k(\sigma)}{s_k(\sigma)} \right]^2}, \quad (2)$$

where $\mu_k(\sigma)$ and $s_k(\sigma)$ are, respectively, the mean and the standard deviation of the distribution of π corresponding to galaxies in the velocity dispersion bin given by σ . We now propose the ansatz that these Gaussian distributions be interpreted as the probability distribution function (PDF) of BC galaxies (for $k = \text{SF}$) and red sequence galaxies (for $k = \text{Q}$). Once the PDFs are defined for the BC and RS, the green valley subset is assumed to follow a probability distribution function given by

$$\mathcal{P}_{\text{GV}}(\pi; \sigma) \equiv \frac{1}{s_{\text{GV}}(\sigma)\sqrt{2\pi}} e^{-\frac{1}{2} \left[\frac{\pi - \mu_{\text{GV}}(\sigma)}{s_{\text{GV}}(\sigma)} \right]^2}, \quad (3)$$

where the width of the Gaussian is chosen

$$s_{\text{GV}}(\sigma) = \frac{1}{2} s_{\text{Q}}(\sigma), \quad (4)$$

and the mean is given by

$$\mathcal{P}_{\text{SF}}[\mu_{\text{SF}}(\sigma); \sigma] = \mathcal{P}_{\text{Q}}[\mu_{\text{Q}}(\sigma); \sigma]. \quad (5)$$

We emphasize these constraints are purely empirical and defined ad hoc. The constraint on the mean implies that at the peak of the GV PDF, a BC galaxy and a RS galaxy are indistinguishable from a probabilistic point of view. The constraint on the width ensures that the GV does not include large fractions of galaxies in the BC or RS regions. Note that this method is performed independently within each velocity dispersion bin. The actual selection of GV galaxies follows a Monte Carlo sampling method. For each galaxy within a given velocity dispersion bin, a uniform random deviate (r) is obtained between 0 and 1, and the galaxy is accepted into the GV subset if $\mathcal{P}_{\text{GV}}[\pi; \sigma] > r$. The probability distribution functions obtained for the six velocity dispersion bins can be found in fig. 1 of A19. The GV set is further split into an upper- (uGV), middle- (mGV), and lower- (lGV) green valley, defined by the terciles of the distribution of π in the GV sample within each velocity dispersion bin. Table A1, in the appendix, shows the number of galaxies in the uGV and lGV within each velocity dispersion bin and the fraction of galaxies according to their BPT flag. For reference, we include in the table the results when colour is not corrected with respect to intrinsic dust attenuation.

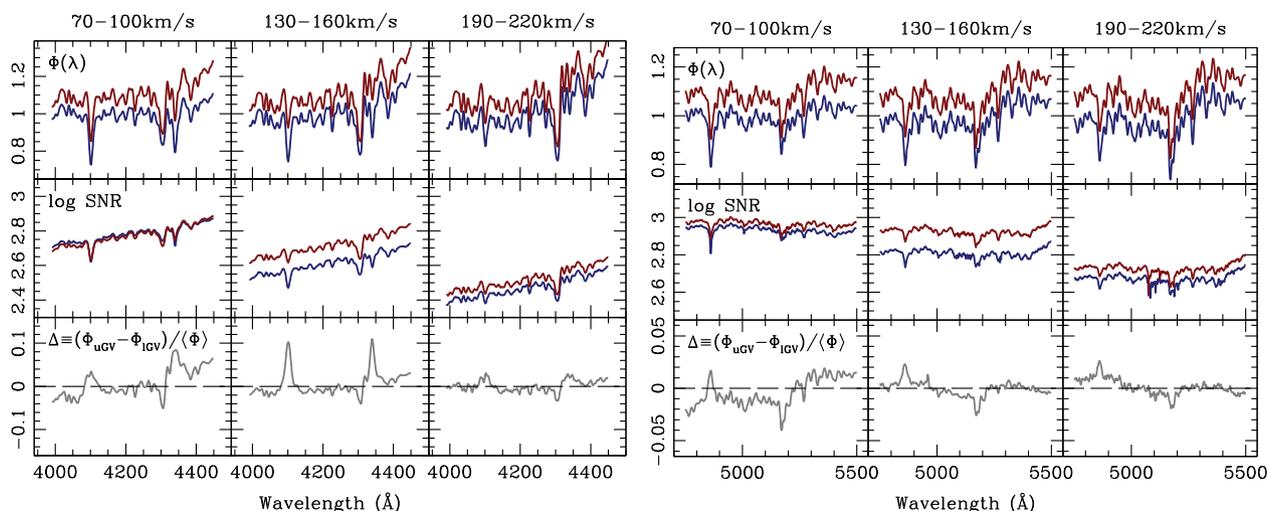


Figure 1. A comparison of the stacks is shown here in two important spectral windows: the neighbourhood of the $H\gamma$ and $H\delta$ absorption lines (left-hand panels) and the region around the $H\beta$ and $Mg+Fe$ complex (right-hand panels). From top to bottom, the panels show the fluxes of the IGv (in blue) and the uGV (in red), with a small arbitrary vertical offset to avoid crowding; the signal-to-noise ratio on a logarithmic scale; and the relative flux difference between uGV and IGv spectra. The top labels show the velocity dispersion in each case. All stacks have been convolved to a common velocity dispersion equivalent of 235 km s^{-1} .

2.3 Spectral Stacking

The subsamples of GV galaxies are then used to produce high-quality stacked spectra. High S/N is needed for a robust analysis of the stellar population content. However, more importantly, our motivation to stack the spectra is to average out galaxy-to-galaxy variations, leading to a set of ‘super-spectra’ for which the variations between different regions of the selection plane are only caused by the transitional mechanisms that give rise to the BC/GV/RS distribution.

We follow the standard procedure for the stacking of the SDSS spectra (see e.g. Ferreras et al. 2013). The stacking was carried on spectra that were de-reddened and brought to a rest-frame wavelength in the air system, applying a normalization according to the median flux in the rest-frame interval $5000\text{--}5500 \text{ \AA}$. The process implies resampling the flux within each spectral pixel following a linear split between adjacent pixels according to the amount of overlap between the original pixel and the sampled pixel. Each resulting stack is then corrected for nebular emission by performing spectral fitting with the STARLIGHT code (Cid Fernandes et al. 2005). In the stacking procedure, we exclude Seyfert AGN (BPT = 4) and Composite systems (BPT = 3), since prominent AGN luminosity contaminates the continuum, affecting the colours and the 4000\AA break strength, parameters used in the definition of the GV. The residuals with respect to the best fit spectrum are then used to fit Gaussian profiles within the standard emission regions, which are then removed from the stacks (see A19 and La Barbera et al. 2013 for details). In order to compare the spectral features across the wide range of velocity dispersion, we convolve all stacks with a Gaussian kernel to produce a velocity dispersion of 235 km s^{-1} in all cases. Fig. 1 compares the stacked data of uGV and IGv galaxies in two important regions: the interval around the age-sensitive Balmer indices $H\gamma$ and $H\delta$ (left-hand panels) and the region covering the metallicity-sensitive indices Mgb and (Fe) (right-hand panels). From top to bottom, we show the stacked spectra; the S/N; and the difference between uGV and IGv spectra, in three velocity dispersion bins, as labelled.

2.4 Uncertainty of the stacked spectra

One of the key constraints in our sample selection is the signal-to-noise ratio of individual spectra ($\text{snMedian}_r > 10$) in order to avoid stacking large numbers of noisy data. This constraint results in stacked spectra with a very high S/N (see Fig. 1) when computed with the standard statistical noise carried from the individual data. Such high values of S/N lead to underestimated uncertainties on the derived parameters, as the higher values of the best-fitting χ^2 reflect the shortcomings of population synthesis models at this level of detail. Therefore to ensure our results have more realistic uncertainties, we adapt the noise level including two estimates – added in quadrature – that take into account additional sources of uncertainty in the stacking procedure. (1) We create Monte Carlo realizations of each stack by using the uncertainty of individual fluxes. We carry out the same analysis for these stacks as our original set, therefore giving us a more robust statistical uncertainty of the derived parameters. (2) For each velocity dispersion bin, we bootstrap the subsample, selecting, at random, only 60 per cent of the galaxies. We carry out the same process as for the original stacks, therefore incorporating the systematical uncertainty in our error bars caused by the sample selection. Bins comprising fewer galaxies are expected to carry a larger uncertainty, accounting for sample selection systematics.

Additional systematics may be expected, inherently to the methodology adopted here. One such systematic relates to the use of SSP models (Bruzual & Charlot 2003; Vazdekis et al. 2012) that carry their own systematic uncertainties that depend upon the stellar library, isochrones, and initial mass function (IMF) chosen. Furthermore, the use of STARLIGHT to perform spectral fitting will carry additional uncertainties. One way to mitigate this systematic would involve comparisons among independent spectral fitting algorithms, such as PPF (Cappellari & Emsellem 2004) or FIREFLY (Wilkinson et al. 2017), beyond the scope of this paper. Another source of uncertainty arises from the emission-line correction that we apply to the Balmer absorption lines. However, our use of a battery of emission-line diagnostics and the comparison

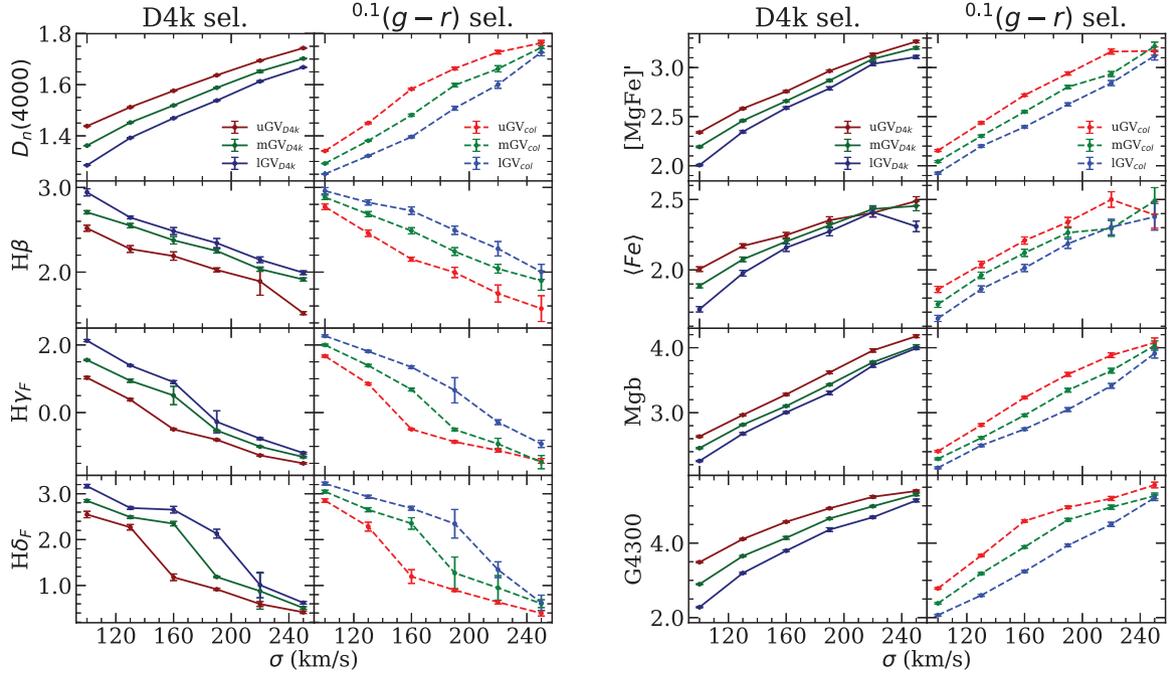


Figure 2. Comparison between line strengths of GV galaxies selected by 4000 Å break strength (D4k) or dust-corrected $^{0.1}(g-r)$ colour (col). Each panel shows the results for the upper, middle, and lower GVs, as labelled. *Left:* From top to bottom, we show the age-sensitive indices $D_n(4000)$, $H\beta$, $H\gamma_F$, and $H\delta_F$. *Right:* metallicity-sensitive indices (from top to bottom), $[MgFe]$, $\langle Fe \rangle$, Mgb, and the age-sensitive index G4300. All measurements are given as equivalent widths, in Å, except for $D_n(4000)$, which is a dimensionless ratio.

with spectral fitting – that mask out such regions – mitigates this potential systematic.

3 LINE STRENGTH ANALYSIS

Our first approach to the analysis of the underlying stellar populations in GV galaxies focuses on the observed absorption-line strengths. We select a battery of standard indices from the Lick system: $H\beta$, Mgb, Fe5270, Fe5335, G4300 (Trager et al. 1998), the higher order Balmer indices $H\gamma_F$ and $H\delta_F$ (Worthey & Ottaviani 1997), as well as the $D_n(4000)$ (Balogh et al. 1999) index already used for the definition of the GV. We combine the iron abundance indices into an average $\langle Fe \rangle \equiv (\text{Fe}5270 + \text{Fe}5335)/2$, and also measure the standard index $[MgFe] \equiv \sqrt{\text{Mgb}(0.72 \times \text{Fe}5270 + 0.28 \times \text{Fe}5335)}$ (Thomas, Maraston & Bender 2003). These indices can be split into two categories – age-sensitive and metallicity-sensitive. The Balmer indices, $D_n(4000)$ and G4300 are usually considered age-sensitive, while the others are metallicity-sensitive. However, any and all spectral indices mentioned here (and, unfortunately, elsewhere) suffer from the age–metallicity degeneracy (e.g. Worthey 1994; Ferreras, Charlot & Silk 1999).

3.1 General trends

This approach, solely based on the observed line strengths, is meant to assess in a model-independent way the variations between different regions across the GV. Fig. 2 shows the line strengths measured in the stacks, plotted with respect to velocity dispersion. We note these measurements are taken from the stacks that are smoothed to a common velocity dispersion of 235 km s^{-1} . Within each subfigure, the left-hand (right-hand) panels correspond to a

selection of GV galaxies based on 4000 Å break strength [dust-corrected $^{0.1}(g-r)$ colour]. Each panel shows independently the trends in the upper, middle, and lower GV, including an error bar obtained from bootstrapping the sample. The $D_n(4000)$ index increases strongly with velocity dispersion in both cases and in all three regions of the GV, in agreement with previous studies (see e.g. Kauffmann et al. 2003; Graves et al. 2009). However, at low velocity dispersion, the D4k selection produces overall higher values of the break, along with a wider range, towards lower values of the Balmer indices, consistently supporting the hypothesis that the D4k selection produces a GV with older and more homogeneous populations, especially at the low-mass end. At the high-mass end, both selection criteria give rather similar results, although the lGV set defined by D4k appears to give slightly lower values than the colour-based lGV. However, this behaviour is not paralleled by the Balmer lines, so the mapping into population trends becomes less trivial. Nevertheless, the strong trends found in all age-sensitive indices with respect to velocity dispersion give robust confirmation of the well-known age–mass relation (see e.g. Gallazzi et al. 2005).

Both selection methods unsurprisingly produce the lowest (i.e. youngest) break strengths and highest (i.e. youngest) Balmer indices in the lGV at the low-mass end, whereas at high-velocity dispersion, the differences between lGV and uGV are minor. We should keep in mind that the age-sensitive indices presented in Fig. 2 behave differently with respect to the age distribution, with the Balmer indices being more sensitive to recent star formation episodes compared to $D_n(4000)$ (Poggianti & Barbaro 1997). Regardless of the GV selection method, as we traverse from lGV to uGV, we find a decrease in the line strengths of all Balmer indices, thus indicating a smooth transition from the younger lGV to the predominantly quenched, passively evolving uGV. It is worth noting that the colour-based selection produces overall higher Balmer

indices, possibly implying the presence of younger (but dustier) galaxies, with respect to the D4k selection. Even though the colour selection includes an intrinsic dust correction, biases may appear as the correction is prone to systematics regarding the derivation of the dust corrections as well as variations of the dust attenuation law caused by the diverse range of dust geometry and chemical composition in galaxies (see e.g. Tress et al. 2018; Narayanan et al. 2018). Moreover, note that the K -correction applied to bring the observed colour within a fiducial value ($z = 0.1$ in our case) may also introduce an additional systematic: the median K -correction applied is 0.04 mag but there is an obvious dependence with redshift – with the correction trivially vanishing at $z = 0.1$ – and a more subtle trend with the intrinsic colour – with the K -correction being larger in the redder galaxies. The difference in this correction with respect to the intrinsic colour can be as high as ~ 0.1 mag, thus comparable with the interval that defines the GV. Such behaviour can introduce a correlation in the selection of the GV. In contrast, the 4000 Å break selection depends neither on dust correction (see Appendix B) nor on the K -correction (as the index is directly measured on the rest-frame spectra).

The panels on the right of Fig. 2 present the results for metal-sensitive indices along with G4300. The index G4300 increases with velocity dispersion, roughly following a very similar trend as $D_n(4000)$. Note that this index separates more smoothly the LGV, mGV, and uGV, confirming a strong correlation with the 4000 Å break. For $[\text{MgFe}]'$, $\langle \text{Fe} \rangle$, and Mgb, we find the expected positive correlation with increasing velocity dispersion (e.g. Sansom & Northeast 2008). The line strength $[\text{MgFe}]'$ – that can be approximately considered a total metallicity indicator – shows that, in general, the D4k selection features slightly more metal-rich populations compared to the colour selection, in all GV regions. By comparing $\langle \text{Fe} \rangle$ and Mgb, we find both produce similar trends. As we move up the GV, from LGV to uGV, the data show increasing metallicity. It is worth mentioning here that the dependence of these indices on age – due to the age-metallicity degeneracy – is such that higher values of the index could also be explained by *older* ages. Section 4 is devoted to a comparison of the stacked spectra with population synthesis models via spectral fitting, to be able to break such degeneracies. Moreover, we show below (Section 3.2) an analysis of stellar ages based on SSPs.

Therefore, Fig. 2 shows a subtle but measurable difference with respect to the GV selection method (D4k versus colour). These differences are especially substantial at low-velocity dispersion, where the contribution from dusty, star-forming galaxies may introduce a larger systematic on the dust correction needed when using a colour selection.

3.2 SSP properties

In A19, we provided an estimate of the SSP-equivalent ages of GV stacks restricted to the subset of quiescent galaxies. Here, we include star-forming and LINER-like AGN to produce stacks that give a more comprehensive description of the average properties of GV galaxies. We also include more information about the SSP model fitting procedure – which is identical to the one presented in A19 – and extend the analysis, including a simple measurement of non-solar abundance ratios. The interpretation of the stacked spectra is done via a comparison of a selected set of age- and metallicity-sensitive line strengths, between the observed measurements and the values obtained from stellar population synthesis models.

3.2.1 Age and metallicity

In this section, we produce easy-to-interpret ‘SSP-equivalent’ ages, instead of a more complex combination of populations, left to Section 4. SSP-derived ages should be interpreted as a luminosity averaged age, as if the whole stellar content of the galaxy were formed in a single burst. An alternative definition – based on composite age distributions following a pre-defined functional form of the star formation rate – can be prone to biases due to the specific form adopted. We show both estimates of age in this paper to be able to assess the actual variations in the underlying populations of GV galaxies. We follow a Bayesian approach, probing a large volume of SSPs from the MIUSCAT population synthesis models (Vazdekis et al. 2012), comparing the observed and the model line strengths with a standard χ^2 statistic:

$$\chi^2(t, Z) = \sum_i \left[\frac{\Delta_i(t, Z)}{\sigma_i} \right]^2, \quad (6)$$

where $\Delta_i(t, Z) = O_i - M_i(t, Z)$ is the difference between the observed line strength and the model prediction for the i th index, and σ_i is the corresponding uncertainty. The grid of SSP models comprise 8192 synthetic spectra. The stellar age ranges from 0.1 to 13.5 Gyr, in 128 logarithmically spaced steps, and metallicity ($[Z/H]$), varies from -2.0 to $+0.2$ dex, with 64 steps. We note the original models have a reduced set of metallicity steps (seven in total) and we interpolate (bi)linearly for a given choice of (log) age and metallicity.

Since the signal-to-noise ratio of the data is very high (Fig. 1), we need to apply offsets to the individual indices to account for potential variations due to differences in the $[\text{Mg/Fe}]$ abundance ratio of the populations or, indeed, due to an extended age distribution. Our modulus operandi involves computing the best-fitting solution (i.e. giving the minimum χ^2) for a fiducial stack. This fiducial stack is chosen as the one that gives the lowest value of χ^2 for the best fit. We then define the offsets for each line strength from this best-fitting solution, and apply these offsets (δ_i), such that $\Delta_i(t, Z) = O_i - M_i(t, Z) - \delta_i$ in equation (6) – to *all* the stacks in the sample. Given the large S/N of the spectra, we also add in quadrature – as a potential systematic error, and in order to produce conservative error bars – an additional amount corresponding to 5 per cent of the measured line strength. The resulting χ^2 distributions are bivariate functions of age and metallicity. We fix the stellar IMF to Kroupa (2001). Note that the results for alternative choices of the IMF, such as Chabrier or Salpeter, give very similar results, and that, within the range of velocity dispersion values considered in this sample, no substantial variations of the IMF are expected (see, e.g. Ferreras et al. 2013).

Fig. 3 shows the corresponding probability contours of the bivariate likelihood $\mathcal{P}(t, Z)$ derived from the spectral stacks of the uGV (red) and LGV (blue) galaxies, selected according to 4000 Å break strength. The contours are slightly smoothed by a Gaussian kernel, and shown at the equivalent 1, 2, and 3 σ confidence levels, with each panel representing a velocity dispersion bin. Note the expected positive correlation between velocity dispersion and either SSP-equivalent age or metallicity. We note that the method is especially good for determining *relative* variations in the stellar age, whereas metallicity is less well constrained. The difference in age between LGV and uGV galaxies is apparent. We marginalize over metallicity, producing the trends in SSP-equivalent age shown in Fig. 4, with the error bars given at the 1σ level. We show the uGV and LGV trends with respect to velocity dispersion in the D4k-selected (left) and colour-selected (right) GV. The bottom panels show the age difference between the two. We stress that this paper focuses on spectral stacks that include star-forming, quiescent and

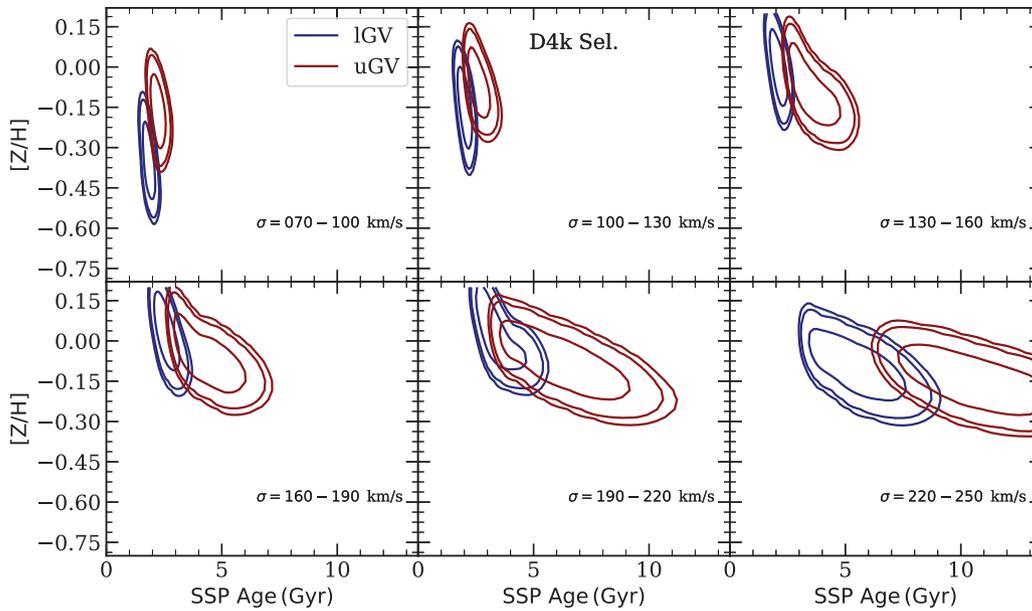


Figure 3. The likelihood derived from the line strength analysis of SSP-equivalent age and metallicity is shown with contour plots at the equivalent 1, 2, and 3 σ levels. These stacks correspond to the selection of GV galaxies based on 4000 Å break strength. The blue (red) contours represent IG (uGV) stacks.

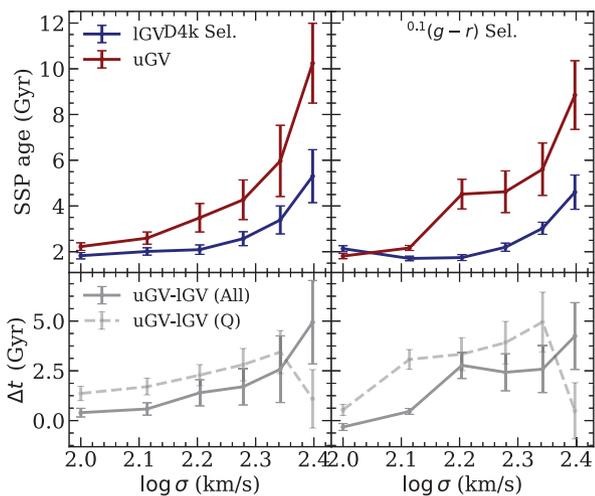


Figure 4. The SSP-equivalent age derived from line strengths is shown with respect to velocity dispersion in the IG (blue) and uGV (red) subsets for the D4k- (left) and the colour-selected (right) GV. The bottom panels show the age difference between uGV and IG stacks. These are derived from the stacks presented in this paper that comprise quiescent, star-forming, and LINER AGN galaxies. The dashed grey lines in the bottom panels contrast the results with A19, where the stacks only involve quiescent GV galaxies.

LINER-like galaxies. The dashed grey lines in the bottom panels show the analysis when restricting the stacks to quiescent galaxies, as shown in fig. 4 of A19. Both sets of stacks feature a similar increasing trend with σ , except at the highest velocity dispersion bin, where the quiescent sample shows a significant decrease.

3.2.2 $[Mg/Fe]$

Overabundances in $[Mg/Fe]$ are traditionally associated with short and intense star formation episodes, where the delayed Fe-rich contribution from type-Ia supernovae is not incorporated into stars

(see e.g. Thomas, Greggio & Bender 1999). Standard models based on a single or double degenerate progenitor imply delays between 0.5 and 2 Gyr (Matteucci & Recchi 2001). Therefore, populations with supersolar $[Mg/Fe]$ are expected to have been formed over similar time-scales. Therefore, an estimate of $[Mg/Fe]$ provides a stellar clock that has been exploited, for instance, to show that massive early-type galaxies must have formed their central regions within a dynamical time-scale. Here, we look for potential variations of $[Mg/Fe]$ in the stacked GV spectra, following the proxy adopted in La Barbera et al. (2013). This proxy allows one to use standard, solar-scaled population synthesis models to measure $[Mg/Fe]$. The procedure involves constraining a grid of SSP models using two different sets of line strengths, one involving age-sensitive indices along with an Mg-sensitive index (obtaining a metallicity $[Z_{Mg}/H]$; in this case, we use Mg $_{gb}$) and another one involving the same age-sensitive indices plus a Fe-sensitive index (producing $[Z_{Mg}/H]$, we use here (Fe)). The difference, i.e. $[Z_{Mg}/Z_{Fe}]$, is the adopted proxy for $[Mg/Fe]$.

Fig. 5 plots $[Z_{Mg}/Z_{Fe}]$ against velocity dispersion for both definitions of the GV, where the numbers in the legend represent the Pearson correlation coefficient (pcc). Our estimate of pcc along with its uncertainty involves 100 Monte Carlo realizations. For each realisation, we remove at random one data point and calculate the resulting pcc; this is done to mitigate the effect of outliers. The pcc is quoted as the median of the distribution and the uncertainty is one standard deviation. The data points are shifted horizontally by an arbitrary amount to avoid overcrowding. In the D4k selection (top panel), the uGV behaves differently with respect to IG and mGV, which behave in a similar manner to each other. Both mGV (pcc = $+0.77 \pm 0.06$) and IG (pcc = $+0.59 \pm 0.14$) show a weak but significant correlation with velocity dispersion, whereas the abundance ratio in uGV galaxies (pcc = -0.24 ± 0.14) seems rather constant. Interestingly, the colour-based selection (bottom panel) shows an increasing trend in all subsamples of the GV, although $[Z_{Mg}/Z_{Fe}]$ appears to flatten in uGV galaxies with $\sigma \gtrsim 150 \text{ km s}^{-1}$. The trends support the scenario of a more extended star formation history (SFH) in lower mass galaxies (see e.g. de la Rosa et al. 2011).

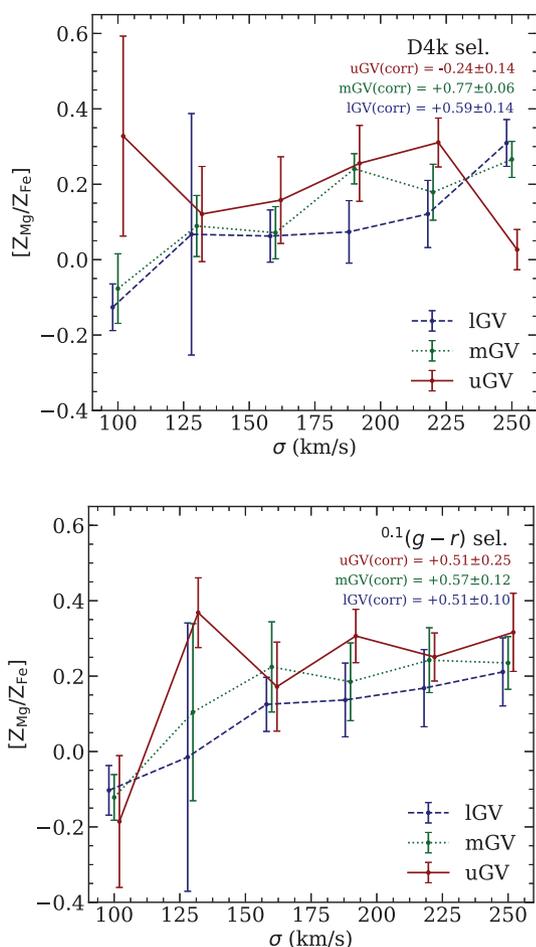


Figure 5. The relation between the abundance ratio proxy $[Z_{\text{Mg}}/Z_{\text{Fe}}]$ and velocity dispersion for 4000 Å break strength (top) and colour selection (bottom). The blue, green, and red lines show the trends for lGV, mGV, and uGV galaxies, respectively (see the text for details about the derivation of this $[Z_{\text{Mg}}/Z_{\text{Fe}}]$ proxy). The numbers in red, green, and blue show the Pearson correlation coefficient (pcc) between $[Z_{\text{Mg}}/Z_{\text{Fe}}]$ and velocity dispersion in the uGV, mGV, and lGV subsamples, respectively.

3.3 Difference regarding (nebular) activity

In A19, we restricted the stacking procedure to quiescent galaxies. The motivation in that letter was to assess the transition period of quenched galaxies across the GV, by considering systems where star formation is already absent. In this paper, we consider, instead, the general trends of GV galaxies, so that the different contributions of quiescent, star-forming, and AGN systems (see Table A1) manifests in those trends. Moreover, as systems with nebular emission are expected to be significantly affected by dust, we want to explore the differences between the D4k selection (minimally affected by dust) and the colour selection (that applies a dust correction, but may be affected by systematics from this correction). Therefore, a comparison between the quiescent stacks of A19 and those that include star-forming and LINER-like emission provides useful insight on the properties of GV galaxies and the potential biases caused by the selection method.

Fig. 6 shows the difference in the age-sensitive indices between the Q stacks (hereafter Q_{stack}) and the combined Q+SF+LINER stacks (hereafter All_{stack}). The top and bottom panels show the difference in results for uGV and lGV galaxies, respectively. Solid

and dashed lines show the results for D4k and colour selection, respectively. In uGV galaxies, a decrease in the difference of $D_n(4000)$ with respect to velocity dispersion is evident for both D4k (pcc = -0.92 ± 0.02) and colour selection (pcc = -0.90 ± 0.01). This trend can be attributed to the lower contribution of star-forming galaxies, as velocity dispersion increases (see Table A1). It should be noted that the variation in $\Delta D_n(4000)$ (leftmost panels) for the D4k selection should be, by construction, minimal, as we are constraining the $D_n(4000)$ index within certain values. Note, in contrast, the different trends found in the Balmer indices. For the uGV, inclusion of SF galaxies increases Balmer absorption in both definitions of the GV, as expected from the decrease in average age. Furthermore, the values of pcc show a stronger correlation/anticorrelation in uGV in comparison to lGV; this effect can be attributed to a lower percentage of SF and AGN galaxies in uGV in contrast to lGV with increasing velocity dispersion. We find a more homogeneous distribution of stellar populations when GV galaxies are selected according to D4k, whereas the colour-based selection produces larger differences in the indices in both uGV and lGV.

Fig. 7 shows the results for the remaining line strengths. Note the age-sensitive G4300 behaves similarly to $D_n(4000)$, as in Fig. 2. Both Figs 6 and 7 show that in all cases, the line strength variations are significantly smaller for the D4k selection, confirming that a more homogeneous distribution of GV galaxies is produced when selecting the sample on break strength. A colour-based selection, even after a careful dust correction is applied, produces a more complex mixture of galaxies, regarding nebular activity. We argue that the D4k selection results in a more representative sample of transitioning galaxies from the BC to the RS. Note that for the metallicity sensitive indices, the difference between stacks gives a negative value that may suggest lower average metallicities when stacking only quiescent galaxies. Note that e.g. $[Z_{\text{Mg}}/Z_{\text{Fe}}]$ also increases with stellar age, so that an age-dependent explanation would need to invoke *younger* populations in Q galaxies. In contrast, the colour selection yields positive variations in the metal-sensitive indices, as expected if All_{stack} is dominated by younger, metal-poor, star-forming galaxies. This result further supports the idea of population contamination when using colour selection. This contamination seems to affect not only the age-sensitive but also the metallicity-sensitive indices at all values of the velocity dispersion, although the difference appears to decrease towards higher velocity dispersion, where the contamination from dusty BC galaxies decreases.

4 SPECTRAL FITTING ANALYSIS

In order to look in more detail at the stellar population content of GV galaxies, we carried out spectral fitting, by use of the STARLIGHT code (Cid Fernandes et al. 2005), to produce best-fitting *composite* mixtures. Variations of these mixtures across the GV will inform us of the transition between the lGV to the uGV – note that depending on whether the dominant mode is quenching or rejuvenation, it is possible to evolve in *both directions*. STARLIGHT performs linear superpositions of SSP spectra supplied by the user, selecting a best fit by minimizing a χ^2 statistic with an MCMC sampler. In this paper, we use a grid of $N_* = 138$ SSPs from the models of Bruzual & Charlot (2003, hereafter BC03), adopting a Chabrier (2003) IMF. Our grid consists of 28 distinct stellar ages and six different metallicities. The age ranges from 1 Myr to 13 Gyr, spaced logarithmically, and the metallicity varies from $[Z/H] = -2.3$ to $+0.4$.

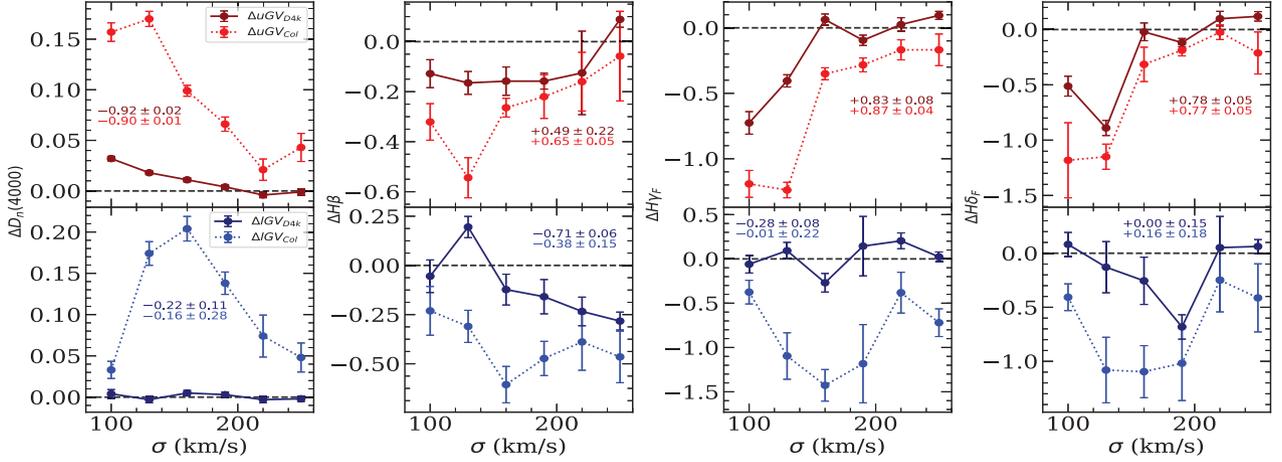


Figure 6. Differences in age-sensitive line strengths between uGV (top panel) and lGV (bottom panel) between Q only stacks and ‘full’ stacks, comprising SF, LINERS, and Q galaxies. The light red and blue dotted data shows the difference for colour selection, while dark red and blue solid lines show the difference in the D4k selection. Likewise, the numbers shown in light red and light blue give the Pearson correlation coefficient regarding the colour selection data points, while the dark red and blue text shows the correlation coefficient calculated for the D4k-selected sample. The error bars are quoted at the 1σ level.

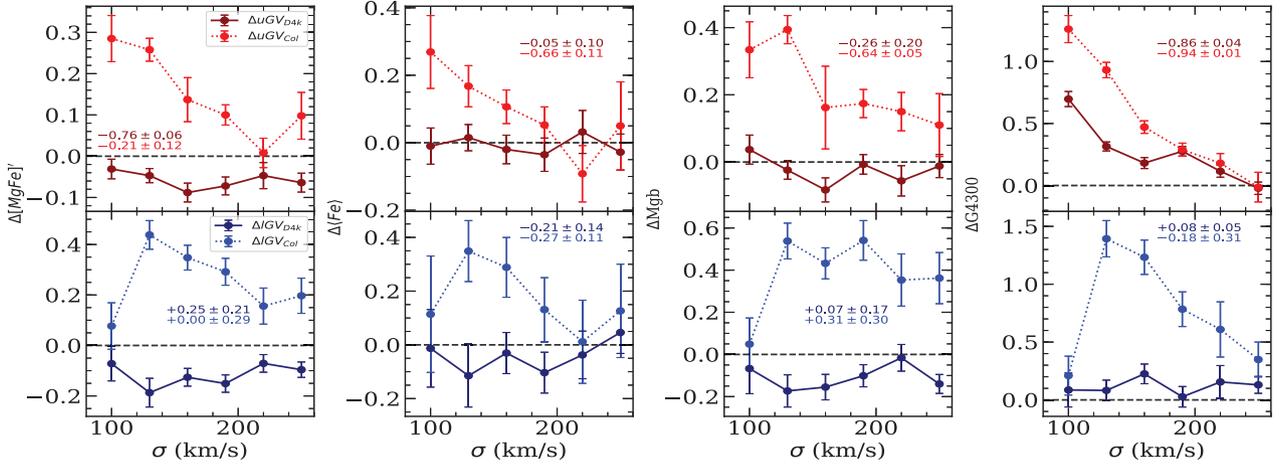


Figure 7. Same as Fig. 6 but here we show metallicity sensitive indices and G4300.

We mask out the standard spectral regions where nebular emission may be prominent. The fitting range we chose – 3500–7500Å – includes a number of age- and metallicity-sensitive regions such as those targeted in the previous section. Spectral fitting provides an alternative approach to individual line strength analysis; the larger amount of information, including the stellar continuum from the NUV, optical and NIR windows, allows for constraints on more complex distributions of stellar ages and metallicities.

4.1 Luminosity-weighted parameters

Fig. 8 shows the luminosity-weighted averages of some key stellar population parameters of the GV stacks as a function of velocity dispersion. The left-hand (right) panels show the D4k- (colour-) based selection, respectively. The blue dashed, green dotted, and red solid lines represent the result for lGV, mGV, and uGV, respectively. Each panel quotes the corresponding Pearson correlation coefficient (pcc). From top to bottom, we show the average stellar age, $\langle t \rangle$, a parameter, Δt , defined below, that keeps track of the width of the age distribution, the average total metallicity, $\langle [Z/H] \rangle$, and the dust

attenuation applied as a foreground screen, A_V . The average age is defined as

$$\langle \log t \rangle = \sum_{j=1}^{N_*} x_j \log t_j, \quad (7)$$

where x_j is the normalized luminosity weight (i.e. $\sum_j x_j = 1$) and t_j is the age of the j th SSP in the basis set (see Cid Fernandes et al. 2005 for details). The average age shows the well-established trend, where velocity dispersion, roughly a proxy for galaxy mass, is positively correlated with the average age (e.g. Gallazzi et al. 2005). Galaxies on the uGV are consistently older at all values of velocity dispersion. The age difference between mGV and lGV is less prominent than between these two and the uGV. A possible explanation for this trend is discussed in Section 5.2. The age difference between the uGV and lGV stays in the region 0.5–1 Gyr, a consistent result with respect to the SSP analysis shown in Section 3.2.

The uncertainties of the parameter estimates are obtained by making 20 Monte Carlo realizations of each stack, by adding noise consistently with the uncertainties in each flux bin, and re-running each one of them through STARLIGHT. The realizations produce a

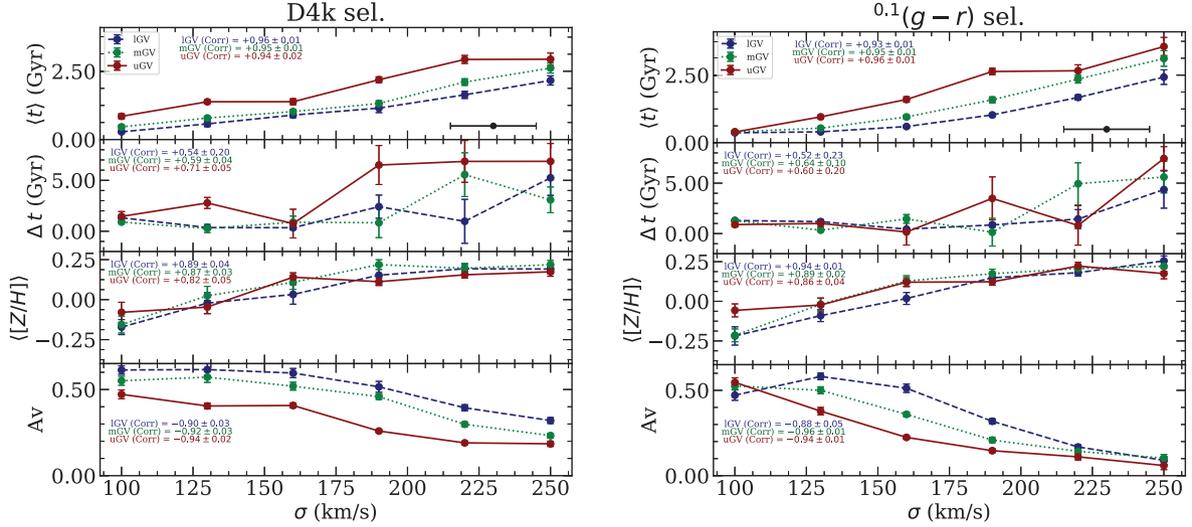


Figure 8. From top to bottom, trends with velocity dispersion of average stellar age, Δt – that acts as pseudo- quenching time-scale – metallicity and dust attenuation. The blue dashed, green dotted, and red solid lines show the results for IG, mG, and uG, respectively. Results are shown for the 4000 Å break selection (left) and the colour selection (right) of GV galaxies. The numbers in each panel quote the Pearson correlation coefficient (pcc), where the colours correspond to IG, mG, and uG, accordingly.

distribution from which the standard deviation of the parameter estimates is quoted as the uncertainty. Galaxies in the IG have a smoother age trend with respect to velocity dispersion.

The second age indicator, Δt (the second panel from the top), is extracted from the cumulative stellar mass profile:

$$\mathcal{C}(s) = \sum_j x_j(t \leq s). \quad (8)$$

Defining the inverse of this function as $\tau(y) \equiv \mathcal{C}^{-1}(y)$, we take the time interval $\Delta t \equiv \tau(0.70) - \tau(0.30)$, i.e. the time lapse spanning the epochs when the galaxy, or its progenitors, formed between 30 per cent and 70 per cent of its total stellar mass. The motivation behind this definition is to provide a GV transition interval that could be related, for instance, with a quenching time-scale. However, note two important caveats. First, if the galaxy has experienced a rejuvenation episode, the recently formed stars will be given more weight, thus leading to high Δt values: even if the actual quenching time-scale is relatively short. Secondly, we are dealing with stacks that include star-forming galaxies. Therefore, our definition of Δt should be considered as an effective GV time-scale, rather than a true quenching interval. Previous results from the literature noted that the quenching time-scale evolves in a complex way with velocity dispersion, with an initial increase, followed by a decrease at the massive end (Gabor et al. 2010; Wright et al. 2019). Here, we find Δt increases in all cases, in contrast with the trends found in the line strength analysis of A19, where a non-monotonic behaviour was found between the SSP-equivalent age difference of galaxies on the uG and IG with respect to velocity dispersion.

The third panel from the top shows the average total metallicity, calculated in a similar manner to average age, namely

$$\langle [Z/H] \rangle = \sum_{j=1}^{N_*} x_j [Z/H]_j, \quad (9)$$

where $[Z/H]_j$ is the individual SSP metallicity of the j th component. A strong positive trend is also found between total metallicity and velocity dispersion, once more in agreement with previous

studies of the general population (see e.g. Gallazzi et al. 2005; Graves, Faber & Schiavon 2010). At the low-mass end, the colour-based selection (panels on the right) shows a consistent trend towards a higher metallicity in the uG with respect to the IG. However, this trend is less evident in the D4k selection (left-hand panels), which is less sensitive to contamination from dusty, star-forming (and possibly lower metallicity) galaxies, especially in the IG, resulting in a weaker correlation for D4k selected samples in comparison to a colour-based GV. The D4k selection shows that, within error bars, metallicity does not segregate within the GV at fixed velocity dispersion. This result suggests a potential bias when selecting GV according to colour. The next (bottom) panels of Fig. 8 show the monotonically decreasing trend of dust attenuation with σ , consistent with previous studies (e.g. La Barbera et al. 2014), featuring a clear stratification from IG to uG, with mG galaxies having, once more, properties closer to IG galaxies. This information can also help assess potential biases related to the dust correction needed in the colour-based selection. It is worth mentioning the small difference in A_V at the lowest velocity dispersion in colour-based GV galaxies. One could argue that the dust correction could be partly responsible for this result, whereas the D4k selection shows the A_V stratification between uG, mG, and IG at all values of σ .

Fig. 9 shows the variation in average metallicity as a function of Δt and average age, as labelled. The results of a D4k (colour) selection of GV galaxies is shown on the left (right) panels, following the same colour coding as the previous figure to represent the uG, mG, IG stacks. The marker size maps velocity dispersion. Focusing on the D4k selected sets, we find two different trends in the sample: (i) At low metallicity ($[Z/H] \lesssim +0.1$), GV galaxies have short Δt ($\lesssim 3$ Gyr); (ii) At higher metallicity, GV galaxies have a broader distribution of Δt , a result indicative of rejuvenation. In this region, galaxies have higher velocity dispersion and feature older stellar populations. Moreover, IG and mG galaxies have relatively shorter Δt , with respect to uG systems, that have $\Delta t \gtrsim 5$ Gyr. Therefore, a higher fraction of uG galaxies at the massive end appear to have undergone more substantial episodes of rejuvenation. The standard age–metallicity relation can be found in

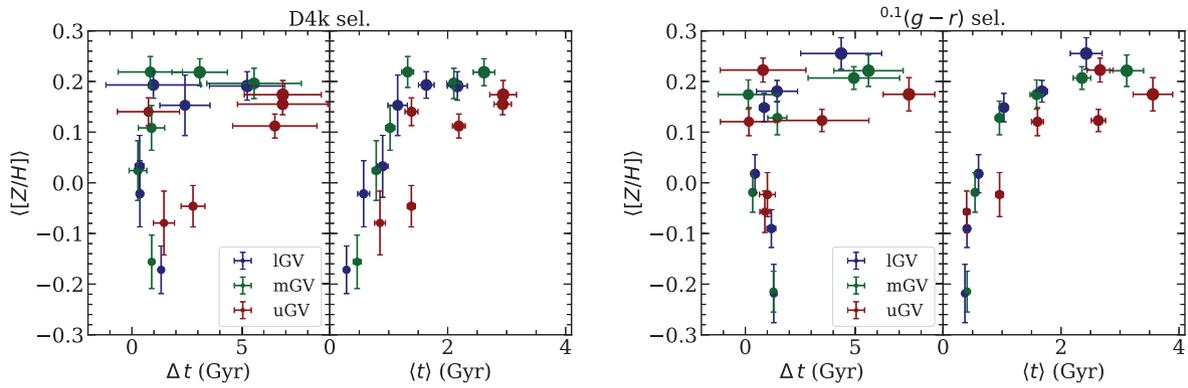


Figure 9. Trends between metallicity and either Δt or average age. The blue, green, and red data points show the results for IGV, mGV, and uGV, respectively. The marker size follows velocity dispersion. The uncertainty in average metallicity remains constant, whereas the error bar in Δt_Q increases with average metallicity. Results are shown for the 4000 Å break selection (left) and the colour selection (right) of GV galaxies.

the figure, with a significant stratification towards older populations at fixed metallicity in uGV galaxies. This effect is more pronounced in the D4k selection, whereas the colour-based selection produces a more complex mixture at low-velocity dispersion, as expected from the contribution of dust, more prevalent at this end of the distribution.

4.2 Star formation history

The next step in the analysis of the spectral fitting constraints is the SFH, namely the distribution of SSP weights, x_j as a function of age – i.e. marginalized with respect to metallicity. Note that individual SFHs constrained on a galaxy-by-galaxy basis are rather uncertain with any population fitting code, and STARLIGHT is no exception. However, as we are dealing with stacked spectra covering a large number of galaxies, we can assume that the derived SFHs represent statistical trends in the various regions of the GV probed here. Fig. 10 shows the luminosity-weighted output for IGV (blue), mGV (green), and uGV (red). The histograms bin the age intervals in a linear manner. The average age and metallicity, quoted in each panel, have been calculated using the SSP ages of the basis set, along with their corresponding weights, following equations (7) and (9). The left-hand and right-hand panels show the results at the lowest and highest velocity dispersion bins, $70 < \sigma < 100 \text{ km s}^{-1}$ and $220 < \sigma < 250 \text{ km s}^{-1}$, respectively. The upper (lower) panels show the results for the D4k (colour) selection, as labelled. Note these results are robust regarding the *relative* weight contributions, whereas absolute estimates may carry larger uncertainties. To assess the statistical uncertainty, we perform for each stack a Monte Carlo set of 20 realizations of spectra with the same flux distribution and noise compatible with the stack under consideration, following an identical methodology. The shaded regions in the figure show the expected uncertainty from this comparison. Note that spectral fitting inherently constrains luminosity-weighted properties. A translation into mass-weighted values unavoidably carries additional uncertainties, related to the mapping from luminosity into stellar mass. For instance, a recent episode of star formation can bias the results as the hot, massive stars present in young populations contribute significantly more than their cool, low-mass (although equally young) counterparts.

At low-velocity dispersion (left-hand panels), the stellar populations are mostly young. As we traverse the GV from IGV to uGV, more weight is given to the older components, increasing

the average age from $\langle t \rangle \sim 0.3 \text{ Gyr}$ in the IGV to $\sim 1 \text{ Gyr}$ in the uGV, for the D4k selection, whereas the colour-based selection produces a more homogeneous distribution, with undistinguishable age differences ‘across the valley’, and a significantly larger scatter. In all cases, the SFHs concentrate within the most recent $\sim 2 \text{ Gyr}$, with small, subdominant old populations that become, only slightly, more prominent in the uGV. At high-velocity dispersion (right-hand panels), the SFHs evolve towards older components, with average (luminosity-weighted) ages $\sim 2\text{--}3 \text{ Gyr}$.

Fig. 11 shows the variation of the mass fraction in old ($> 10 \text{ Gyr}$) stars with respect to velocity dispersion and average age, for the D4k (left) and colour (right) selection. Both cases produce similar increasing trends of the old contribution in the most massive galaxies and towards higher average ages. The latter statement is not trivial, as this diagnostic is sensitive to whether the age distribution changes its width with respect to average age. The D4k selection produces consistently higher old stellar fractions at all values of velocity dispersion, whereas the colour-based selection, once more, shows some mixing at the low-mass end. Regardless of the selection process, uGV galaxies display more of a difference with respect to mGV and IGV galaxies. Note that at low-velocity dispersion, the colour selection yields a lower fraction in old stars, specially in the uGV. This is interesting as even though both selection methods feature not too dissimilar low fractions of Q galaxies (7.3 ± 0.4 per cent for D4k, and 4.2 ± 0.4 per cent for colour), we see a greater number of SF galaxies in the colour-based selection (namely, 70.0 ± 1.3 per cent in the D4k selection versus 78.4 ± 2.1 per cent for the colour selection). This could be a further indication of a possible bias due to dust attenuation that causes BC galaxies to ‘creep’ into the GV (Schawinski et al. 2014). This theory is further supported at intermediate velocity dispersion bins, $100 < \sigma < 190 \text{ km s}^{-1}$, where even though there is a lower contribution of SF galaxies in the D4k Selection of the uGV, a higher fraction of old stars is found in the colour-based GV stacks.

4.3 Mass-weighted population properties

In addition to the luminosity-weighted properties presented above, we can extend the analysis by use of the stellar-mass-to-light ratio (Υ_*) provided by the population synthesis models for each SSP. Although this translation carries additional uncertainty, it is a way to assess whether the older components are more dominant than expected from a simple fit to the observations, which are inherently

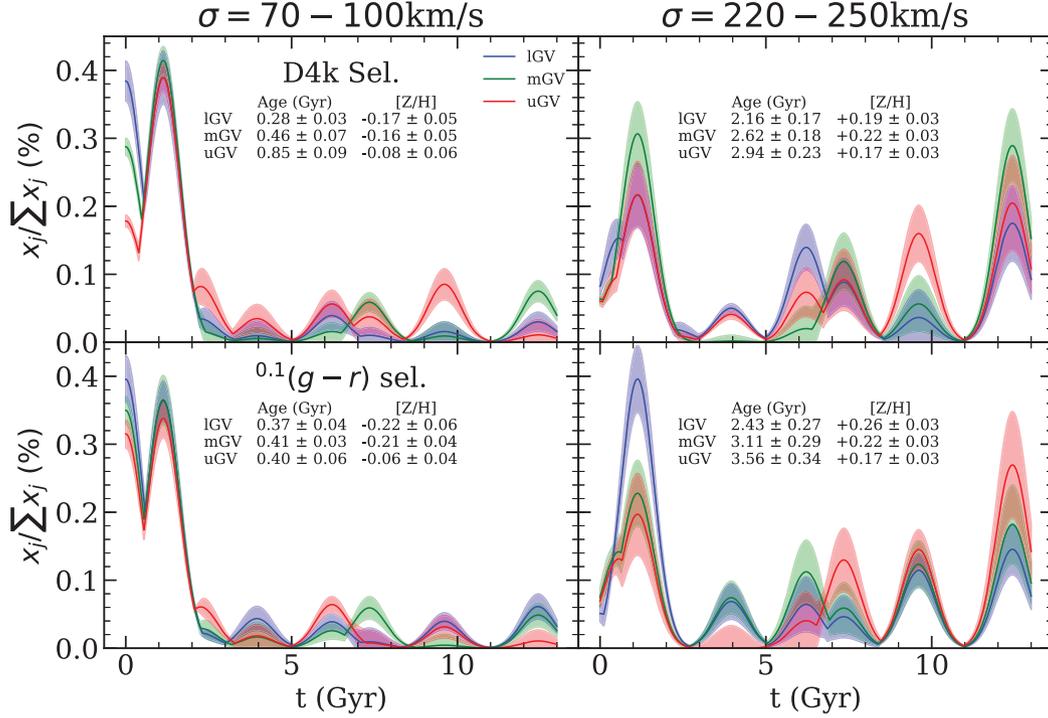


Figure 10. The SFH is shown for both $D_n(4000)$ (top) and colour (bottom) selected GV galaxies. The left and right sides show the SFH in the lowest velocity dispersion bin $70 < \sigma < 100 \text{ km s}^{-1}$ and the highest velocity dispersion bin $220 < \sigma < 250 \text{ km s}^{-1}$, respectively. The blue, green, and red curves represent the SFHs of IGV, mGV, and uGV galaxies, respectively.

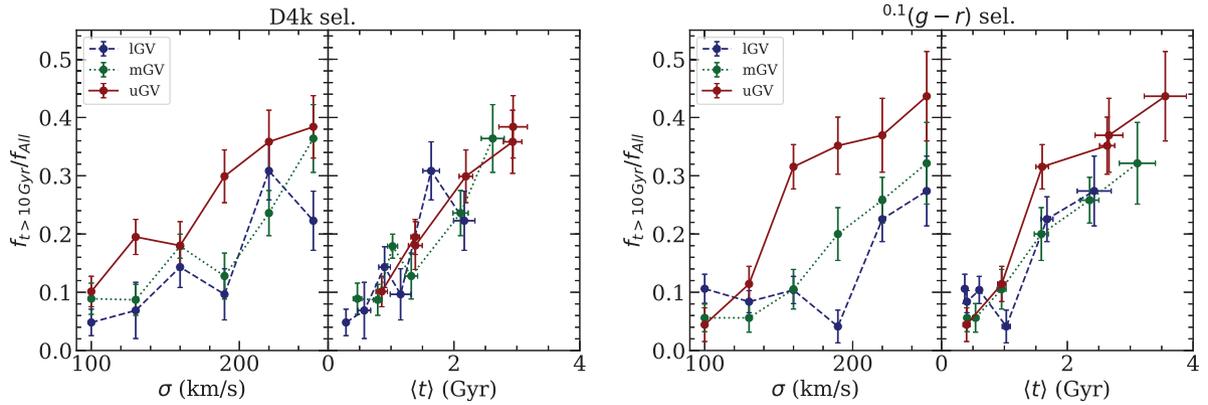


Figure 11. Relation between the mass fraction in old stellar populations ($\gtrsim 10 \text{ Gyr}$), with respect to velocity dispersion (left) and average age (right). The blue, green, and red lines correspond to IGV, mGV, and uGV galaxies, respectively. Results are shown for the 4000 \AA break selection (left) and the colour selection (right) of GV galaxies.

biased towards the most luminous stars. Mass-weighted parameters provide a more physical interpretation of the SFHs. The analysis is based on models with a fixed IMF, namely Chabrier (2003). We stress that within the velocity dispersion probed by this sample, no significant variations from a ‘standard’ IMF are expected (see e.g. Ferreras et al. 2013; La Barbera et al. 2013).

Fig. 12 is the equivalent of the best-fitting stellar parameters shown in Fig. 8 for the mass-weighted case, using the same line and colour coding. Similarly to the luminosity-weighted values, a general increase is found in average age with velocity dispersion but the absolute values are higher, as expected, and plateau at the massive end. Regarding GV subregions, we also find here more affinity between IGV and mGV, whereas uGV

galaxies appear older. This result is consistent regardless of the GV selection method, confirming that a selection based on the 4000 \AA break provides a homogeneous population. An increased scatter is evident in the mass-weighted estimates, partly due to the added uncertainties regarding the translation from light to mass. The Δt parameter shows a significant difference with respect to the luminosity-weighted counterpart, with overall high values and a decreasing trend with velocity dispersion, and no segregation regarding GV location (i.e. IGV, mGV, and uGV). Note, though, there is an anticorrelation that is weaker in comparison to Fig. 8. Estimates of average metallicity are now higher and appear rather flat with respect to velocity dispersion, within error bars.

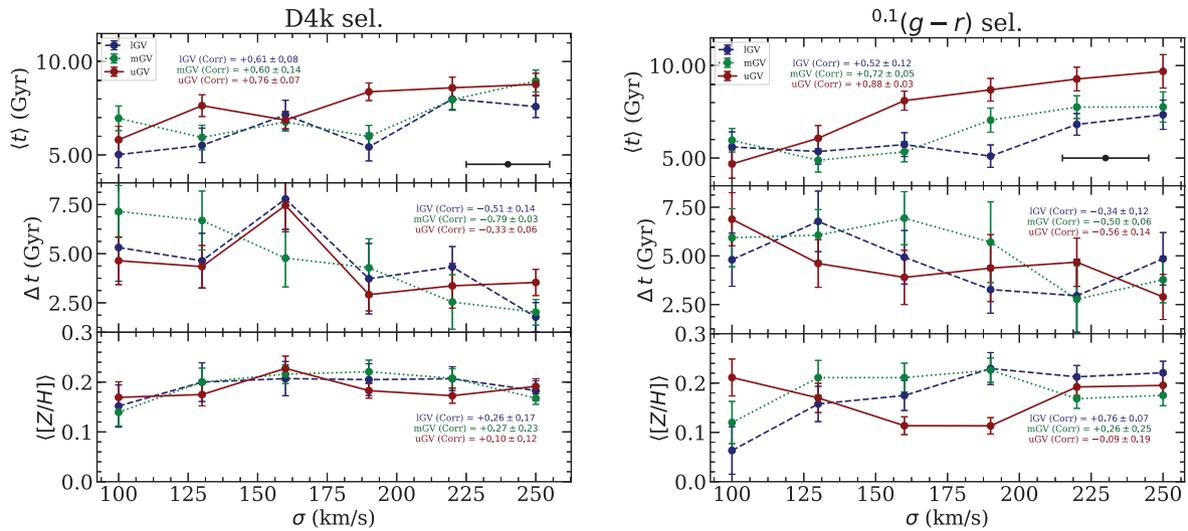


Figure 12. This is the equivalent of Fig. 8, showing mass-weighted parameters.

5 DISCUSSION

This paper looks in detail at the stellar population properties of green valley galaxies, selected with a new methodology based on the 4000 Å break strength (A19), and contrasts the results with respect to the traditional approach based on dust-corrected broadband colours. In this section, we briefly explore the implications of this analysis.

5.1 Dust-related systematics

The traditional selection of GV galaxies, based on colours derived from broad-band photometry, is affected by dust attenuation. In order to remove the effect of dust, a model is applied to derive a colour correction term. However, these corrections are subject to uncertainties that depend on the model fitting as well as on additional systematics related to the details of dust attenuation in galaxies. It is worth emphasizing that the net effect of dust is to impose an effective, wavelength-dependent attenuation law. However, in detail, it is a result of a wide range of mechanisms involving scattering and absorption of photons from the illuminating source (i.e. the underlying stellar populations) by the dust particles. The effective attenuation depends not only on the composition of dust but also on its distribution within the galaxy (see e.g. Galliano, Galametz & Jones 2018). The dust is typically concentrated around star-forming sites and motivates the birth cloud model, where a time-dependent dust attenuation provides a suitable description of the net attenuation law (see e.g. Charlot & Fall 2000). Observationally, star-forming galaxies feature a wide range of effective attenuation laws beyond the standard ones that fit the Milky Way average extinction curve (Cardelli et al. 1989) or the average attenuation of star-burst galaxies (Calzetti et al. 2000). The variation of the parameters that describe the attenuation law also appear to correlate (Narayanan et al. 2018; Tress et al. 2018). Therefore, such trends can lead to significant systematics in the dust correction.

Our comparison of GV galaxies between the dust-corrected colour selection and our proposed 4000 Å break strength selection enables us to assess the role of these systematics. In Appendix B, we quantify the dependence of the two observables chosen to select GV galaxies, on dust attenuation, using a simple attenuation law parametrized by the colour excess.

Table A1, in the appendix, shows the fraction of galaxies in the IGV and uGV, when selected according to either D4k or colour, with the latter shown with and without a dust correction. A graphical description of this table can be found in fig. 3 of A19. Note the D4k-selected GV yields a larger population of SF galaxies, than the *uncorrected* colour selection, especially towards high velocity dispersion ($\sigma \sim 200 \text{ km s}^{-1}$), along with a lower percentage of Q galaxies. Such a trend could be down to two reasons. First, dust could have reddened the galaxies to different amounts, so that SF galaxies occupy a wider region, leading to broader Gaussian PDFs when performing a colour-based selection. Secondly, due to our GV definition being dependent on the PDF of SF galaxies, the GV might have been shifted towards the RS in the colour-based approach. This explains the large (small) percentage of Qs (SF) population in IGV 72.5 ± 13.5 per cent (7.5 ± 4.3 per cent) and uGV 82.2 ± 13.5 per cent (8.9 ± 4.4 per cent), at the highest velocity dispersion ($220 < \sigma < 250 \text{ km s}^{-1}$).

The introduction of a dust correction makes the D4k- and colour-based selections closer together (see also fig. 3 of A19), illustrating the importance of dust correction when using colours. In more detail, note that the dust-corrected colour-based GV gives a lower fraction of Q galaxies in both IGV and uGV, with respect to the D4k selection. Although this might seem counter-intuitive, note that the largest effect when applying the dust correction of the colours is to increase the number of SF galaxies. Therefore, we deduce that most of the galaxies that appear on the GV after the dust correction is applied originate from the RS defined by the dust-uncorrected classification – as the effect of the correction is always to make the colours bluer. Another interesting trend can be seen when going from intermediate ($\sigma = 160\text{--}190 \text{ km s}^{-1}$), to high ($\sigma = 190\text{--}220 \text{ km s}^{-1}$) velocity dispersion, where we see an increase in the SF population in both D4k and dust-corrected $^{0.1}(g-r)$ selection of IGV and uGV. Note this trend is not seen in the dust uncorrected $^{0.1}(g-r)$ selection.

Moreover, note the difference in the line strengths between the full GV stacks and those consisting exclusively of Q galaxies – shown in Figs 6 and 7. The D4k-selected sample shows a more homogeneous distribution, in contrast with the larger variations found in the colour-based selection. These results illustrate the highly non-trivial issue of the systematics expected in the selection

of GV galaxies, and leads us to adopt the D4k selection as a more robust representation of the GV.

5.2 Interpretation of the GV as a transition region

We now take the D4k-selected GV as our standard sample. The differences in the stellar population properties of the three different areas of the GV, at fixed velocity dispersion, reflect the nature of the GV as a transition phase. The line strength results allow us to see in a model-independent way these variations. Fig. 2 shows a substantial difference in the higher order Balmer lines, especially $H\delta_F$, with respect to the other indices. This line is especially sensitive to recent episodes of star formation (see e.g. Martin et al. 2007) and thus may imply, when considering stacked spectra, that the contribution from rejuvenated galaxies dominates the flux, especially at high-velocity dispersion. Also note that at low-velocity dispersion, the trend of $H\delta_F$ is smoother, tentatively meaning that a smoother decaying (or truncated) star formation is in operation, suggesting a quenching mechanism – of otherwise younger populations – at the low-mass end.

Further supporting the results from line strength analysis, the population constraints based on spectral fitting (Fig. 8), give further evidence towards rejuvenation at high-velocity dispersion: the parameter Δt is defined as an estimator of the width of the stellar age distribution, and stays at $\Delta t \lesssim 2$ Gyr for $\sigma < 170$ km s⁻¹ (luminosity-weighted) – corresponding to a more compact age distribution – followed by very large values of Δt at the massive end, as expected from the presence of two or more disjoint star formation events across cosmic time, expected when rejuvenation produces a significant young component. Moreover, Fig. 11 emphasizes that the fraction of old (>10 Gyr) stars in uGV galaxies is high in massive galaxies and low at small velocity dispersion. Therefore, in this SDSS-based, low-redshift sample, quenching appears at late cosmic times in low-mass galaxies, whereas at the massive end one can only measure recent rejuvenation events on an otherwise old population. The mass-weighted results (Fig. 12) feature more scatter – as expected from the added uncertainties in Υ_* , when converting the SSP contributions into mass fractions – but interestingly produce a *decreasing* trend of Δt with velocity dispersion, implying that the rejuvenation events at the massive end cannot involve a large mass fraction of young stars. Nelson et al. (2018) explored the fractional contribution of rejuvenated galaxies in the IllustrisTNG simulation, finding that ~ 10 per cent of the subset of massive galaxies ($M_*/M_\odot > 10^{11} M_\odot$) have undergone rejuvenation once and ~ 1 per cent have experienced more than one rejuvenation event. Note our analysis shows rejuvenation to be dominant in stacked spectra at the massive end. However, the percentage of different types of galaxies in the stacks (Table A1) are roughly in agreement with the numerical simulations. Focusing on the uGV at high-velocity dispersion ($220 < \sigma < 250$ km s⁻¹), we find 19 per cent are star-forming galaxies. If we assume that a fraction of these SF galaxies are simply transitioning from BC to RS, with the remainder representing rejuvenation events, i.e. galaxies that have dropped down from RS, we might find similar fractions of rejuvenated systems as those found in the literature (Thomas et al. 2010; Nelson et al. 2018). A similar argument can be made for galaxies in lGV and mGV. However, the fractional contribution from star-forming galaxies is higher, and we expect a smaller contribution from rejuvenation events.

Regarding metallicity, we recover the standard mass–metallicity relation, as shown in Fig. 8. Although on a speculative tone, note the metallicity trend between uGV and lGV gets inverted between low- and high- velocity dispersion (in the luminosity-weighted

version). Such a trend would be a consequence of fresh, lower metallicity gas contributing to the rejuvenation events at the massive end of the sample.

Concerning the transition from BC to RS, previous work from the literature indicates a rapid evolution through the GV due to its sparsity (see e.g. Baldry et al. 2004; Taylor et al. 2015). However, this transition time depends on morphology. For instance, Schawinski et al. (2014) distinguish at least two morphologically related transition paths. Early-type galaxies are thought to traverse the GV in a rapid manner, quenching their star formation very quickly and moving on to the RS, while, in contrast, late-type galaxies are expected to undergo a slower quenching process. This is supported by Kelvin et al. (2018), where they look at structural variations with respect to colour and morphology, and argue in favour of inside–out formation, which is related to slow quenching, instead of a violent transformative event. Additionally, the observational constraints from the stacked spectra give time-scales between 2 and 4 Gyr (Phillipps et al. 2019). Using SSP-equivalent ages, the derived transition times are similar when stacking spectra regardless of nebular activity (Fig. 4). However, the difference between uGV and lGV luminosity-weighted average ages, from spectral fitting, results in a lower transition time ~ 1.0 Gyr. Interpreting Δt as a transition time-scale leads to a higher value $\gtrsim 5$ Gyr, with respect to Phillipps et al. (2019). Note this is to be expected as (i) STARLIGHT is very robust at tracing average parameters but produce weaker constraints on the details of the SFH; (ii) the parameter Δt traces the transition time in a slightly different manner, as it is very sensitive to recent bursting episodes (see Section 4.1 for details), while the methodology adopted by Phillipps et al. (2019) uses a fixed exponentially decaying SFH, thus making it less sensitive to rejuvenation effects.

In addition, state-of-the-art simulations give further support to a rapid transition through the GV; Wright et al. (2019) state that low-velocity dispersion galaxies feature relatively long quenching time-scales, $\tau_Q \gtrsim 3$ Gyr. This time-scale increases with velocity dispersion; but at the highest values of velocity dispersion, they find a drop to $\tau_Q \lesssim 2$ Gyr. As for the physical mechanism that produces this transition, it is stated that in low-mass galaxies it is mostly due to processes such as ram pressure stripping, while in more massive galaxies quenching operates through events such as stellar feedback (Wright et al. 2019). Finally, in the most massive systems, major mergers and quasar-mode AGNs are thought to quench star formation.

Finally, note the similar behaviour between lGV and mGV, in contrast with uGV for the D4k-selected sample. Interestingly, this behaviour between the different GV regions was also seen by Phillipps et al. (2019) in their study of ‘green’ galaxies using sSFR. They noted a lower transition time going from their ‘lGV’ to ‘mGV’ – selected by $sSFR_{lGV}/sSFR_{mGV} \sim 1.6$, giving 2 Gyr – with respect to their ‘mGV’ to ‘uGV’ – selected by $sSFR_{mGV}/sSFR_{uGV} \sim 2.5$, giving 3–4 Gyr. Fig. 13 shows the relation between D4k and sSFR (*top*) and between colour and sSFR (*bottom*). The relation with D4k presents a stronger correlation ($pcc = -0.925$) compared to colour ($pcc = -0.847$); therefore, it is not surprising that sSFR behaves in a similar manner to the 4000 Å break strength. This similarity reinforces the trends found here.

6 CONCLUSIONS

We present in this paper a detailed analysis of the recently proposed re-definition of green valley galaxies based on the 4000 Å break strength (A19), along with a comparison with the standard selection

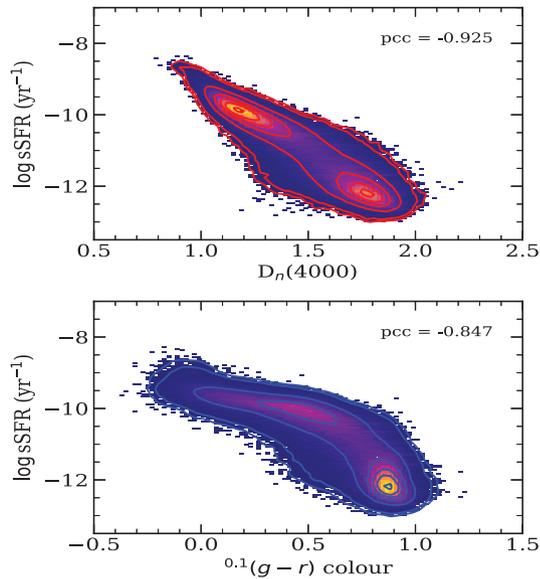


Figure 13. Relation between the sSFR and D4k (*top*) and sSFR and dust-corrected colour (*bottom*). The values denoted by pcc give the Pearson correlation coefficient. Note D4k shows a stronger (anti-)correlation with sSFR than colour.

based on dust-corrected colours from broad-band photometry. We make use of a large sample of high-quality spectroscopic data from the Sloan Digital Sky Survey (SDSS). The new definition adopts the well-known spectral index $D_n(4000)$ of Balogh et al. (1999), whereas the colour-based approach uses the SDSS-defined, dust-corrected colour $^{0.1}(g-r)$, i.e. K -corrected to redshift $z = 0.1$. The ‘population’ indicator, i.e. either $D_n(4000)$ or $^{0.1}(g-r)$, is plotted against velocity dispersion (σ), and the sample – defined between 70 and 250 km s $^{-1}$ – is split into six bins in σ . A probability-based approach is followed, where the star-forming and quiescent samples define a BC and a red sequence (RS), respectively, and an intermediate population, i.e. the green valley (GV) is introduced, and further split into three regions, lower (IGV), middle (mGV), and upper (uGV), based on the value of the population indicator.

Our results show overall consistent properties between the new definition, that is more resilient to potential systematics from the dust properties, and the dust corrected selection based on colour, with similar fractions between star-forming (SF), quiescent (Q), and AGN galaxies, with respect to velocity dispersion (see table A1 and fig. 3 in A19). However, when studying the stellar population property in more detail, differences are found between these two selection criteria that may affect the interpretation of galaxy evolution between the BC and RS regions. For instance, Figs 6 and 7 show the difference between the line strength indices in spectral stacks comprising either the full set of GV galaxies, or only the quiescent subsample. The colour-based selection produces a different, more complex population mixture, part of which may be a systematic bias caused by dust attenuation and the subsequent correction. We also find that the population properties of IGV and mGV galaxies are closer together, with the uGV sample representing an altogether different set, with older, less dusty and more extended population mixtures (see Figs 8 and 9).

The population analysis, based on spectral fitting of high-quality stacked data, reveals the standard age- and metallicity-positive correlations with velocity dispersion (or alternatively mass). Moreover, we define a parameter, Δt , that describes the width of the age

distribution, and find an interesting difference between low- and high- σ galaxies (Fig. 9). The former have rather narrow widths ($\Delta t \lesssim 0.3$ Gyr), whereas the latter feature more extended distributions ($\Delta t \gtrsim 4$ Gyr). This result is consistent with the idea that at the low-mass end, the data reveal quenching of star formation, whereas massive galaxies display significant (luminosity weighted) late events, which would imply rejuvenation. The mass-weighted equivalent (Fig. 12), although presenting more uncertainty from the conversion of light into mass, confirms that these events do not contribute very large amounts in terms of the mass fraction.

ACKNOWLEDGEMENTS

Funding for SDSS-III has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, and the U.S. Department of Energy Office of Science. The SDSS-III web site is <http://www.sdss3.org/>.

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SUPPORTING INFORMATION

Supplementary data are available at *MNRAS* online.

GViD_TabC1.csv

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APPENDIX A: FRACTIONS ACCORDING TO NEBULAR ACTIVITY

Table A1 shows the distribution of galaxy spectra in the upper (uGV) and lower (lGV) green valley, with respect to velocity dispersion, split according to nebular activity, following the BPT standard classification (Baldwin et al. 1981). For reference, we show three selection criteria, from top to bottom, the 4000 Å break strength (adopted in this paper), the uncorrected ($g - r$) colour evaluated at a fiducial redshift of $z = 0.1$, and the dust-corrected colour, all measured within the SDSS spectroscopic fibre. A graphical version of this table can be found in fig. 3 of A19.

Table A1. Number of SDSS galaxy spectra in the upper and lower sections of the green valley, following the definition of GV based on the 4000 Å break strength. The table also shows the fractional contribution (as percentages) with respect to the ‘spectral activity’, classified as star-forming (labelled SF; BPT flag 1 or 2); quiescent (labelled Q; BPT flag –1), or Active Galactic Nucleus, including LINER emission (labelled AGN; BPT flag 4 or 5).

σ (km s ⁻¹)	No. Gal	Lower GV			Upper GV			
		$f(\text{SF})$ per cent	$f(\text{Q})$ per cent	$f(\text{AGN})$ per cent	$f(\text{SF})$ per cent	$f(\text{Q})$ per cent	$f(\text{AGN})$ per cent	
D4k selection								
70–100	4265	95.1 ± 1.5	1.3 ± 0.2	3.6 ± 0.3	3845	70.0 ± 1.3	7.3 ± 0.4	22.6 ± 0.8
100–130	2369	77.8 ± 1.8	3.2 ± 0.4	19.1 ± 0.9	2627	42.2 ± 1.3	17.3 ± 0.8	40.5 ± 1.2
130–160	1078	45.8 ± 2.1	8.2 ± 0.9	46.0 ± 2.1	1344	24.5 ± 1.3	25.7 ± 1.4	49.8 ± 1.9
160–190	500	26.6 ± 2.3	17.0 ± 1.8	56.4 ± 3.4	631	13.8 ± 1.5	39.5 ± 2.5	46.8 ± 2.7
190–220	190	33.2 ± 4.2	25.3 ± 3.6	41.6 ± 4.7	254	14.6 ± 2.4	51.2 ± 4.5	34.3 ± 3.7
220–250	118	24.6 ± 4.6	28.8 ± 4.9	46.6 ± 6.3	117	19.7 ± 4.1	47.0 ± 6.3	33.3 ± 5.3
Colour selection ^{0.1} ($g - r$) (no dust correction)								
70–100	3384	95.7 ± 1.7	1.7 ± 0.2	2.6 ± 0.3	3174	83.9 ± 1.6	7.7 ± 0.5	8.3 ± 0.5
100–130	1844	81.1 ± 2.1	8.5 ± 0.7	10.5 ± 0.8	1824	56.2 ± 1.8	25.4 ± 1.2	18.4 ± 1.0
130–160	813	52.6 ± 2.5	24.8 ± 1.7	22.5 ± 1.7	953	25.6 ± 1.6	52.4 ± 2.3	22.0 ± 1.5

Table A1 – *continued*

σ (km s ⁻¹)	No. Gal	$f(\text{SF})$ per cent	$f(\text{Q})$ per cent Lower GV	$f(\text{AGN})$ per cent	No. Gal	$f(\text{SF})$ per cent	$f(\text{Q})$ per cent Upper GV	$f(\text{AGN})$ per cent
160–190	311	30.5 ± 3.1	44.7 ± 3.8	24.8 ± 2.8	353	16.7 ± 2.2	65.4 ± 4.3	17.8 ± 2.2
190–220	103	18.4 ± 4.2	61.2 ± 7.7	20.4 ± 4.4	110	10.0 ± 3.0	74.5 ± 8.2	15.5 ± 3.7
220–250	40	7.5 ± 4.3	72.5 ± 13.5	20.0 ± 7.1	45	8.9 ± 4.4	82.2 ± 13.5	8.9 ± 4.4
Colour selection ^{0.1} ($g - r$) (dust corrected)								
70–100	3534	94.5 ± 2.3	0.8 ± 0.2	4.7 ± 0.3	3233	78.4 ± 2.1	4.2 ± 0.4	17.6 ± 0.8
100–130	1623	69.2 ± 2.7	3.8 ± 0.5	27.0 ± 1.5	1722	44.8 ± 1.9	13.6 ± 0.9	41.6 ± 1.8
130–160	1028	40.8 ± 2.4	6.7 ± 0.8	52.5 ± 2.8	1194	22.2 ± 1.5	22.7 ± 1.5	55.1 ± 2.7
160–190	487	23.8 ± 2.5	12.3 ± 1.7	63.9 ± 4.6	586	14.0 ± 1.6	32.6 ± 2.7	53.4 ± 3.7
190–220	231	31.6 ± 4.2	10.0 ± 2.2	58.4 ± 6.3	266	24.1 ± 3.3	42.1 ± 4.7	33.8 ± 4.1
220–250	110	27.7 ± 5.6	20.9 ± 4.8	51.8 ± 8.5	125	25.6 ± 5.1	36.8 ± 6.3	37.6 ± 6.4

APPENDIX B: THE EFFECT OF DUST

To illustrate the dependence of the 4000 Å break and colour selection of GV galaxies with respect to dust attenuation, we compare in Fig. B1 the difference between the trends found for the location of the BC (blue); GV (green), and RS (red), as a function of velocity dispersion. Each one corresponds to the mean of the PDF associated with each sub-population (see Section 2.2). The top and bottom panels display the difference between BC, GV, and RS with and without dust correction for $D_n(4000)$ and colour, respectively. To test for systematics, we apply either a Milky Way extinction law (Cardelli et al. 1989, dashed lines) or a Calzetti et al. (2000, solid lines) law. Note the small difference when using the selection based on break strength (top panels), especially on

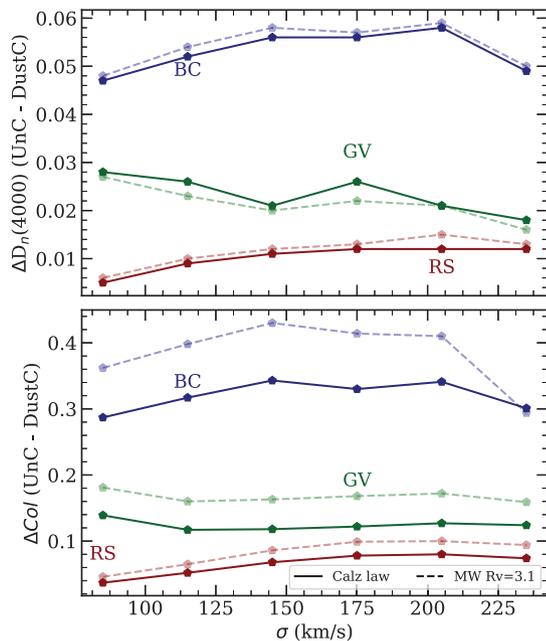


Figure B1. Dependence of 4000 Å break strength (top) and $(g - r)$ colour (bottom) on dust attenuation. The blue, green, and red data points show the difference in 4000 Å break strength (top) and colour (bottom), after correction for dust attenuation. The solid and dashed lines represent the two attenuation laws considered, Calzetti et al. (2000) and Cardelli et al. (1989), respectively.

GV galaxies, at the level $\Delta D_n(4000) < 0.03$, whereas the colours (bottom panels) are not only substantially affected – with correction terms comparable to the actual separation between BC and RS, but are also heavily dependent on the attenuation law adopted, and thus prone to systematics from the variance regarding the details of dust composition and geometry.

APPENDIX C: THE EFFECT OF APERTURE

This study focuses on the use of spectroscopic data of the classic SDSS data set, therefore confined to a 3 arcsec diameter fibre. For consistency, our comparison with respect to colour, ^{0.1}($g - r$), is done within the same aperture. This could introduce a bias with respect to stellar mass (or velocity dispersion), as more massive, and generally larger, galaxies would have a lower fraction of the light from their stellar populations inside the fibre. To assess this bias, we use the JHU/MPA catalogue (Kauffmann et al. 2003) and compare the colour within the aperture with the modelled colour for the whole galaxy (Fig. C1). The difference between these two definitions of colour shows a minimal trend with stellar mass. Due to $D_n(4000)$ tracing, the average age in a similar manner to colour,

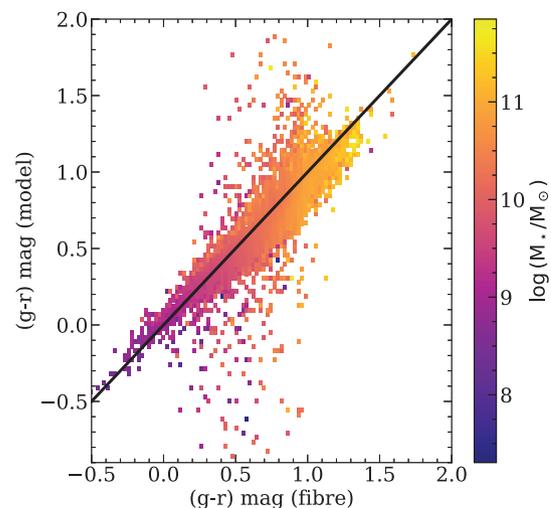


Figure C1. Relation between the colour measured inside the 3 arcsec fibre, and the one from a surface brightness modelling to the whole galaxy (i.e. determined from the official SDSS model magnitudes). The data are colour coded with respect to stellar mass (colour bar on the right). The solid black line illustrates a 1:1 correspondence.

we expect a similar, minor, difference between $D_n(4000)$ inside the fibre and $D_n(4000)$ measured in the whole galaxy.

Though there is no bias in relation to stellar mass, we do see an offset between the colour in the fibre and that of the whole galaxy. Therefore, a similar behaviour in $D_n(4000)$ is expected. The inconsistency in colour between fibre and whole galaxy is partially due to biases from surface brightness modelling, as well as from the presence of gradients in population content. One physical mechanism that can give rise to these gradients is the inside–out/outside–in quenching. For instance, inside–out quenching will result in younger populations outside of the reach of the fibre (Kelvin et al. 2018). The opposite will be true when galaxy is undergoing outside–in quenching. Another cause for such behaviour would be galaxy morphology. More specifically, spiral galaxies with a strong bulge will produce a greater difference between fibre and whole galaxy estimates of both the colour and $D_n(4000)$.

APPENDIX D: SDSS GREEN VALLEY PROBABILITY CATALOGUE

Adopting the methodology laid out in A19, we are able to assign to each galaxy, on the $D_n(4000)$ versus velocity dispersion plane, a probability of it belonging to the BC ($\hat{\mathcal{P}}_{BC}$), Green Valley ($\hat{\mathcal{P}}_{GV}$), or Red Sequence ($\hat{\mathcal{P}}_{RS}$). Each probability can be written as

$$\hat{\mathcal{P}}_k = \eta_k \mathcal{P}_k(\pi; \sigma), \quad (\text{D1})$$

where \mathcal{P}_k is given by equation (2) and η_k is a weight factor dependent on the number of galaxies in BC, GV, or RS.

To assign a probability to an individual galaxy, we firstly obtain the PDF averages: μ_{BC} , μ_{GV} , μ_{RS} , and ‘widths’: s_{BC} , s_{GV} , and s_{RS} for 11 bins from 50 to 350 km s^{−1}. Then we interpolate between the velocity dispersion bins with a third-order polynomial that enables us to find the effective μ_k and s_k in each group, BC, GV, and RS, at any velocity dispersion. For each galaxy, we obtain its $\mathcal{P}_k(\mathcal{G}_i)$, along with $\mu_k(\mathcal{G}_i)$ and $s_k(\mathcal{G}_i)$. To determine η_k , we select all galaxies with velocity dispersion within an interval centred at the σ of the chosen galaxy, with width $\Delta\sigma = 15$ km s^{−1}, and then assign them either to the BC, GV, or RS, following the methodology described in A19, and in Section 2.2 of this paper. For any galaxy sitting

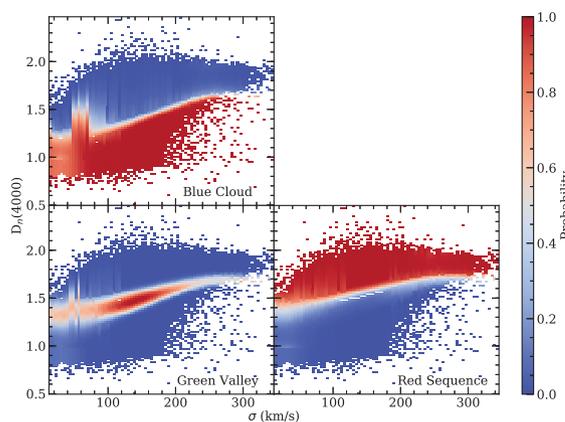


Figure D1. The probability of galaxies belonging to the BC (top left), Green Valley (bottom left), and Red Sequence (bottom right). Blue colours represent galaxies with a low probability of residing in the three regions, as labelled, while red shows high probability (see colour bar for reference). For ease of visualization, the resulting density plots have been modified with a Gaussian smoothing kernel.

on adjacent regions, we assign them evenly to their overlapping regions; e.g. if they overlap between BC and GV, they are equally likely to count towards the BC or GV. Thus, we obtain η_k for each galaxy. Once we obtain $\hat{\mathcal{P}}_k$, we normalize the total probability to unity. Note we assign galaxies with $D_n(4000) > 1.99$, $\hat{\mathcal{P}}_{RS} = 1$, and $\hat{\mathcal{P}}_{BC} = \hat{\mathcal{P}}_{GV} = 0$, as we know that galaxies with a high 4000 Å break strength are old and quiescent. Likewise galaxies with $D_n(4000) < 0.8$ are assigned $\hat{\mathcal{P}}_{BC} = 1$ and $\hat{\mathcal{P}}_{GV} = \hat{\mathcal{P}}_{RS} = 0$.

A small number of galaxies from the catalogue is shown in Table D1 for reference. The full catalogue can be found in the online version of the paper. Note owing to the methodology used, the probabilities presented here are not unique solutions, but a realization of the three groups. Thus, if one were to carry out the outlined steps, the results should not be identical, but statistically equivalent. Fig. D1 illustrates the probability density of galaxies residing in BC, GV, or RS, as presented in A19 and this paper.

Table D1. Probabilities of BC, GV, or RS membership assigned to each galaxy from the SDSS set. This table shows a small portion of the full set, giving the SDSS spectral identification (plate, Julian date, and fibre ID) along with the 4000 Å break strength and velocity dispersion (measured within the 3 arcsec diameter fibres of the spectrograph). The final three columns list the normalized probability of belonging to either BC, Green Valley, or Red Sequence, respectively, using the methodology presented here and in A19.

Plate	SDSS ID		$D_n(4000)$	Velocity dispersion (km s ^{−1})	Probabilities		
	MJD	Fibre ID			$\hat{\mathcal{P}}_{BC}$	$\hat{\mathcal{P}}_{GV}$	$\hat{\mathcal{P}}_{RS}$
315	51663	560	1.012	64.5	0.970	0.009	0.021
326	52375	86	1.584	99.2	0.001	0.026	0.973
326	52375	119	1.509	104.6	0.011	0.360	0.629
326	52375	150	1.777	168.2	0.000	0.000	1.000
327	52294	147	1.651	147.9	0.001	0.013	0.986

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