



HAL
open science

Implementation of counted layers for coherent ice core chronology

Bénédicte Lemieux-Dudon, Lucie Bazin, Amaelle Landais, Habib Toyé Mahamadou Kele, Myriam Guillevic, Philippe Kindler, Frédéric Parrenin, Patricia Martinerie

► **To cite this version:**

Bénédicte Lemieux-Dudon, Lucie Bazin, Amaelle Landais, Habib Toyé Mahamadou Kele, Myriam Guillevic, et al.. Implementation of counted layers for coherent ice core chronology. *Climate of the Past*, 2015, 11 (6), pp.959-978. 10.5194/cp-11-959-2015 . insu-01203665

HAL Id: insu-01203665

<https://insu.hal.science/insu-01203665>

Submitted on 23 Sep 2015

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Implementation of counted layers for coherent ice core chronology

B. Lemieux-Dudon¹, L. Bazin², A. Landais², H. Toyé Mahamadou Kele¹, M. Guillevic^{2,3}, P. Kindler⁴, F. Parrenin⁵, and P. Martinerie⁵

¹Laboratoire Jean Kuntzmann, Grenoble, France

²Laboratoire des Sciences du Climat et de l'Environnement, UMR8212, CEA-CNRS-UVSQ, Orme des Merisiers, Gif sur Yvette, France

³Centre for Ice and Climate, Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark

⁴Climate and Environmental Physics, Physics Institute & Oeschger Centre for Climate Change Research, University of Bern, Bern, Switzerland

⁵Laboratoire de Glaciologie et Géophysique de l'Environnement, UMR5183, Univ. Grenoble Alpes-CNRS, Grenoble, France

Correspondence to: B. Lemieux-Dudon (benedicte.lemieux@imag.fr)

Received: 22 July 2014 – Published in Clim. Past Discuss.: 28 August 2014

Revised: 1 June 2015 – Accepted: 3 June 2015 – Published: 25 June 2015

Abstract. A recent coherent chronology has been built for four Antarctic ice cores and the NorthGRIP (NGRIP) Greenland ice core (Antarctic Ice Core Chronology 2012, AICC2012) using a Bayesian approach for ice core dating (Datice). When building the AICC2012 chronology, and in order to prevent any confusion with official ice core chronology, the AICC2012 chronology for NGRIP was forced to fit exactly the GICC05 chronology based on layer counting. However, such a strong tuning did not satisfy the hypothesis of independence of background parameters and observations for the NGRIP core, as required by Datice. We present here the implementation in Datice of a new type of markers that is better suited for constraints deduced from layer counting: the duration constraints. Estimating the global error on chronology due to such markers is not straightforward and implies some assumption on the correlation between individual counting errors for each interval of duration. We validate this new methodological implementation by conducting twin experiments and a posteriori diagnostics on the NGRIP ice core. Several sensitivity tests on marker sampling and correlation between counting errors were performed to provide some guidelines when using such a method for future dating experiments. Finally, using these markers for NGRIP in a five-core dating exercise with Datice leads to new chronologies that do not differ by more than 410 years

from AICC2012 for Antarctic ice cores and 150 years from GICC05 for NGRIP over the last 60 000 years.

1 Introduction

The reference timescale for Greenland ice cores, GICC05, has been obtained by layer counting back to 60 ka (thousands of years before 1950; Vinther et al., 2006; Rasmussen et al., 2006; Andersen et al., 2006; Svensson et al., 2008). This chronology is absolute, with an increasing associated uncertainty with depth, reaching more than 2.6 at 60 ka. Because this chronology is based on layer counting, the duration of events is rather precise, even for old ages, with an average relative counting error of 0 to 20 %. The uncertainty of the GICC05 age scale, however, cumulates the counting error through the maximum counting error (MCE). It maximizes this uncertainty since it assumes that the layer-counting error is fully correlated from one interval to another (Rasmussen et al., 2006).

This chronology has been used as a reference for many records of the North Atlantic region (Austin et al., 2012; Walker et al., 2012; Austin and Hibbert, 2012; Davies et al., 2012; Blockley et al., 2012b). It has also been used as a basis over the last 60 kyr for the recent construction of the coherent

Antarctic Ice Core Chronology (AICC2012) gathering one Greenland ice core (NorthGRIP – NGRIP) and four Antarctic ice cores (EPICA Dome C – EDC; EPICA Dronning Maud Land – EDML; Talos Dome ice core – TALDICE; and Vostok; Bazin et al., 2013; Veres et al., 2013). For the construction of AICC2012 with the Bayesian tool Datic (Lemieux-Dudon et al., 2009, 2010), we have imposed a 1σ deviation for NGRIP of 50 years maximum. Even if such a constraint is artificially too strong compared to the true uncertainty of GICC05, it forces a coherency within 5 years between the NGRIP AICC2012 chronology and GICC05.

Still, the strong tie of AICC2012 to GICC05 has led to some technical problems when optimizing the chronology with Datic. Three glaciological parameters are indeed optimized during this process: accumulation rate, ice thinning and lock-in depth (i.e. the depth at which air is trapped when snow is sufficiently compacted). The Bayesian approach requires starting with first-guess (background) scenarios for the three parameters. They are then modified within their imposed variance range so that the final chronology fits the absolute and relative age constraints for each ice core within error bars.

In practice, to force the NGRIP AICC2012 chronology to fit the GICC05 age scale, the modelled thinning function and accumulation rate of the GICC05 chronology (hereafter DJ–GICC05 scenarios; Vinther et al., 2006; Rasmussen et al., 2006; Andersen et al., 2006; Svensson et al., 2008) have been imposed as background scenarios in Datic. The variance associated with these background scenarios was set to be very small in order to prevent any deviation from the GICC05 timescale.

Even if the uncertainty of the GICC05 timescale is well constrained, this is not true for the DJ–GICC05 scenarios of thinning and accumulation. The thinning function is deduced from a simple Dansgaard–Johnsen (DJ) ice flow model (Dansgaard and Johnsen, 1969; Andersen et al., 2006) that has been parameterized to obtain the best match between the modelled and observed depth–age horizons in the ice cores. Then, the thinning function calculated with the DJ model is used together with the observed annual layer thicknesses to produce an accumulation rate history. No uncertainty value is associated with the reconstructions of thinning and accumulation rate in Greenland ice cores, but thinning and accumulation reconstructed from such 1-D ice flow models are only a first approximation (Cutler et al., 1995; Parrenin et al., 2004, 2007).

Recently, studies combining air isotopic measurements ($\delta^{15}\text{N}$ of N_2) with firnification models have suggested that, both in NGRIP and NEEM, the accumulation rates reconstructed from the GICC05 or ss09sea chronologies, through layer counting and the DJ flow model, were overestimated for the last glacial period (Huber et al., 2006; Guilleveic et al., 2013; Kindler et al., 2014). Indeed, $\delta^{15}\text{N}$ of N_2 of air trapped in an ice core indicates the depth and the amplitude of abrupt temperature changes in the gas phase through

thermal fractionation. The depth difference between the same abrupt temperature changes recorded in the ice phase through ice $\delta^{18}\text{O}$ increase/decrease and in the gas phase through a positive/negative $\delta^{15}\text{N}$ peak is called delta-depth (Δdepth). Moreover, in the absence of any abrupt temperature change and convection at the top of the firn, the $\delta^{15}\text{N}$ gives an indication of the past lock-in depth (LID) through gravitational fractionation. A firnification model including heat diffusion and mainly driven by temperature and accumulation rate can reproduce long-term and abrupt $\delta^{15}\text{N}$ variations with depth for Greenland ice cores. The same would not be true in Antarctica, where a strong discrepancy between firnification models and data is observed (Landais et al., 2006). For NGRIP, it has been shown that the $\delta^{15}\text{N}$ profile is best reproduced when the ss09sea accumulation rate is decreased by $\sim 20\%$ over the period 20 to 60 ka (Kindler et al., 2014; Huber et al., 2006).

It thus appears that the way NGRIP was implemented in the Datic tool for the AICC2012 chronology is not optimal. In addition to GICC05 chronological uncertainties that were not taken into account by construction, imposing the DJ–GICC05 accumulation rate and thinning scenarios with artificially reduced variances most probably led to incorrect output scenarios for these glaciological parameters.

In this paper, we propose an improvement of Datic to better implement the chronological uncertainties. Markers of duration are integrated in Datic with associated counting error. This allows for the strong constraints on thinning and accumulation rate to be relaxed. It also allows the NGRIP chronology to differ from GICC05 chronology within its error bars.

The outline of the manuscript is as follows. First, a methodological section presents and validates the improvements made to the Datic tool in order to integrate the duration constraints with their uncertainties. Then, we discuss different ways to implement the counting errors within the global chronological uncertainty. We also present some sensitivity experiments using the modified Datic tool for optimizing the sampling strategy and correlation between counting errors. Finally, we focus on how this new version of Datic modifies the NGRIP and the four Antarctic ice core chronologies compared to AICC2012.

2 Implementation of constraints from counted layers in Datic

2.1 Methodology

The purpose of the following section is to describe the modifications implemented in Datic (Lemieux-Dudon et al., 2009, 2010) to take into account the duration constraints. This type of marker enables one to constrain the duration of depth intervals along ice cores. This constraint is applied by feeding Datic with the beginning and end depths of the

interval, its duration, the duration uncertainty, and optionally the error correlation between markers.

Datice aims at obtaining the best age model scenario by formulating an optimization problem with a cost function that is accounted for by two main types of constraint: the palaeo-observations \mathbf{Y} and a first-guess age model \mathbf{X}^b (referred to as the prior or background; Ide et al., 1997). Datice requires that the background age model and the palaeo-observations be independent from each other, since the cost function J is derived from the Bayes theorem:

$$J(\mathbf{X}) = -\log(P(\mathbf{Y}|\mathbf{X})P_b(\mathbf{X})) \quad (1)$$

where $P(\mathbf{Y}|\mathbf{X})$ and $P_b(\mathbf{X})$ are the likelihood and prior probability distribution (Tarantola, 2005).

In practice, Datice is applied to several ice cores with a large set of palaeo-observations in order to calculate coherent chronologies for both the ice and gas phases. The chronologies are deduced from the scenarios of three glaciological parameters for each core indexed with k (Appendix Sect. A): (i) T_k the total thinning function, (ii) A_k the accumulation rate, and (iii) C_k the lock-in depth in ice equivalent (LIDIE). To run a Datice experiment, palaeo-observations and the background parameters $T_k^b(z)$, $A_k^b(z)$ and $C_k^b(z)$ must be provided with their respective uncertainties. The minimization of the cost function J enables one to refine the background by identifying correction functions $\tau_k(z)$, $\alpha_k(z)$ and $\gamma_k(z)$ at each depth level z_k :

$$T_k(z) = \tau_k(z) \cdot T_k^b(z), \quad (2)$$

$$A_k(z) = \alpha_k(z) \cdot A_k^b(z), \quad (3)$$

$$C_k(z) = \gamma_k(z) \cdot C_k^b(z). \quad (4)$$

From a particular set of correction functions, one can deduce a particular age model. Hereafter, a particular age model is written $\mathbf{X} = (\boldsymbol{\alpha}_k, \boldsymbol{\tau}_k, \boldsymbol{\gamma}_k)^T$.

The Datice cost function formulation (Eq. 5) relies on the following important statistical assumptions. In the prior probability distribution of Eq. (1), the parameters T_k , A_k and C_k are supposed to be independent and log-normally distributed, with medians equal to $T_k^b(z)$, $A_k^b(z)$ and $C_k^b(z)$, respectively. The prior probability distribution is further rewritten in terms of the correction functions (Eqs. 2, 3, 4), to which we apply the change of variable $\tilde{\mathbf{X}} = \log(\mathbf{X})$ in order to transform lognormal into normal probability distributions (pdf's; Tarantola, 2005). Using this change of variable, since observations of different types are supposed to be independent with either normal or log-normally distributed errors, the likelihood of Eq. (1) is itself a product of normal pdf's. Under these assumptions, the cost function J sums up quadratic terms (Eq. 5).

Until now, observation \mathbf{Y} could be of the following types: ice and gas age markers (^{ia} and ^{ga}), delta-depth markers (^{dd}), or ice and gas stratigraphic links (^{is} and ^{gs}; Lemieux-Dudon et al., 2010; Buiron et al., 2011; Veres et al., 2013; Bazin

et al., 2013). The application of the duration constraints (^{ad}) leads to an additional term in the cost function (Eq. 5), with special care to preserve the Datice hypothesis of no error correlation between (i) observations of different types, (ii) observations from different cores, or (iii) observations and background model scenarios:

$$\begin{aligned} J(\tilde{\mathbf{X}}) = & \sum_{k=1}^N (\tilde{\mathbf{X}}_k - \tilde{\mathbf{X}}_k^b)^T [\mathbf{B}]^{-1} (\tilde{\mathbf{X}}_k - \tilde{\mathbf{X}}_k^b) \\ & + \sum_{k=1}^N (\mathbf{Y}_k^{\text{dd}} - \mathbf{h}_k^{\text{dd}}(\tilde{\mathbf{X}}_k))^T [\mathbf{R}_k^{\text{dd}}]^{-1} (\mathbf{Y}_k^{\text{dd}} - \mathbf{h}_k^{\text{dd}}(\tilde{\mathbf{X}}_k)) \\ & + \sum_{k=1}^N (\mathbf{Y}_k^{\text{ia}} - \mathbf{h}_k^{\text{ia}}(\tilde{\mathbf{X}}_k))^T [\mathbf{R}_k^{\text{ia}}]^{-1} (\mathbf{Y}_k^{\text{ia}} - \mathbf{h}_k^{\text{ia}}(\tilde{\mathbf{X}}_k)) \\ & + \sum_{k=1}^N (\mathbf{Y}_k^{\text{ga}} - \mathbf{h}_k^{\text{ga}}(\tilde{\mathbf{X}}_k))^T [\mathbf{R}_k^{\text{ga}}]^{-1} (\mathbf{Y}_k^{\text{ga}} - \mathbf{h}_k^{\text{ga}}(\tilde{\mathbf{X}}_k)) \\ & + \sum_{k_1=1}^N \sum_{k_2=k_1+1}^N (\mathbf{h}_{k_2}^{\text{is}}(\tilde{\mathbf{X}}_{k_2}) - \mathbf{h}_{k_1}^{\text{is}}(\tilde{\mathbf{X}}_{k_1}))^T [\mathbf{R}_{k_1,k_2}^{\text{is}}]^{-1} \\ & (\mathbf{h}_{k_2}^{\text{is}}(\tilde{\mathbf{X}}_{k_2}) - \mathbf{h}_{k_1}^{\text{is}}(\tilde{\mathbf{X}}_{k_1})) \\ & + \sum_{k_1=1}^N \sum_{k_2=k_1+1}^N (\mathbf{h}_{k_2}^{\text{gs}}(\tilde{\mathbf{X}}_{k_2}) - \mathbf{h}_{k_1}^{\text{gs}}(\tilde{\mathbf{X}}_{k_1}))^T [\mathbf{R}_{k_1,k_2}^{\text{gs}}]^{-1} \\ & (\mathbf{h}_{k_2}^{\text{gs}}(\tilde{\mathbf{X}}_{k_2}) - \mathbf{h}_{k_1}^{\text{gs}}(\tilde{\mathbf{X}}_{k_1})) \\ & + \sum_{k=1}^N (\mathbf{Y}_k^{\text{ad}} - \mathbf{h}_k^{\text{ad}}(\tilde{\mathbf{X}}_k))^T [\mathbf{R}_k^{\text{ad}}]^{-1} (\mathbf{Y}_k^{\text{ad}} - \mathbf{h}_k^{\text{ad}}(\tilde{\mathbf{X}}_k)). \quad (5) \end{aligned}$$

In Eq. (5), the first term measures the distance between the current age model $\tilde{\mathbf{X}}$ and the background scenarios $\tilde{\mathbf{X}}^b$. The six following terms are related to the observation constraints and measure the distance between the current age model $\tilde{\mathbf{X}}$ and the observations \mathbf{Y} . Importantly, to map the current age model $\tilde{\mathbf{X}}$ to the observation \mathbf{Y} , we must introduce the non-linear observation operators \mathbf{h} . The background and observations uncertainties provided to Datice are stored in the background and observation error covariance matrices \mathbf{B} and \mathbf{R} (Appendix D1). The cost function terms are weighted according to the uncertainties specified in the \mathbf{B} and \mathbf{R} matrices. The cost function reaches a minimum value for a specific set of correction functions $\tilde{\mathbf{X}}^a$ (Eqs. 2, 3, 4). At this minimum, a trade-off is reached between the background and observation constraints. The new age scales are then deduced from the correction functions $\tilde{\mathbf{X}}^a$ (Appendix Sect. A). They are hereafter called analysed chronologies following the unified notation for data assimilation (Ide et al., 1997). By propagating the errors stored in the \mathbf{B} and \mathbf{R} matrices, Datice estimates the error associated with the age solution (Appendix Sect. D2). We refer to this error as the analysed error. Both the analysed age scales and analysed errors are highly sensitive to the errors specified in the \mathbf{B} and \mathbf{R} error covariance matrices.

In this article, we wish to design Datice experiments with duration constraints derived from the GICC05 counted layer chronology. In Sect. 2.3, we especially investigate the setting of the observation error covariance matrix \mathbf{R}^{ad} associated with these markers:

$$\mathbf{R}_{ij}^{\text{ad}} = \rho_{ij}^{\text{ad}} \sigma_i^{\text{ad}} \sigma_j^{\text{ad}}, \quad (6)$$

where $\mathbf{R}_{ij}^{\text{ad}}$ accounts for the error covariance between the i^{th} and j^{th} pair of markers Y_i^{ad} and Y_j^{ad} . σ_i^{ad} and σ_j^{ad} are their standard deviations and ρ_{ij}^{ad} is their error correlation coefficient.

2.2 Validation of Datice developments: twin experiments

In this section, twin experiments are performed to test the incorporation of duration constraints within the Datice tool. A twin experiment enables one to test any data assimilation system. It consists in the construction of some synthetic data and background by applying random perturbations of known statistical distribution to a given model scenario. The unperturbed model scenario is referred to as the “truth”. The aim of this validation method is to rebuild the truth by running the data assimilation system on the perturbed data and background.

In our case, we designed a twin experiment based on 51 simulations where the Datice system is run with the NGRIP ice core alone. The duration constraints are the only type of observation included. The GICC05 age scale is considered as the “truth”. We construct synthetic observations and backgrounds by applying random perturbations to the “true” GICC05 model scenario. The objective is to run the Datice system with the synthetic data as input and to rebuild GICC05 as accurately as possible.

Each twin experiment inputs are prepared using the following method. To build the 51 sets of synthetic markers of duration constraint \mathbf{Y}^{ad} , we first sample the “true” duration constraints $\mathbf{Y}^{\text{ad},t}$ from the GICC05 age scale every 100 years.

For this experiment, the markers $\mathbf{Y}^{\text{ad},t}$ represent the “truth” (superscript t) as extracted from the “true” age model GICC05. We then construct the observation error covariance matrix \mathbf{R}^{ad} (see Sect. 2.1) based on the MCE data under the assumption of full error correlation (see details in Sect. 2.3). To provide the markers of duration \mathbf{Y}^{ad} that will effectively be applied in the simulations, the “true” markers $\mathbf{Y}^{\text{ad},t}$ are perturbed within their uncertainty range through random normal perturbations specified according to the observation error covariance matrix \mathbf{R}^{ad} :

$$\mathbf{Y}^{\text{ad}} = \mathbf{Y}^{\text{ad},t} + \delta^{\text{ad}} \quad \text{with} \quad \delta^{\text{ad}} \sim \mathcal{N}(0, \mathbf{R}^{\text{ad}}). \quad (7)$$

In the same way, the 51 background scenarios are built from the “true” GICC05 thinning function and accumulation rate by applying random perturbations, with the particularity that

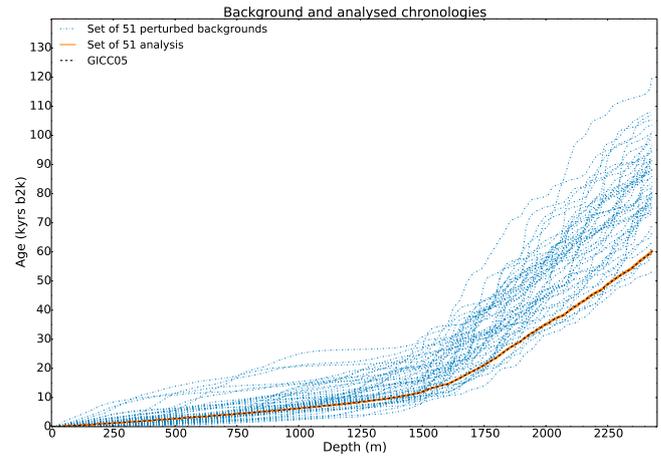


Figure 1. Twin experiments: 51 perturbed background chronologies (dashed blue lines) and the corresponding 51 analysed chronologies, i.e. output chronologies from Datice (orange lines). The GICC05 chronology (the “truth” in our twin experiments) is represented by the dashed black line for comparison.

thinning function and accumulation rate are log-normally distributed as discussed in Sect. 2.1. We construct the random lognormal perturbations δ_α and δ_τ on the basis of the background error covariance matrices \mathbf{B}_τ and \mathbf{B}_α , which are specified according to Bazin et al. (2013) with adapted values (see Table 4 and Appendix Sect. B):

$$\log(\delta_\tau) \sim \mathcal{N}(0, \mathbf{B}_\tau), \quad (8)$$

$$\log(\delta_\alpha) \sim \mathcal{N}(0, \mathbf{B}_\alpha), \quad (9)$$

where \mathbf{B}_α and \mathbf{B}_τ are the first two diagonal and uncorrelated blocks of matrix \mathbf{B} introduced in Eq. (5) of Sect. 2.1.

To construct the perturbed background thinning function T^b and accumulation rate A^b , the δ_α and δ_τ vectors are applied as multiplicative factors to the “true” GICC05 thinning function T_i^t and accumulation rate A_i^t at each depth level z_i (with index i running from 1 at the top of the core to n at the bottom):

$$T_i^b = \delta_{i,\tau} T_i^t, \quad (10)$$

$$A_i^b = \delta_{i,\alpha} A_i^t. \quad (11)$$

Figure 1 shows the large spread of the resulting perturbed background age scales (dashed lines) and a superimposition of the corresponding analysed age scales (orange lines). Figure 2 shows the difference between the set of analysed chronologies minus GICC05 (upper panel) and the error of the analysed chronologies, i.e. σ^a the a posteriori standard deviation calculated by Datice (lower panel). Histograms of the background and analysed chronologies are shown in Fig. 3 for the 1800 m depth level.

Figures 1, 2 and 3 all show the convergence toward GICC05 even though Datice is fed with perturbed background scenarios and duration constraints. In the Datice system, the calculation of the analysed error σ^a relies upon

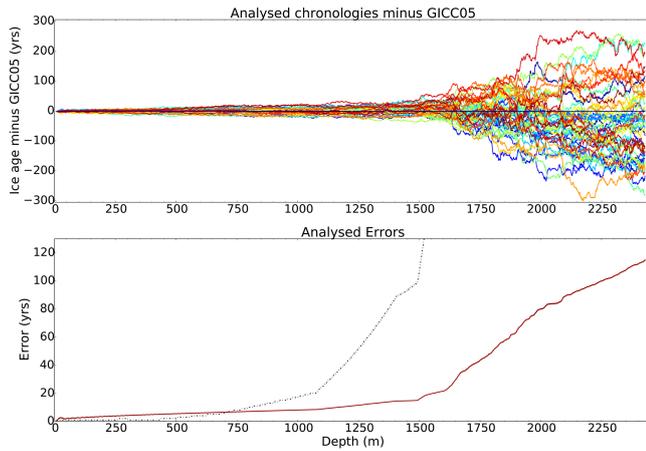


Figure 2. Twin experiments: 51 analysed chronologies, i.e. output chronologies from Datice. Top: comparison of the 51 analysed chronologies with GICC05. Bottom: the corresponding 51 analysed errors (red). The dashed black line represents the maximum counting error associated with GICC05 and considered as equivalent to a 2σ uncertainty.

the assumption of normally distributed errors. This may be a strong assumption. However, the histogram of analysed chronologies (i.e. output chronologies) is rather symmetric and centred on GICC05 compared to the very asymmetric histogram of the perturbed background age scales (Fig. 3). Moreover, at depth level 1800 m, 96% of the 51 output chronologies are located inside a $\pm 2\sigma^a$ envelope centred on GICC05 (Fig. 3). This result gives confidence in the methodology applied to calculate the analysed error (see Appendix Sect. E). A larger number of samples would be helpful to refine this analysis.

Finer diagnostics confirm the reliability of the Datice methodological developments. As investigated in Desroziers et al. (2009), several levels of a posteriori diagnostics can be applied on data assimilation system on the basis of ensemble of analyses conducted on ensemble of perturbed background and observations. The construction of our twin experiment appropriately relies on an ensemble of both perturbed background and observations. It consequently enables one to verify the first level of these diagnostics (Desroziers et al., 2009). It states that for weakly non-linear observation operators \mathbf{h} (see Eq. (5), Sect. 2.1), when both the \mathbf{B} and \mathbf{R} matrices are calibrated, averaging the values of the cost function at the optimum (when $\tilde{\mathbf{X}}^a$ optimum is reached) must be equal to the number of observations p :

$$\mathbf{E} \left[J \left(\tilde{\mathbf{X}}^a \right) \right] = p. \quad (12)$$

In our twin experiment, we apply 633 duration constraints. The average of the cost function at optimum $\tilde{\mathbf{X}}^a$ over our 51 simulations gives a value of 626 in accordance with Eq. (12). This is quite a fair result, and it validates our methodological development.

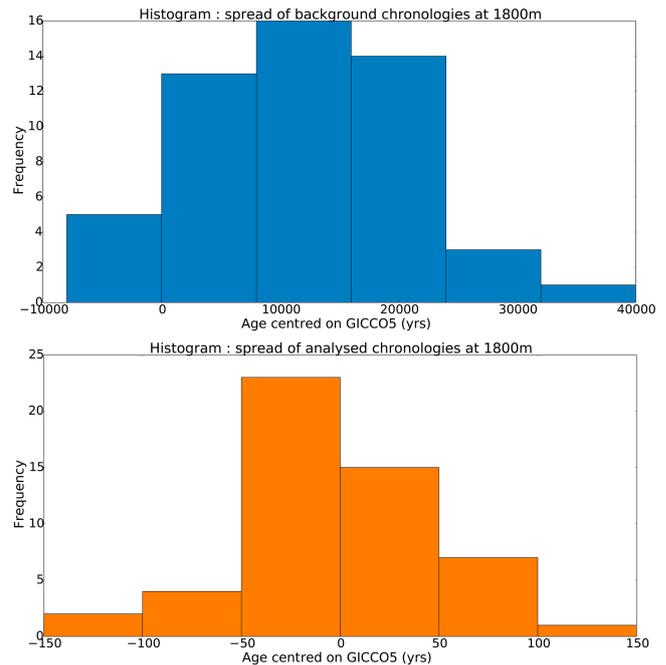


Figure 3. Twin experiments: (top) histograms of the 51 perturbed background (blue) and (bottom) the corresponding 51 analysed chronologies, i.e. output chronologies from Datice (red) at 1800 m depth for NGRIP ice core.

One should note that we have applied perfectly calibrated background and observation error covariance matrices. Indeed, the background and observation errors specified in the cost function are exactly the \mathbf{B} and \mathbf{R} matrices that have been used to produce the synthetic backgrounds and observations based on the true scenario. In a more complex experiment, the \mathbf{B} and \mathbf{R} matrices are usually misspecified because the background and observation errors, $\tilde{\epsilon}^b$ and ϵ^o , are usually poorly known since the truth itself, $\tilde{\mathbf{X}}^t$, is the unknown (see Appendix Sect. D1). In such cases, the a posteriori diagnostics are applied to calibrate the error covariance matrices. In future work we wish to conduct such calibration on Datice experiments involving several ice cores.

2.3 Implementing layer-counting error (MCE)

Layer counting consists in identifying annual cycles on the basis of annual layer proxies recorded along the core. The identification of annual cycles is subjected to errors. In order to deal with uncertain annual layers and to derive a counting error estimate, GICC05 adopted the following statistical approach. If the i^{th} cycle is identified as a certain annual cycle, the layer is counted as a full year with a zero error. Otherwise, for an uncertain i^{th} annual cycle, the layer counts as half a year plus or minus half a year. For each cycle numbered with index i , the two following variables n_i and σ_i are introduced in order to record the layer detection and associ-

ated error:

$$n_i \pm \sigma_i = 1 \pm 0 \text{ yr} \quad \text{for a certain layer,} \quad (13)$$

$$n_i \pm \sigma_i = 0.5 \pm 0.5 \text{ yr} \quad \text{for an uncertain layer.} \quad (14)$$

Ages along the ice core can thus be inferred by summing up the n_i cycles. For instance between depths z_q and z_p , delimiting the start and end depths of the q^{th} and p^{th} individual cycles, respectively, the duration Y_{z_q, z_p} (in years) is written as

$$Y_{z_q, z_p} = \sum_{i=q}^p n_i. \quad (15)$$

The official GICC05 age scale provides depth levels and cumulative counting error corresponding to time windows of 20 years. The GICC05 error estimate is called the maximum counting error (MCE). The MCE sums up the error of the individual cycles (i.e. σ_i) over the corresponding time window:

$$Y_{z_q, z_p}^{20 \text{ yr}} = \sum_{i=q}^{q+19} n_i = 20 \text{ yr}, \quad (16)$$

$$\text{MCE}_{z_q, z_p}^{20 \text{ yr}} = \sum_{i=q}^{q+19} \sigma_i. \quad (17)$$

For our experiments, the objective is to apply the GICC05 measure of duration $Y_{z_q, z_p}^{20 \text{ yr}}$ as duration constraints in Datice simulations. Two questions arise at this stage:

- Over which time window should we define our GICC05 markers of duration? Shall we apply markers of duration on 20 yr time window or choose another sampling rate (i.e. 20-, 40-, 60-year time window)?
- How should we infer the associated error when applying different time windows?

Neither of these questions are trivial. They are closely interlinked through the existence of error correlation between annual layers and the assumptions inherent to the MCE construction.

The MCE can be expressed through formulation of the GICC05 counting process with two normal probability density functions (pdf's): (i) the pdf of annual cycles identified as certain with a 1-year mean and a variance that tends to zero and (ii) the pdf of annual cycles identified as uncertain with a mean and standard deviation both set to half a year. Under this formalism (Appendix Sect. C1), the calculation of the error Σ_{z_q, z_p} on any counting measure Y_{z_q, z_p} is well documented, and the role played by the error correlation between annual cycles n_i and n_j becomes quite clear. If ρ_{ij} records such correlation, the Σ_{z_q, z_p} error is written as

$$\Sigma_{z_q, z_p}^2 = \sum_{i=q}^p \sigma_i^2 + 2 \sum_{i=q}^p \sum_{j=q, j>i}^p \rho_{ij} \sigma_i \sigma_j. \quad (18)$$

The Σ_{z_q, z_p} error reaches a minimum value in the case of a null error correlation between any pair of cycles (i.e. $\rho_{ij} = 0$):

$$\text{Min} \left[(\Sigma_{z_q, z_p})^2 \right] = \sum_{i=q}^p \sigma_i^2. \quad (19)$$

Conversely, the error reaches a maximum value when the error correlation between annual cycles is maximum (i.e. $\rho_{ij} = 1$):

$$\text{Max} \left[(\Sigma_{z_q, z_p})^2 \right] = \sum_{i=q}^p \sigma_i^2 + 2 \sum_{i=q}^p \sum_{j>1, j=q}^p \sigma_i \sigma_j = \left(\sum_{i=q}^p \sigma_i \right)^2. \quad (20)$$

The MCE calculation is based upon Eq. (1) and is therefore an upper estimate of the error regarding the value of the correlation coefficient (but not regarding the assumptions on the error σ_i). In particular, the error correlations have an “infinite range” along the core (ρ_{ij} does not decrease with the distance between the measured cycles) and pairs of annual cycles are fully correlated regardless of their respective position. Such description is not entirely realistic. Still, Rasmussen et al. (2006) have acknowledged that the assumption of full correlation of counting errors is not correct and stated that “recognizing that the counting errors in reality are neither uncorrelated nor fully correlated, we adopt the simple and conservative approach, summing up the uncertainties as if they were correlated”. In this study, the 1σ uncertainty of the GICC05 ice core is considered as half the MCE.

Following this approach means that errors for duration constraints at 40, 60 or 80 years will be derived by summing up the GICC05 20-year-window MCE 2, 3 and 4 times, respectively, in the case of full correlation within the time windows associated with the chosen sampling rate (Appendix Sects. C3 and C2).

However, the final chronology error should not depend on the arbitrary choice of the sampling rate. The option has thus been included in the Datice approach to apply error correlation on a finite interval and avoid abrupt cut-off of error correlation between adjacent intervals. This development should permit sampling of the markers with a certain step and apply error correlations beyond this time interval. Indeed, in future chronologies constructions, the value of the error correlation may change along the core in relationship with changes of climatic periods.

For this formulation of error correlation on a finite range, the correlation coefficients ρ_{ij}^{ad} of the observation error covariance matrix \mathbf{R}^{ad} (Eq. 6) are set according to a correlation function f that smoothly decreases with the distance between two duration constraints Y_i^{ad} and Y_j^{ad} :

$$\rho_{ij}^{\text{ad}} = f \left(|z_i^{\text{ad}} - z_j^{\text{ad}}| \right). \quad (21)$$

The shape of the function f is chosen as the product of a Gaussian and a triangular function:

$$f(|z_i^{\text{ad}} - z_j^{\text{ad}}|) = \exp\left(-\frac{(z_i^{\text{ad}} - z_j^{\text{ad}})^2}{2L^{\text{ad}2}}\right) \left(1 - \frac{|z_i^{\text{ad}} - z_j^{\text{ad}}|}{2L^{\text{ad}}}\right), \quad (22)$$

where L^{ad} must be set in metres in order to adjust the width of the f function and therefore the scope of the error correlation: the larger L^{ad} is, the higher the correlation between markers of duration.

With this new formulation of the error correlation, we can explore how both sampling and error correlation independently affect the final chronology and provide some guidelines for future constructions of ice core chronologies.

2.4 Tests and optimization of the Datice system to apply the GICC05 duration constraints

In this section, we extract several sets of duration constraints from GICC05, with different sampling and/or different assumptions regarding their associated errors. These inputs are used to conduct multiple Datice experiments and thus to investigate the sensitivity of the solution to sampling and error correlation assumptions. In the two following sections, experiments are run on the NGRIP core alone with only duration constraints. Details on the background settings are provided in Table 4. The marker errors are derived under either (i) the full correlation assumption AddMCE or (ii) the assumption of non-correlation beyond the 20-year-window SqrAddMCE (see Sect. 2.3 and Appendix Sect. C3).

In these experiments, a classical 1 m depth grid resolution is imposed, as in AICC2012. On such a depth grid, the annual layer thickness drops below 0.05 m yr^{-1} at some depth level so that the number of years in a 1 m layer becomes larger than 20 years. Datice cannot handle markers of duration that are sampled below the depth grid resolution. This technical issue prevents us from applying the GICC05 20-year-window markers and MCEs directly (Eqs. 16 and 17). In order to test fine sampling of the duration markers whilst avoiding sampling resolution below the depth grid, we implemented an adaptive sampling ranging from 40 to 140 years back to 60 ka.

2.4.1 Sampling and error correlation influence

To study the influence of the sampling, we run three experiments with markers sampled at three uniform rates (100, 200 and 300 years) as well as one experiment with the adaptive sampling between 40 and 140 years.

In these four experiments, the associated errors are derived from the 20-year-window MCE data under the AddMCE assumption of full error correlation between annual cycles over the length of the sampling interval. As discussed in Sect. 2.3, error correlation and sampling are interlinked together. To investigate the error correlation influence, we run a second

Table 1. Summary of the simulation configurations for the experiments of Sect. 2.4.1. Sampling and error correlation influence.

Name	MCE assumption	Sampling	Correlation coefficient
300yrs_AddMCE	AddMCE	300 yr	None
200yrs_AddMCE	AddMCE	200 yr	None
100yrs_AddMCE	AddMCE	100 yr	None
40–140 yr_AddMCE	AddMCE	Adaptative	None
40–140 yr_SqrAddMCE	SqrAddMCE	Adaptative	None
CorrCoeff_40–140 yr_AddMCE	AddMCE	Adaptative	$L^{\text{ad}} = 200 \text{ yr}$

experiment based on the adaptive sampling between 40 and 140 years, but with errors derived under the SqrAddMCE assumption of non-correlation beyond the 20-year windows. This assumption corresponds to the addition of squared MCE over 20-year windows to obtain the squared error over the sampling interval (40 to 140 years) used as input for Datice. Table 1 summarizes the experiment configurations.

Figures 4 and 5 show the different NGRIP simulations. As expected and discussed in Sect. 2.3, the age solutions and their associated errors are sensitive to the sampling. For the four experiments run under the AddMCE assumption, we better reproduce the GICC05 details with finer sampling rates (Fig. 5). Still, finer sampling of duration constraints is not the main reason for the better agreement with GICC05. Indeed, as error correlations are cumulative under the AddMCE assumption, the observation error largely increases with the length of the marker sampling window. Consequently, the strength of the constraint decreases, which deteriorates the convergence toward GICC05. The impact of observation error is also illustrated by Fig. 4 for the case of comparing the two adaptive sampling simulations, i.e. 40–140 yr_AddMCE and 40–140 yr_SqrAddMCE. The simulation run under the assumption of non-correlation beyond 20 years (SqrAddMCE) better converges toward GICC05, with a smaller associated error. As expected, the SqrAddMCE assumption strongly reduces the observation error at any depth along the core with respect to the full correlation assumption AddMCE.

Option SqrAddMCE may therefore be a way to relax the dependence of the analysed error to the sampling. However, as mentioned above, the abrupt loss of correlation at the boundaries of sampling interval may be questioned. At the junction of two duration constraints, neighbouring annual cycles from either side do not share any error correlation, while each of them correlates with much distant layers (as long as these layers are included in the same sampling interval). We actually rather expect error correlations to smoothly decrease with the distance between annual cycles. To circumvent this problem, we have designed an experiment called CorrCoeff_40–140 yr_AddMCE (shown in Figs. 4 and 5), which implements a correlation coefficient smoothly decreasing with the distance between markers. This implementation is discussed in the next section.

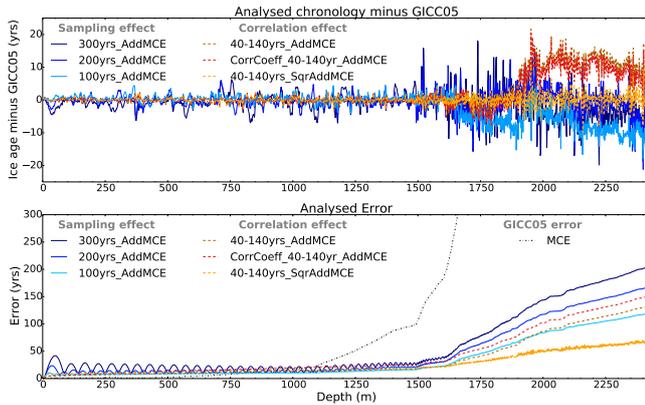


Figure 4. Sensitivity of the age and error solution to sampling of duration constraints and to the MCE assumptions. The difference between analysed chronologies and GICC05 age scale are shown in the top panel. Analysed errors and MCE are plotted in the bottom panel. The simulations settings are (i) three different uniform sampling rates (300, 200 and 100 years) and (ii) three adaptive samplings ranging from 40 to 140 years. The marker errors are derived under the AddMCE assumption (full correlation between annual cycles), except for (i) simulation 40–140 yr_SqrAddMCE, which is run under the SqrAddMCE assumption (correlation cut-off above 20 years), and (ii) simulation CorrCoeff_40–140 yr_SqrAddMCE, which is run with a finite depth range correlation coefficient. Table 1 summarizes experiment configurations.

We have demonstrated the sensitivity of the solution to the sampling and to the MCE assumptions applied to derive the observation error. However both issues are not fully decoupled in this first illustration. Hereafter, we investigate possible ways to study the error correlation independently of the sampling.

2.4.2 Finite range versus infinite range error correlation influence

In this section, we apply different correlation coefficients between duration constraints as implemented in Datic (Eqs. 6 and 21). In the following experiments, we investigate two correlation configurations: (i) correlation coefficients with infinite depth range along the core (hereafter InfiniteRangeCorr) and (ii) correlation coefficient smoothly decreasing with the distance between markers (hereafter FiniteRangeCorr) (Eq.).

In this set of experiments, due to large correlation coefficient values, the level of observation error is largely increased compared to the experiments of Sect. 2.4.1. To operate with configurations where the minimization and solution are still strongly driven by the constraint of the markers of duration, the background errors have been exaggerated (Table 4). With such a configuration, the analysed error should tend toward the observation error (Appendix Sect. E1):

$$\sigma_b \gg \sigma_o \implies \sigma_a \sim \sigma_o, \quad (23)$$

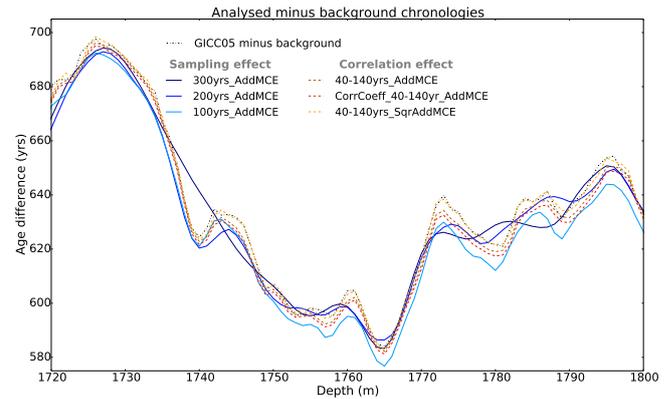


Figure 5. Sensitivity of the age solution to sampling of duration constraints. The simulations settings are as follows: (i) three different uniform sampling rates (dark to light-blue lines: 300, 200 and 100 years) and (ii) one adaptive rate ranging from 40 to 140 years (dashed coloured lines). The marker errors are derived under the AddMCE assumption (full correlation between annual cycles), except for (i) simulation 40–140 yr_SqrAddMCE, which is run under the SqrAddMCE assumption (correlation cut-off above 20 years), and (ii) simulation CorrCoeff_40–140 yr_SqrAddMCE, which is run with a finite depth range correlation coefficient. The curves represent the difference between the different analysed and background chronologies. The difference between GICC05 and background chronologies is displayed for comparison (dashed black line). Table 1 summarizes experiment configurations.

where σ_b , σ_o and σ_a are the background, observation and analysed errors, respectively.

In a first set of experiments, we investigate the InfiniteRangeCorr option. The correlation coefficient ρ_{ij}^{ad} (Eq. 21) is set to constant values ranging from 0.2 to 0.8. Such a configuration implies identical error correlations between markers separated by a large or a small distance, as the MCE formulation does for the GICC05 chronology. The MCE formulation implies a correlation coefficient of 1 all along the ice core. In the Datic approach, it is technically impossible to attribute a value of 1 to ρ_{ij}^{ad} due to the \mathbf{R}^{ad} matrix inversion in the cost function formulation (Eq. 5). As a consequence, the Datic experiment run with a correlation coefficient of 0.8 is the closest analogue to the MCE formulation, and we expect the analysed error to closely approach the MCE.

Figure 6 shows the InfiniteRangeCorr experiments with (i) a comparison of the background and analysed chronologies with the reference chronology GICC05 as well as (ii) a comparison of the Datic analysed errors and the MCE. As expected, the analysed errors tend toward the MCE for higher correlation coefficients. The full convergence to the MCE values is, however, hampered since more error correlation between markers progressively rules out the hypothesis of Eq. (23): when the observation error becomes too large, the analysed error is also driven by the background

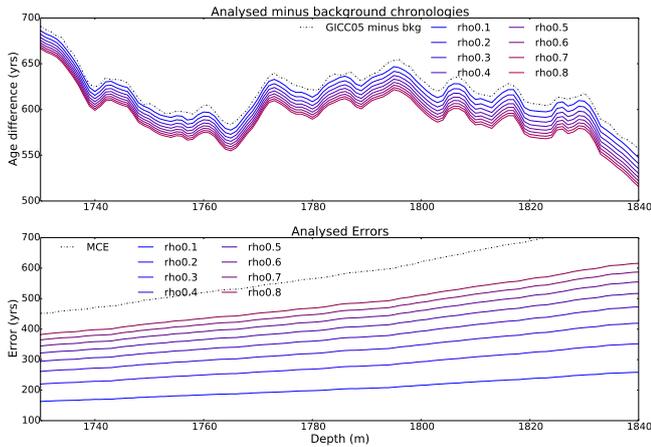


Figure 6. Sensitivity of the solution to correlation coefficient values applied between duration constraints (infinite depth range case). Top panel: GICC05 minus background chronology (black dashed line), Difference between analysed and background chronologies (blue to pink lines). Bottom panel: MCE (black dashed line) and analysed errors (blue to pink lines) The duration constraints are sampled every 100 years on GICC05, and correlation coefficients range from 0.8 to 0.2. The MCE assumption is AddMCE (full error correlation between cycles).

Table 2. Summary of the simulation configurations for the experiments of Sect. 2.4.2. Finite range versus infinite range error correlation influence.

Name	MCE assumption	Sampling coefficient	Correlation
CorrCoeff_300_yr_AddMCE	AddMCE	300 yr	$L^{\text{ad}} = 300$ yr
CorrCoeff_200_yr_AddMCE	AddMCE	200 yr	$L^{\text{ad}} = 300$ yr
CorrCoeff_100_yr_AddMCE	AddMCE	100 yr	$L^{\text{ad}} = 300$ yr
CorrCoeff_80_yr_AddMCE	AddMCE	100 yr	$L^{\text{ad}} = 300$ yr
CorrCoeff_40–140_yr_AddMCE	AddMCE	Adaptative	$L^{\text{ad}} = 300$ yr

error (Eq. E11). Analysed chronologies also show some predictable behaviour. When the correlation coefficient increases, the confidence in the duration constraints decreases and the analysed chronologies stay close to the background chronologies. Importantly, the reconstructed chronologies show an increasing bias relatively to GICC05 with increasing correlation coefficient. This problematic bias is closely related to the infinite depth range of the correlation coefficient.

We test hereafter the FiniteRangeCorr experiment with the finite depth range correlation coefficient. We ran simulations with five different types of sampling: (i) four uniform sampling rates (300, 200, 100 and 80 years) and (ii) the adaptive sampling between 40 and 140 years (CorrCoeff_40–140_yr_AddMCE experiment). An error correlation is applied between markers according to Eq. (21), and for all experiments we have set the correlation length L^{ad} to 300 years (Eq. 22). Table 2 summarizes the experiment configurations.

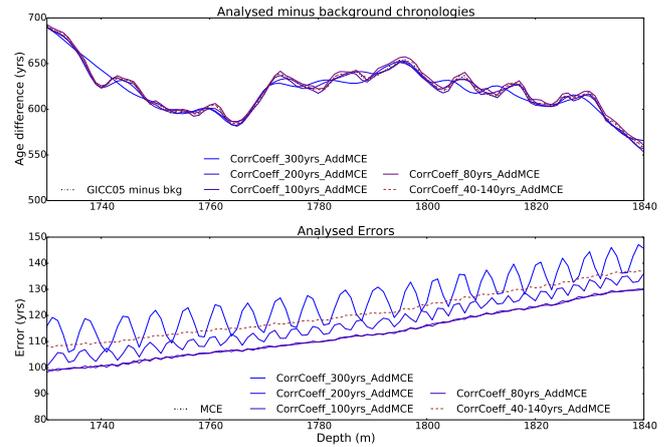


Figure 7. Sensitivity of the solution to correlation coefficient values applied between duration constraints (finite depth range case). Top panel: GICC05 minus background chronology (black dashed line) and difference between analysed and background chronologies. Bottom panel: MCE (black dashed line) and analysed errors (blue to pink lines). The duration constraints are correlated through a correlation function (Gaussian times triangle), the correlation length is 300 years. Uniform marker sampling at 80-, 100- and 200-year rates are shown with the blue to pink lines. The adaptive sampling between 40 and 140 years is shown in brown. The MCE assumption is AddMCE (full error correlation between cycles). Table 2 summarizes experiment configurations.

Figure 7 shows a comparison between background, analysed chronologies and GICC05 as well as analysed errors. As expected and already shown in previous sections, we clearly observe that there is a good fit to GICC05 with a better resemblance for the highest sampling rate. Importantly, in comparison to the InfiniteRangeCorr experiments, the analysed chronologies are not biased relative to GICC05. Moreover, despite the different sampling rates, the analysed errors show very similar values contrary to tests presented in the previous section. This is due to the fact that the analysed error is mainly influenced by the correlation coefficient on a finite length, which more efficiently intercorrelates markers sampled on short time windows.

In summary, the tests presented in the two previous sections suggest some guidelines for future constructions of chronology using the duration constraints. The central problem is the definition of the error associated with annual layer counting and how this error is correlated with other layers' error. We showed that making different assumptions on the error correlation leads to significant difference in the final chronology and associated error. For experiments with Datice applied to several ice cores including NGRIP, if the objective is to preserve the NGRIP age scale, our recommendations are (i) to sample the duration constraints over small time windows (e.g. 100 years or apply an adaptive sampling rate), (ii) to use a small uncertainty for the observations (this is directly linked with a large or short range of correlation be-

tween layer-counting errors), or (iii) to increase the NGRIP overall background error.

3 Application to five site experiments and comparison with AICC2012

After having validated the new developments for the implementation of duration constraints and possible error correlation, we show a first application of the new Daticce tool to a five-ice-core experiment (NGRIP, EDC, EDML, Vostok, TALDICE).

To use Daticce properly, the age constraints and the background scenarios need to be independent from each other. This was not the case when building AICC2012 for the NGRIP ice core. Here, the new development of Daticce allows one to use scenarios for background accumulation rate and thinning function independently from the age constraints deduced from GICC05 for NGRIP. In this application, the thinning function is the same as for AICC2012, obtained from the 1-D DJ glaciological model adapted to NGRIP (Andersen et al., 2006). However, we have largely increased its associated variance to make it comparable with variances associated with the background thinning function of the other cores implemented in Daticce. For the accumulation rate, we use the ss09sea accumulation rate based on the water isotopes record (Johnsen et al., 2001). The variance of NGRIP background accumulation rate is similar to the variances of background accumulation rates of the other ice cores in the building of AICC2012. The LIDIE background scenario in AICC2012 was built from a firnification model (Goujon et al., 2003) whose input parameters (temperature and accumulation rate) were roughly adjusted to be coherent with the mean $\delta^{15}\text{N}$ values measured over the NGRIP ice core. It is thus independent of GICC05 and has been kept unchanged for our study.

Concerning the age constraint, the absolute age markers deduced from GICC05 were replaced by the duration constraints. The markers of duration are obtained from the GICC05 chronology with adaptive lengths of intervals between 40 and 140 years under the AddMCE assumption (full correlation between annual cycles) and a correlation length of 300 years. In order to constrain the relative gas chronology vs. the ice chronology, we use information derived from $\delta^{15}\text{N}$ of air trapped in ice bubbles. New $\delta^{15}\text{N}$ data on the NGRIP ice core have been published since the AICC2012 chronology (Kindler et al., 2014). In particular, these data allow for identification of depths of rapid temperature increases associated with the beginning of Greenland Interstadial (GI) 1 to 7 in the gas phase. The depth differences between peaks of $\delta^{18}\text{O}_{\text{ice}}$ and $\delta^{15}\text{N}$ of a concomitant event recorded in the ice and the gas phases are thus used as delta-depth (Δdepth) constraints. With the new set of data from Kindler et al. (2014), we were thus able to deduce new Δdepth markers that were not available for the construction of AICC2012 (Table 3). Their uncertainties depend on the resolution of measure-

Table 3. New Δdepth markers of NGRIP deduced from the data of Kindler et al. (2014).

Depth (m)	Δdepth (m)	σ (m)	Event
1490.2	25.07	2.5	Holocene
1520.5	21.84	2.5	
1574.4	23.51	2.5	
1603.0	26.42	2.5	D-O 1
1792.7	25.07	2.5	D-O 2
1868.1	22.62	2.5	D-O 3
1888.4	21.87	2.5	D-O 4
1950.6	21.32	2	D-O 5
1972.6	20.42	2	D-O 6
2007.8	19.22	2	D-O 7
2099.9	17.77	2	D-O 8

ments and the difference of Δdepth estimates. Indeed, the Δdepth can be estimated from the difference between mid-slopes of $\delta^{18}\text{O}_{\text{ice}}$ and $\delta^{15}\text{N}$ increases or from the difference between the maxima of $\delta^{15}\text{N}$ and $\delta^{18}\text{O}_{\text{ice}}$.

Figure 8 compares the new Daticce chronology produced here (NGRIP-free) to AICC2012 for the five sites between 35 and 48 ka. We emphasize that the NGRIP-free chronology discussed here should not be taken as a new official chronology. It is only a test for our methodological development. Moreover, the AICC2012 chronology has the strong advantage of being in exact agreement with the GICC05 chronology and hence facilitating the multi-archive comparison, taking GICC05 as a reference, as has already been done in many studies (INTIMATE project: Blockley et al., 2012a). When looking at the NGRIP ice records, the final NGRIP-free chronology does not differ from the GICC05 or AICC2012 chronologies by more than 150 years over the last 60 kyr (Fig. 8).

The Antarctic chronologies are not much modified compared to the AICC2012 chronologies. They all differ by less than 410 years from AICC2012 (Fig. 8), which is well within the uncertainties of these chronologies (400–1000 years over this period). The small differences between the NGRIP-free and AICC2012 chronologies mean that the relationship between Greenland and Antarctic climate discussed with AICC2012 for the millennial-scale variability of the last glacial period stays valid on NGRIP-free (Veres et al., 2013). We observe a classical see-saw pattern with Antarctic temperature increasing during the Greenland stadials, with a faster and shorter increase at EDML than at EDC (Fig. 8).

4 Conclusions

The Bayesian tool Daticce used for the construction of coherent ice core chronology has been improved and now enables one to consider the duration of events as dating constraints. We validated this new methodological implementa-

Table 4. Summary of the simulation configurations.

Experiment	Variance profile	A^b	T^b	C^b	Objective
Twin experiments (Sect. 2.2)	Changing with depth Bazin et al. (2013)	–	σ_b of thinning divided by 3	–	Avoid correction on the thinning in experiment with ice age only
Sensitivity to sampling and MCE (Sect. 2.4.1)	Constant with depth	$\sigma_b = 0.8$ triangular ρ_b function 2500 yr width	$\sigma_b = 0.5$ triangular ρ_b function 60 m width	–	Simplify the experiment
Correlation between markers Sect. (2.4.2)	Constant with depth	$\sigma_b = 3.2$ triangular ρ_b function 2500 yr width	$\sigma_b = 2$ triangular ρ_b function 60 m width	–	Reinforce the marker constraints: $\sigma_b \gg \sigma_o$

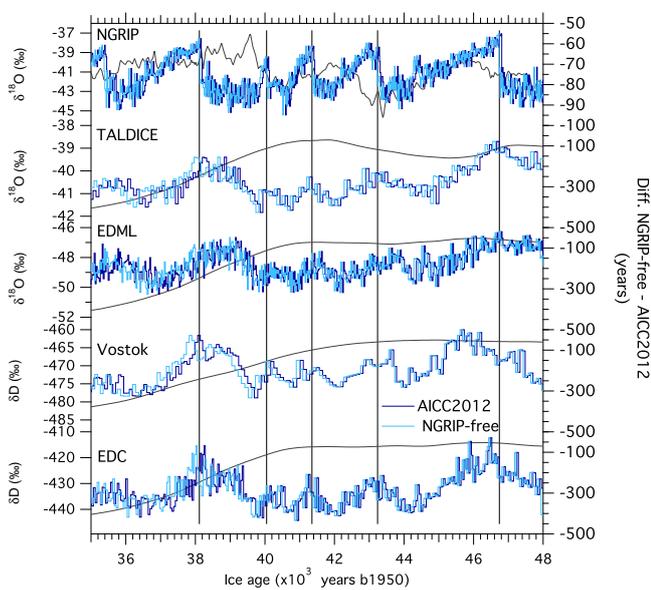


Figure 8. Comparison of NGRIP $\delta^{18}\text{O}$ (NorthGRIP Community Members, 2004), TALDICE $\delta^{18}\text{O}$ (Stenni et al., 2011), EDML $\delta^{18}\text{O}$ (EPICA Community Members, 2006, 2010), Vostok δD (Petit et al., 1999) and EDC δD (Jouzel et al., 2007) water isotopes on different coherent chronologies (AICC2012 in dark blue and NGRIP-free in light blue). The differences between the NGRIP-free and AICC2012 chronologies for each sites are represented by the black lines.

tion by conducting twin experiments and a posteriori diagnostics.

In comparison to age markers, duration constraints are more coherent with the building of chronologies based on layer counting where the absolute error, defined as the maximum counting error for GICC05, increases with depth due to cumulative effects. To account for the fact that the counting errors on duration constraints are neither fully correlated nor uncorrelated, we have also introduced the possibility to adjust correlation between duration errors with a correlation co-

efficient that smoothly decreases with the distance between markers.

There is no objective way to choose the best representation of the correlation, and future dating experiments may propose different correlation coefficients for layer counting performed at different periods (glacial vs. interglacial times). We have thus presented here some sensitivity tests for the sampling and correlation of errors associated with duration constraints. These tests lead to general guidelines for future dating experiments including layer counting as absolute age constraints. For example, to best respect an ice core chronology based on layer counting, we would favour a high-frequency sampling of duration constraints with a correlation on a finite depth range. Finally, the comparison of AICC2012 with the chronology obtained over five polar sites using the improved Datice tool incorporating duration constraints and associated correlation of errors shows differences of less than 410 years over the last 60 kyr, well within the uncertainties associated with the AICC2012 chronology. Huge efforts in annual layer counting were produced in the recent years for ice core chronologies, in particular for the Western Antarctic Ice Sheet (WAIS) ice core (WAIS Divide Project Members, 2013). Future dating experiments should thus benefit from the methodological development and validation of the Bayesian tool presented in this study.

Appendix A: Datice age models

The Datice age models are derived from three key ice core quantities: the total thinning function $T(z)$, the accumulation rate $A(z)$ and the LIDIE $C(z)$. They allow one to estimate the ice age chronology $\Psi(z)$ as follows:

$$\Psi(z) = \int_0^z \frac{D(z')}{T(z') \cdot A(z')} dz', \quad (\text{A1})$$

with $D(z)$ being the relative density of the snow/ice material.

The gas chronology $\chi(z)$ is defined using Δdepth data, which measures the in situ depth difference between ice and gas of the same age. Δdepth can be approximated as follows:

$$\Delta\text{depth}(z) = C(z) \cdot T(z). \quad (\text{A2})$$

The gas age is further calculated as the ice age of the layer situated at the depth $(z - \Delta\text{depth})$

$$\chi(z) = \Psi(z - \Delta\text{depth}(z)). \quad (\text{A3})$$

The background age scenarios $T^b(z)$, $A^b(z)$ and $C^b(z)$, as well as age constraints, are required to run Datice. To optimize the gas and ice age scales, the specifications of the background and age constraint uncertainties are further needed. Depending on the confidence assigned to the background and to the markers, Datice will modify, to some extent, the initial background scenario.

Appendix B: Error specification in the Datice experiments

B1 Background variances changing with depth

Here we reiterate the formulations used to define the thinning function and the LIDIE variances (Eqs. B1 and B4, respectively), since several coefficients were modified in this study.

The standard deviation of the thinning function is defined as

$$\sigma_T(z) = c_{T_1} + c_{T_2} \cdot \int_0^z \frac{D(z)}{T(z)} dz + c_{T_3} \cdot \frac{\sigma_{A,loc}}{\sigma_{A,loc}^{max}}, \quad (B1)$$

where c_{T_1} , c_{T_2} and c_{T_3} are user-defined constant parameters (c_{T_2} equals $c \cdot 0.1/H$, where H is the maximum depth of the input and c a user-defined constant), $T(z)$ is the thinning function, $D(z)$ the relative density, $\sigma_{A,loc}$ the local standard deviation of accumulation and $\sigma_{A,loc}^{max}$ the maximum standard deviation of accumulation. The last term was implemented in order to increase the thinning variance during large climatic transitions since it has been suggested that the mechanical properties of ice can be modified in these periods. For the purpose of the tests performed in this study, we have corrected the c_{T_2} value (from 0.000016 to 0.000064) that was used for NGRIP when building AICC2012. This correction allows for having a coherent parameterization of the thinning variance for the five ice cores. Moreover, we have reduced the c_{T_1} values from 0.01 to 0.00001 in order to be closer to the zero-variance hypothesis at the surface for all sites. We have also divided the c_{T_3} values by 2 for all five sites. The other coefficients have the same values as used to build AICC2012 (Supplement to Bazin et al., 2013).

The standard deviation for the accumulation rate is

$$\sigma_A(z) = \sigma_{b,A} \cdot \frac{|A_0 - A|}{|A_0 - A|_{max}} \cdot \left(1 + c_{A_1} \frac{z}{z_{max}}\right), \quad (B2)$$

where $\sigma_{b,A}$ is a reference standard deviation, A_0 is the mean Holocene accumulation rate and c_{A_1} is a constant parameter. The variance associated with the accumulation rate scenario thus increases when the background accumulation rate strongly deviates from the Holocene value. The reason for such a parameterization is that the reconstruction of accumulation rate from water isotopes through the exponential law is semi-empirical and its extrapolation far from the present-day conditions may be problematic.

In order to avoid too small variances, a threshold value, σ_m , is implemented for each ice core. If σ_A is smaller than σ_m , then σ_A is recalculated as

$$\sigma_A = \sigma_m \cdot \left(1 + c_{A_1} \frac{z}{z_{max}}\right), \quad (B3)$$

where σ_m represents the minimum values, defined by the user.

We have kept the same values for all Antarctic sites for $\sigma_{b,A}$. For NGRIP, we have increased its value from 0.8 to 0.9, and increased the minimum value from 0.15 to 0.2.

The formulation for the LIDIE standard deviation is

$$\sigma_L(z) = \frac{\sigma_{b,L}}{\sigma_{b,A}} \cdot \frac{\sigma_A(z)}{1 + \frac{m_{A,loc}}{m_{A,loc}^{max}}}, \quad (B4)$$

where $m_{A,loc}$ is the local mean accumulation rate and $m_{A,loc}^{max}$ its maximum value over the length of the core, and $\sigma_{b,L}$ is a reference standard deviation. In this case, the variance on the LIDIE increases with the variance on the accumulation rate, i.e. with the deviation from present-day conditions. This is justified by the fact that we do not have a standardized way to link LIDIE to accumulation rate and/or temperature (firnification model or $\delta^{15}N$ -based estimate). In Sect. 3 of the main text we reduced the value of the $\sigma_{b,L}$ coefficient from 0.6 to 0.3 as well as the minimum value possible (from 0.1 to 0.05) for NGRIP. This means that we have more confidence in our background LIDIE scenario than when building the AICC2012 chronology. The other coefficients have the same values as used to build AICC2012 (Supplement to Bazin et al., 2013).

Appendix C: GICC05 and MCE statistical assumptions

C1 Statistical assumptions to handle the annual layer-counting variables

With the objective of better handling the MCE data, we make Gaussian assumptions and reformulate the GICC05 layer counting with two probability density functions (pdf's):

- The duration of an annual cycle identified as certain is normally distributed with a 1-year average and a zero standard deviation.
- The duration of an annual cycle identified as uncertain is normally distributed with a mean and a standard deviation both set to half a year.

The counting variables n_i and σ_i are statistical parameters of the Gaussian distribution, i.e. the mean and standard deviation.

It should be noted that such a formulation may be questioned: (i) the annual layer counting has a discrete underlying nature, and one might rather prefer to introduce discrete random variables to handle it; (ii) the Gaussian pdf applies to continuous random variables ranging from $-\infty$ to $+\infty$, which is far from being the case here; and (iii) Gaussian-assumption-based theorems are tricky to apply in the zero-variance limit assessed for annual layer identified as certain.

C2 Sampling markers of duration and amount of error correlation accounted for: general case

Sampling markers of duration from the GICC05 layer-counted chronology may lead to a different amount of error correlation between individual measures of annual cycles. Let us first sample the markers on a T -time window and get the two constraints, Y_{z_q, z_p}^T and Y_{z_p, z_m}^T , which measure the annual cycles in years in the two neighbouring depth intervals $[z_q, z_p]$ and $[z_p, z_m]$ along the core. The errors Σ_{z_q, z_p}^T and Σ_{z_p, z_m}^T associated with each marker are written as

$$\left(\Sigma_{z_q, z_p}^T\right)^2 = \sum_{i=q}^p \sigma_i^2 + 2 \sum_{i=q}^p \sum_{j=q, j>i}^p \rho_{ij} \sigma_i \sigma_j, \quad (C1)$$

$$\left(\Sigma_{z_p, z_m}^T\right)^2 = \sum_{i=p+1}^m \sigma_i^2 + 2 \sum_{i=p+1}^m \sum_{j=p+1, j>i}^m \rho_{ij} \sigma_i \sigma_j. \quad (C2)$$

If we double the sampling rate ($2T$ -time window markers), we get a single marker Y_{z_q, z_m}^{2T} (instead of the two constraints Y_{z_q, z_p}^T and Y_{z_p, z_m}^T), which measures the annual cycles in years over the depth interval $[z_q, z_m]$.

$$Y_{z_q, z_m}^{2T} = Y_{z_q, z_p}^T + Y_{z_p, z_m}^T \quad (C3)$$

The error Σ_{z_q, z_m}^{2T} associated with $2T$ -time window marker Y_{z_q, z_m}^{2T} is now written as

$$\left(\Sigma_{z_q, z_m}^{2T}\right)^2 = \sum_{i=q}^m \sigma_i^2 + 2 \sum_{i=q}^m \sum_{j=q, j>i}^m \rho_{ij} \sigma_i \sigma_j. \quad (C4)$$

Rearranging Eq. (C4) in terms of the errors Σ_{z_q, z_p}^T and Σ_{z_p, z_m}^T gives

$$\begin{aligned} \left(\Sigma_{z_q, z_m}^{2T}\right)^2 &= \sum_{i=q}^p \sigma_i^2 + 2 \sum_{i=q}^p \sum_{j=q, j>i}^p \rho_{ij} \sigma_i \sigma_j \\ &+ \sum_{i=p+1}^m \sigma_i^2 + 2 \sum_{i=p+1}^m \sum_{j=p+1, j>i}^m \rho_{ij} \sigma_i \sigma_j \\ &+ 2 \sum_{i=q}^p \sum_{j=p+1}^m \rho_{ij} \sigma_i \sigma_j \\ &= \left(\Sigma_{z_q, z_p}^T\right)^2 + \left(\Sigma_{z_p, z_m}^T\right)^2 + 2 \sum_{i=q}^p \sum_{j=p+1}^m \rho_{ij} \sigma_i \sigma_j. \end{aligned} \quad (C5)$$

In Eq. (C5), the last term corresponds to a part of the error accounted for in the $2T$ -window marker Y_{z_q, z_m}^{2T} that will never be accounted for in the case of the T -window markers Y_{z_q, z_p}^T and Y_{z_p, z_m}^T . It corresponds to error correlations between annual layers i and j that are separated by the longest distance as they are located in the $[z_q, z_p]$ depth interval for the first layer, and in the next interval $[z_p, z_m]$ for the second. The longer range correlation can only be accounted for with the larger sampling rate. This point is illustrated with Fig. C1.

It is worth noting that Eq. (C5) further simplifies with respect to the ρ_{ij} correlation coefficients of the last term:

- When the correlation coefficients are identically null, we get the sum of the squared errors:

$$\left(\Sigma_{z_q, z_m}^{2T}\right)^2 = \left(\Sigma_{z_q, z_p}^T\right)^2 + \left(\Sigma_{z_p, z_m}^T\right)^2. \quad (C6)$$

- When the correlation coefficients are set to 1, we get the squared sum of the errors:

$$\left(\Sigma_{z_q, z_m}^{2T}\right)^2 = \left(\Sigma_{z_q, z_p}^T + \Sigma_{z_p, z_m}^T\right)^2. \quad (C7)$$

C3 Sampling markers of duration and amount of error correlation accounted for: MCE case

Below we briefly discuss the possible implications for choosing a sampling rate of 20 or 40 years. While for the 20-year sampling, we may straightforwardly implement the 20-year-window markers ($Y_{z_q, z_p}^{20\text{yrs}}$) and errors (MCE $_{z_q, z_p}^{20\text{yr}}$) from GICC05, different extreme views can be proposed for a 40-year sampling:

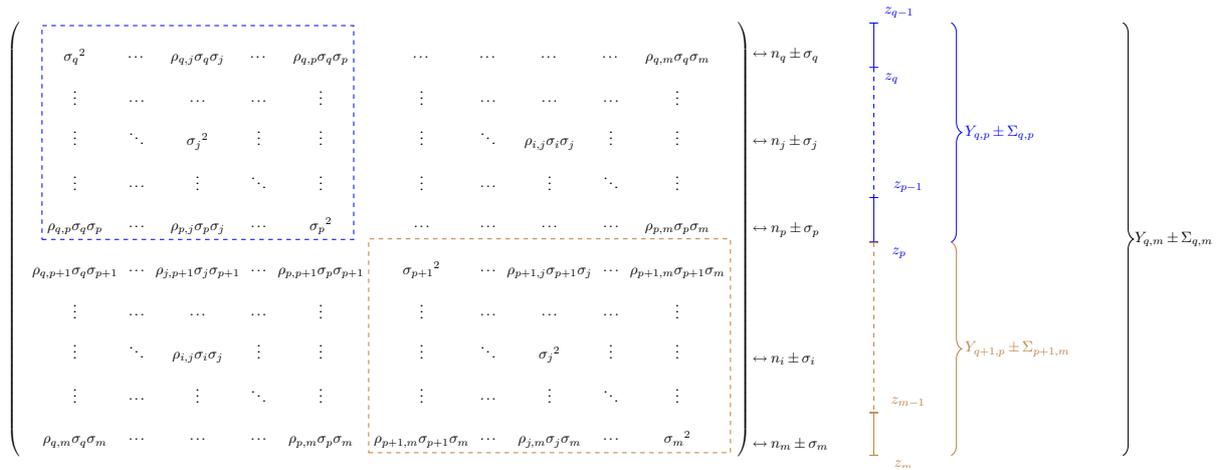


Figure C1. Error covariance matrix \mathbf{R} associated with a duration constraint Y_{z_q, z_m}^{2T} sampled at the $2T$ years rate on a layer-counted chronology, e.g. GICC05. The matrix stores error information related to the measures of annual cycles on the depth interval $[z_q, z_m]$. The diagonal elements record the error variances σ_i^2 associated with each identified annual cycle, while the non-diagonal elements store the error covariances, with especially the error correlation coefficient ρ_{ij} between pairs of annual layers i and j . The error Σ_{z_q, z_m}^{2T} associated with marker Y_{z_q, z_m}^{2T} takes into account the whole error correlations stored in the \mathbf{R} matrix. If the measures of duration are instead sampled at the T sampling rate (i.e. half the previous rate), the marker of duration Y_{z_q, z_m}^{2T} splits into two markers: (i) Y_{z_q, z_p}^T (in blue) and (ii) Y_{z_p, z_m}^T (in brown). The error Σ_{z_q, z_p}^T associated with Y_{z_q, z_p}^T will only account for the correlation of the upper diagonal block of \mathbf{R} (dashed blue line around block). Symmetrically, the error Σ_{z_p, z_m}^T associated with Y_{z_p, z_m}^T will only account for the correlation of the lower diagonal blocks of \mathbf{R} (dashed brown line around block). Correlations of the non-diagonal blocks of \mathbf{R} , which correlate annual layers $i \in [z_q, z_p]$ and $j \in [z_p, z_m]$, are only accounted for in the total error when applying the $2T$ sampling rate.

- Option one: we believe that the full error correlation assessed over the 20-year time window between annual layers cuts-off. Then, no correlation exists between the annual cycles included in the two separated but adjacent depth intervals $[z_q, z_p]$ and $[z_p, z_m]$. Under this assumption, the theory shows that we must sum up the squared 20-year MCEs:

$$\text{MCE}_{z_p, z_m}^{40 \text{ yr}} = \sqrt{\left(\text{MCE}_{z_q, z_p}^{20 \text{ yr}}\right)^2 + \left(\text{MCE}_{z_p, z_m}^{20 \text{ yr}}\right)^2}. \quad (\text{C8})$$

- Option two: we believe that the full error correlation assessed over the 20-year time window between annual layers extends over the 40-year time window (which means over the depth interval $[z_q, z_m] = [z_q, z_p] \cup [z_p, z_m]$). In that case the theory shows that we must sum up the 20-year MCEs:

$$\text{MCE}_{z_p, z_m}^{40 \text{ yr}} = \text{MCE}_{z_q, z_p}^{20 \text{ yr}} + \text{MCE}_{z_p, z_m}^{20 \text{ yr}}. \quad (\text{C9})$$

From this simple illustration, it follows that markers of duration and errors sampled on GICC05 at different rates (i.e. 40–60–80–100 years), derived by summing up the GICC05 20-year-window MCE, must be understood as very different inputs and different simulation outputs must be expected.

In Sect. 2.3 of the main text, we refer to the AddMCE assumption (Eq. C9) when MCEs are added, while at the same time we refer to the AddSqrMCE assumption (Eq. C8) when the squared MCEs are added.

Appendix D: The Datice data assimilation system

D1 Background and observation error covariance matrices

The background and observation errors $\tilde{\epsilon}^b$ and ϵ^o are measures of the background and observation distance to \tilde{X}^t , which records the true but unknown model. In the Datice system, \tilde{X}^t is the set of true correction functions to apply to accumulation, thinning and LIDIE (after exponential transformation). By definition, errors $\tilde{\epsilon}^b$ and ϵ^o are written as

$$\tilde{\epsilon}^b = \tilde{X}^b - \tilde{X}^t, \quad (\text{D1})$$

$$\epsilon^o = Y^o - \mathbf{h}(\tilde{X}^t), \quad (\text{D2})$$

where vectors \tilde{X}^b and Y^o store the background and observation data and \mathbf{h} is the observation operator that maps the model space to the observation space. The background and observation error covariance matrices \mathbf{B} and \mathbf{R} are defined as follows:

$$\mathbf{B} = \mathbf{E} \left[\tilde{\epsilon}^b \tilde{\epsilon}^{bT} \right], \quad (\text{D3})$$

$$\mathbf{R} = \mathbf{E} \left[\epsilon^o \epsilon^{oT} \right], \quad (\text{D4})$$

where $\mathbf{E}[\bullet]$ is the expected value operator and \mathbf{E}^T is the transpose operator.

D2 Analysed error covariance matrix

The analysed error $\tilde{\epsilon}^a$ (random variable) is defined as follows:

$$\tilde{\epsilon}^a = \tilde{X}^a - \tilde{X}^t, \quad (\text{D5})$$

where \tilde{X}^t records the true (but unknown) correction functions (i.e. the correction that would provide the exact true scenario of thinning, accumulation and LIDIE). The analysed error covariance matrix $\tilde{\mathbf{P}}^a$ is given by

$$\tilde{\mathbf{P}}^a = \mathbf{E} \left[\tilde{\epsilon}^a \tilde{\epsilon}^{aT} \right] \quad (\text{D6})$$

Appendix E: Analysed chronology and analysed errors

The ice age scale changes according to the correction function values $\tilde{\mathbf{X}} = (\tilde{\alpha}(z), \tilde{\tau}(z))^T$ as follows:

$$\Psi(\tilde{\mathbf{X}}) = \int_{z=0}^z \frac{\exp(-\tau(z')) \exp(-\alpha(z'))}{T^b(z') A^b(z')} D(z') dz'. \quad (E1)$$

The optimized ice age is calculated by applying in Eq. (A1) the optimized correction functions obtained after minimization of the cost function (Eq. 5):

$$\tilde{\mathbf{X}}^a = (\tilde{\alpha}^a(z), \tilde{\tau}^a(z), \tilde{\gamma}^a(z))^T. \quad (E2)$$

This gives the analysed chronology:

$$\psi^a(z) = \Psi(\tilde{\mathbf{X}}^a) = \int_{z=0}^z \frac{\exp(-\tilde{\tau}^a(z')) \exp(-\tilde{\alpha}^a(z'))}{T^b(z') A^b(z')} D(z') dz'. \quad (E3)$$

To approximate the a posteriori error of the analysed chronology, the covariances of errors of $\tilde{\mathbf{X}}^a$ are required. These covariances of errors are recorded in \mathbf{P}^a , the analysed error covariance matrix, which can be approximated:

$$\frac{1}{\mathbf{P}^a} \sim \frac{1}{\mathbf{B}} + \frac{1}{\mathbf{H}^T \mathbf{R} \mathbf{H}}, \quad (E4)$$

where \mathbf{B} and \mathbf{R} are the background and observation error covariance matrices, respectively Eq. (D1), and where \mathbf{H} is the tangent linear observation operator (linearization of \mathbf{h} at $\tilde{\mathbf{X}}^a$).

Datice calculates the components of \mathbf{P}^a at each depth level on the basis of Eq. (E4). Importantly, \mathbf{P}^a operates a balance between the background and observation errors. The \mathbf{P}^e error covariance propagates to the analysed chronology $\Psi^a(\tilde{\mathbf{X}}^a)$. If we define E^a as the a posteriori error of the analysed chronology, the corresponding analysed error covariance matrix Λ^a is by definition

$$E^a = \Psi(\tilde{\mathbf{X}}^a) - \Psi(\tilde{\mathbf{X}}^t), \quad (E5)$$

$$\Lambda^a = \mathbf{E} [E^a E^{aT}]. \quad (E6)$$

We intend to show how matrix Λ^a depends on matrix \mathbf{P}^a , and then on the error matrices \mathbf{B} and \mathbf{R} . We reiterate the steps to show this link, as described in Lemieux-Dudon et al. (2009). One can first linearize the age scale of Eq. (A1) around $\tilde{\mathbf{X}}^a$ Eq. D5):

$$\Psi(\tilde{\mathbf{X}}^t) = \Psi(\tilde{\mathbf{X}}^a) - \tilde{\epsilon}^{aT} \cdot [\Psi \Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}] + \cdot (\|\tilde{\epsilon}^a\|). \quad (E7)$$

Inserting Eq. (E7) in Eq. (E5) enables one to approximate the a posteriori error E^a :

$$E^a \sim \tilde{\epsilon}^{aT} \cdot [\Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}]. \quad (E8)$$

Importantly, the later approximation is valid if $\tilde{\epsilon}^a$ represents sufficiently small perturbations, i.e. the correction functions $\tilde{\mathbf{X}}^a$ must be close to the true scenario $\tilde{\mathbf{X}}^t$. Under this strong assumption, Eq. (E8) leads to

$$E^a E^{aT} \sim [\Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}]^T \tilde{\epsilon}^a \tilde{\epsilon}^{aT} [\Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}]. \quad (E9)$$

Finally, from Eq. (E9), one can approximate the error matrix of the ice age Λ^a by applying the expected value operator to Eq. (E9) and by using Eq. (D6):

$$\Lambda^a \sim [\Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}]^T \mathbf{P}^a [\Psi \tilde{\mathbf{X}} |_{\tilde{\mathbf{X}}^a}]. \quad (E10)$$

Datice applies Eq. (E10) to approximate the covariances of errors of the analysed chronology. This approximation especially requires that the optimum correction functions $\tilde{\mathbf{X}}^a$ obtained after the minimization of the cost function remains sufficiently close to the true scenario $\tilde{\mathbf{X}}^t$. On the assumption of normally distributed errors, matrix Λ^a provides the standard deviation of the analysed age scale. The process to calculate the analysed error of the gas age scale is similar but relies on Eq. (A3).

E1 Balance between background and observation error and impact on the analysis

The variances of errors of the analysed chronology cumulate the error covariances recorded in matrix \mathbf{P}^a (Eq. E10).

The age solution and its error are therefore largely determined by the balance between observation and background errors (Eq. E4). To fix ideas, instead of matrices \mathbf{P}^a , \mathbf{R} and \mathbf{B} , let us suppose that we deal with the scalars σ^a , σ^o and σ^b . With such a simplification, Eq. (E4) is written as

$$\frac{1}{\sigma_a^2} = \frac{1}{\sigma_b^2} + \frac{1}{\sigma_o^2}. \quad (E11)$$

According to the ratio between observation and background errors, there are two extreme configurations:

- If $\sigma_o \ll \sigma_b$, the minimization and the solution are strongly constrained by the observation, and the analysed error tends to be the observation error:

$$\sigma_a \sim \sigma_o. \quad (E12)$$

- Conversely, if $\sigma_b \ll \sigma_o$, the background scenario dominates and the solution is close to the background. The analysed error tends to the background error:

$$\sigma_a \sim \sigma_b. \quad (E13)$$

An intermediate ratio of background to observation error leads to an intermediate analysed solution and error. In the special case of an equal number of errors in the observation and background, i.e. $\sigma = \sigma_o \sim \sigma_b$, the analysed error is written as

$$\sigma_a \sim \frac{\sigma}{\sqrt{2}}. \quad (\text{E14})$$

Acknowledgements. We thank Eric Wolff for his comments on a preliminary version of this article. We thank Paul Blackwell and the anonymous reviewers for their fruitful comments. This project was funded by the Fondation de France Ars Cuttoli. This work was supported by Labex L-IPSL, which is funded by the ANR (grant no. ANR-10-LABX-0018). This is LSCE contribution no. 5502.

Edited by: N. Abram

References

- Andersen, K. K., Svensson, A., Johnsen, S. J., Rasmussen, S. O., Bigler, M., Röthlisberger, R., Ruth, U., Siggaard-Andersen, M.-L., Peder Steffensen, J., Dahl-Jensen, D., Vinther, B. M., and Clausen, H. B.: The Greenland Ice Core Chronology 2005, 15 42 ka., Part 1: constructing the time scale, *Quaternary Sci. Rev.*, 25, 3246–3257, doi:10.1016/j.quascirev.2006.08.002, 2006.
- Austin, W., Hibbert, F., Rasmussen, S., Peters, C., Abbott, P., and Bryant, C.: The synchronization of palaeoclimatic events in the North Atlantic region during Greenland Stadial 3 (ca 27.5 to 23.3 kyr b2k), *Quaternary Sci. Rev.*, 36, 154–163, doi:10.1016/j.quascirev.2010.12.014, 2012.
- Austin, W. E. and Hibbert, F. D.: Tracing time in the ocean: a brief review of chronological constraints (60–8 kyr) on North Atlantic marine event-based stratigraphies, *Quaternary Sci. Rev.*, 36, 28–37, doi:10.1016/j.quascirev.2012.01.015, 2012.
- Bazin, L., Landais, A., Lemieux-Dudon, B., Toyé Mahamadou Kele, H., Veres, D., Parrenin, F., Martinerie, P., Ritz, C., Capron, E., Lipenkov, V., Loutre, M.-F., Raynaud, D., Vinther, B., Svensson, A., Rasmussen, S. O., Severi, M., Blunier, T., Leuenberger, M., Fischer, H., Masson-Delmotte, V., Chappellaz, J., and Wolff, E.: An optimized multi-proxy, multi-site Antarctic ice and gas orbital chronology (AICC2012): 120–800 ka, *Clim. Past*, 9, 1715–1731, doi:10.5194/cp-9-1715-2013, 2013.
- Blockley, S., Lane, C., Turney, C., and Bronk Ramsey, C.: The INTEgration of Ice core, MARine and TERrestrial records of the last termination (INTIMATE)60,000 to 8000 BP, *Quaternary Sci. Rev.*, 36, p. 1, doi:10.1016/j.quascirev.2011.10.001, 2012a.
- Blockley, S. P., Lane, C. S., Hardiman, M., Rasmussen, S. O., Seierstad, I. K., Steffensen, J. P., Svensson, A., Lotter, A. F., Turney, C. S., and Bronk Ramsey, C.: Synchronisation of palaeoenvironmental records over the last 60 000 years, and an extended INTIMATE event stratigraphy to 48 000 b2k, *Quaternary Sci. Rev.*, 36, 2–10, doi:10.1016/j.quascirev.2011.09.017, 2012b.
- Buiron, D., Chappellaz, J., Stenni, B., Frezzotti, M., Baumgartner, M., Capron, E., Landais, A., Lemieux-Dudon, B., Masson-Delmotte, V., Montagnat, M., Parrenin, F., and Schilt, A.: TALDICE-1 age scale of the Talos Dome deep ice core, East Antarctica, *Clim. Past*, 7, 1–16, doi:10.5194/cp-7-1-2011, 2011.
- Cutler, N. N., Raymond, C. F., Waddington, E. D., Meese, D. A., and Alley, R. B.: The effect of ice-sheet thickness change on the accumulation history inferred from GISP2 layer thicknesses, *Ann. Glaciol.*, 21, 26–32, 1995.
- Dansgaard, W. and Johnsen, S. J.: A flow model and a time scale for the ice core from Camp Century, Greenland, *J. Glaciol.*, 8, 215–223, 1969.
- Davies, S. M., Abbott, P. M., Pearce, N. J., Wastegard, S., and Blockley, S. P.: Integrating the INTIMATE records using tephrochronology: rising to the challenge, *Quaternary Sci. Rev.*, 36, 11–27, doi:10.1016/j.quascirev.2011.04.005, 2012.
- Desroziers, G., Berre, L., Chabot, V., and Chapnik, B.: A posteriori diagnostics in an ensemble of perturbed analyses, *Month. Weather Rev.*, 137, 3420–3436, 2009.
- EPICA Community Members: One-to-one coupling of glacial climate variability in Greenland and Antarctica, *Nature*, 444, 195–198, doi:10.1038/nature05301, 2006.
- EPICA Community Members: Stable oxygen isotopes of ice core EDML, PANGAEA, doi:10.1594/PANGAEA.754444, 2010.
- Goujon, C., Barnola, J.-M., and Ritz, C.: Modeling the densification of polar firn including heat diffusion: Application to close-off characteristics and gas isotopic fractionation for Antarctica and Greenland sites, *J. Geophys. Res.-Atmos.*, 108, 4792, doi:10.1029/2002JD003319, 2003.
- Guillevic, M., Bazin, L., Landais, A., Kindler, P., Orsi, A., Masson-Delmotte, V., Blunier, T., Buchardt, S. L., Capron, E., Leuenberger, M., Martinerie, P., Prié, F., and Vinther, B. M.: Spatial gradients of temperature, accumulation and $\delta^{18}O$ -ice in Greenland over a series of Dansgaard-Oeschger events, *Clim. Past*, 9, 1029–1051, doi:10.5194/cp-9-1029-2013, 2013.
- Huber, C., Beyerle, U., Leuenberger, M., Schwander, J., Kipfer, R., Spahni, R., Severinghaus, J. P., and Weiler, K.: Evidence for molecular size dependent gas fractionation in firn air derived from noble gases, oxygen, and nitrogen measurements, *Earth Planet. Sci. Lett.*, 243, 61–73, doi:10.1016/j.epsl.2005.12.036, 2006.
- Ide, K., Courtier, P., Ghil, M., and Lorenc, A.: Unified notation for data assimilation: operational, sequential and variational, *Practice*, 75, 181–189, 1997.
- Johnsen, S. J., Dahl-Jensen, D., Gundestrup, N., Steffensen, J. P., Clausen, H. B., Miller, H., Masson-Delmotte, V., Sveinbjornsdottir, A. E., and White, J.: Oxygen isotope and palaeotemperature records from six Greenland ice-core stations: Camp Century, Dye-3, GRIP, GISP2, Renland and NorthGRIP, *J. Quaternary Sci.*, 16, 299–307, doi:10.1002/jqs.622, 2001.
- Jouzel, J., Masson-Delmotte, V., Cattani, O., Dreyfus, G., Falourd, S., Hoffmann, G., Minster, B., Nouet, J., Barnola, J. M., Chappellaz, J., Fischer, H., Gallet, J. C., Johnsen, S., Leuenberger, M., Loulergue, L., Luethi, D., Oerter, H., Parrenin, F., Raisbeck, G., Raynaud, D., Schilt, A., Schwander, J., Selmo, E., Souchez, R., Spahni, R., Stauffer, B., Steffensen, J. P., Stenni, B., Stocker, T. F., Tison, J. L., Werner, M., and Wolff, E. W.: Orbital and Millennial Antarctic Climate Variability over the Past 800 000 Years, *Science*, 317, 793, doi:10.1126/science.1141038, 2007.
- Kindler, P., Guillevic, M., Baumgartner, M., Schwander, J., Landais, A., and Leuenberger, M.: Temperature reconstruction from 10 to 120 kyr b2k from the NGRIP ice core, *Clim. Past*, 10, 887–902, doi:10.5194/cp-10-887-2014, 2014.
- Landais, A., Waelbroeck, C., and Masson-Delmotte, V.: On the limits of Antarctic and marine climate records synchronization: Lag estimates during marine isotopic stages 5d and 5c, *Paleoceanography*, 21, PA1001, doi:10.1029/2005PA001171, 2006.
- Lemieux-Dudon, B., Parrenin, F., and Blayo, E.: A probabilistic method to construct a common and optimal chronology for an ice core, *Physics of Ice Core Records*, 233–245, 2009.
- Lemieux-Dudon, B., Blayo, E., Petit, J.-R., Waelbroeck, C., Svensson, A., Ritz, C., Barnola, J.-M., Narcisi, B. M., and Parrenin, F.: Consistent dating for Antarctic and Greenland ice cores, *Qua-*

- ternary *Sci. Rev.*, 29, 8–20, doi:10.1016/j.quascirev.2009.11.010, 2010.
- NorthGRIP Community Members: High-resolution record of Northern Hemisphere climate extending into the last interglacial period, *Nature*, 431, 147–151, doi:10.1038/nature02805, 2004.
- Petit, J. R., Jouzel, J., Raynaud, D., Barkov, N. I., Barnola, J.-M., Basile, I., Bender, M., Chappellaz, J., Davis, M., Delaygue, G., Delmotte, M., Kotlyakov, V. M., Legrand, M., Lipenkov, V. Y., Lorius, C., Pépin, L., Ritz, C., Saltzman, E., and Stievenard, M.: Climate and atmospheric history of the past 420 000 years from the Vostok ice core, Antarctica, *Nature*, 399, 429–436, doi:10.1038/20859, 1999.
- Parrenin, F., Rémy, F., Ritz, C., Siebert, M. J., and Jouzel, J.: New modeling of the Vostok ice flow line and implication for the glaciological chronology of the Vostok ice core, *J. Geophys. Res.-Atmos.*, 109, D20102, doi:10.1029/2004JD004561, 2004.
- Parrenin, F., Dreyfus, G., Durand, G., Fujita, S., Gagliardini, O., Gillet, F., Jouzel, J., Kawamura, K., Lhomme, N., Masson-Delmotte, V., Ritz, C., Schwander, J., Shoji, H., Uemura, R., Watanabe, O., and Yoshida, N.: 1-D-ice flow modelling at EPICA Dome C and Dome Fuji, East Antarctica, *Clim. Past*, 3, 243–259, doi:10.5194/cp-3-243-2007, 2007.
- Rasmussen, S. O., Andersen, K. K., Svensson, A. M., Steffensen, J. P., Vinther, B. M., Clausen, H. B., Siggaard-Andersen, M.-L., Johnsen, S. J., Larsen, L. B., Dahl-Jensen, D., Bigler, M., Röthlisberger, R., Fischer, H., Goto-Azuma, K., Hansson, M. E., and Ruth, U.: A new Greenland ice core chronology for the last glacial termination, *J. Geophys. Res.-Atmos.*, 111, D06102, doi:10.1029/2005JD006079, 2006.
- Stenni, B., Buiron, D., Frezzotti, M., Albani, S., Barbante, C., Bard, E., Barnola, J. M., Baroni, M., Baumgartner, M., Bonazza, M., Capron, E., Castellano, E., Chappellaz, J., Delmonte, B., Falourd, S., Genoni, L., Iacumin, P., Jouzel, J., Kipfstuhl, S., Landais, A., Lemieux-Dudon, B., Maggi, V., Masson-Delmotte, V., Mazzola, C., Minster, B., Montagnat, M., Mulvaney, R., Narcisi, B., Oerter, H., Parrenin, F., Petit, J. R., Ritz, C., Scarchilli, C., Schilt, A., Schüpbach, S., Schwander, J., Selmo, E., Severi, M., Stocker, T. F., and Udisti, R.: Expression of the bipolar see-saw in Antarctic climate records during the last deglaciation, *Nat. Geosci.*, 4, 46–49, doi:10.1038/ngeo1026, 2011.
- Svensson, A., Andersen, K. K., Bigler, M., Clausen, H. B., Dahl-Jensen, D., Davies, S. M., Johnsen, S. J., Muscheler, R., Parrenin, F., Rasmussen, S. O., Röthlisberger, R., Seierstad, I., Steffensen, J. P., and Vinther, B. M.: A 60 000 year Greenland stratigraphic ice core chronology, *Clim. Past*, 4, 47–57, doi:10.5194/cp-4-47-2008, 2008.
- Tarantola, A.: *Inverse Problem Theory and Methods for Model Parameter Estimation*, Society for Industrial and Applied Mathematics, 339 pp., doi:10.1137/1.9780898717921, 2005.
- Veres, D., Bazin, L., Landais, A., Toyé Mahamadou Kele, H., Lemieux-Dudon, B., Parrenin, F., Martinerie, P., Blayo, E., Blunier, T., Capron, E., Chappellaz, J., Rasmussen, S. O., Severi, M., Svensson, A., Vinther, B., and Wolff, E. W.: The Antarctic ice core chronology (AICC2012): an optimized multi-parameter and multi-site dating approach for the last 120 thousand years, *Clim. Past*, 9, 1733–1748, doi:10.5194/cp-9-1733-2013, 2013.
- Vinther, B. M., Clausen, H. B., Johnsen, S. J., Rasmussen, S. O., Andersen, K. K., Buchardt, S. L., Dahl-Jensen, D., Seierstad, I. K., Siggaard-Andersen, M.-L., Steffensen, J. P., Svensson, A., Olsen, J., and Heinemeier, J.: A synchronized dating of three Greenland ice cores throughout the Holocene, *J. Geophys. Res.-Atmos.*, 111, D13102, doi:10.1029/2005JD006921, 2006.
- WAIS Divide Project Members: Onset of deglacial warming in West Antarctica driven by local orbital forcing, *Nature*, 500, 440–444, doi:10.1038/nature12376, 2013.
- Walker, M., Lowe, J., Blockley, S. P., Bryant, C., Coombes, P., Davies, S., Hardiman, M., Turney, C. S., and Watson, J.: Late glacial and early Holocene palaeoenvironmental “events” in Sluggan Bog, Northern Ireland: comparisons with the Greenland NGRIP GICC05 event stratigraphy, *Quaternary Sci. Rev.*, 36, 124–138, doi:10.1016/j.quascirev.2011.09.008, 2012.