Noteworthy Returns from Titan’s Schumann Resonance revealed by HASI-PWA Huygens Instrument

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HASI-PWA was partly designed to detect lightning activity and expected radio signals of Schumann Resonance.

About thunderstorms & lightning: None were detected since 2005...

.. but the Schumann Resonance was there in spite of some instrumental troubles!
Generation Mechanism of Titan’s Schumann Resonance (SR) -- In the absence of lightning --

**Energy source**
- Interaction of Saturn’s Magnetosphere plasma flow with Titan’s Ionosphere
- Ram-side induced Pedersen currents
- $J = \sigma_p E > 2000 \text{A} \rightarrow J/n_e q_e > C_s$
- Low Frequency Ion-acoustic Instability
- ELF modulated sheets $\rightarrow$ EM antennae

**Constraints from the data**
- Because the actual spectral frequency resolution was half of nominal, only the parameters of the 2\textsuperscript{nd} mode are determined with a 75\% confidence level.
- $F_{\text{max}} = 35.5 \pm 0.5 \text{Hz}$, Quality factor $Q = 6.5 \pm 0.5$
- Field amplitude max: $5.5 \text{mV/m/} \sqrt{\text{Hz}}$ at 100 km altitude
- (excerpt from Béghin, JGR-Planets, 2014).
Constraints on the SR cavity derived from Modal Equations

**Inputs:** \( f = 36 \text{ Hz}, Q = 6, \text{ mode index } l = 2 \)

\[
\omega_i = \frac{c}{a} \left[ l(l+1) \frac{h_1 + z_c / R_e \varepsilon_c}{h_2 + z_c} \right]^{1/2} \left[ 1 - i \left( \frac{z_c \delta / R_e \varepsilon_c + \pi \zeta / 4}{h_1 + z_c / R_e \varepsilon_c} + \frac{\pi \zeta / 4}{h_2 + z_c} \right) \right]
\]

\[
Q_l = \left| \frac{R_e f_i}{2 \Im f_i} \right| = \left[ \frac{2 z_c \delta / R_e \varepsilon_c + \pi \zeta / 2}{h_1 + z_c / R_e \varepsilon_c} + \frac{\pi \zeta / 2}{h_2 + z_c} \right]^{1/2}
\]

**Cavity parameters**

- **Atmosphere**
  - Conduction boundary: \( h_1 \)
  - Diffusion boundary: \( h_2 \)
  - Conductivity scale height: \( \zeta \)

- **Surface icy crust**
  - -- thickness: \( z_c \)
  - -- permittivity: \( \varepsilon_c \)
  - -- loss tangent: \( \delta \)

- **Water ocean**
  - Highly conductive

(Béghin et al., Icarus 2012)
Constrained Atmospheric Parameters
- 1- Source Region: Data & Models Profiles

Probable conditions during Huygens descent, derived from regular CASSINI Data

- Huygens descent occurred at middle Latitude daylight ram-side hemisphere
- A bipolar configuration similar to TA-TB-T3 flybys is assumed (Simon et al., 2013)
- Plasma and magnetic field profiles are from RPWS & MAG typical published data.
- Current sheet models are derived from reported data (e.g., Ågren et al., 2011)
- The region of largest ion-acoustic growth-rate ($\gamma$) is highlighted in red (right panel).
Constrained Atmospheric Parameters
- 2 - Ionosphere-Atmosphere Data & Models Profiles

Panel (a)
Atmospheric Pressure & Neutral Gas Temperature, from HASI (Fulchignoni et al., Nature, 2005)
Electrons supposedly thermalized (Te ~ Ti ~ Tn) below 800 km, starting from 1000 K at 1100 km.

Panel (b)
Neutral gas (N₂) density from HASI,
Electron density (Nₑ) from 1100 to 250 km from Radio Occultation (Kliore et al., JGR, 2008),
Nₑ from PWA-HASI below ~105 km to surface (Hamelin et al., PSS, 2007), 110-250 km no data.

Panel (c)
Electron collision frequency (ν/2π) & conductivity (σ) derived from PWA-HASI below 110 km,
constrained by SR conduction-diffusion boundaries and aerosols photoemission threshold up to 160 km (Mishra et al., Icarus, 2014), furthermore derived from Nₑ, N₂ and Tₑ profiles.
Constrained Structure & Physical Properties of the Subsurface

**Linked atmosphere-crust constraints**
- Crust thickness and permittivity are linked to both atmospheric boundaries \((h_1 \& h_2)\) by the modal equation for SR frequency ranging from 35.5 to 36.5 Hz.
- For instance, the degree of freedom is such as \(z_c\) is ranging from \(~40\) to \(80\) km for \(1.8 > \varepsilon_c > 2.2\), whatever atmospheric boundaries (Mishra et al., Icarus, 2014).

**Independent constraints on the crust**
- Assuming a core heat power flux range 400-650 GW (Grasset et al., PSS, 2000)
- A flux of 650 GW implies interface ocean temperature max of 260 K (pure ice)
- Presence of ammonia in the ocean would decrease the temperature down to 200 K, reducing accordingly \(58 < z_c < 80\) km.
**Merged Dispersion Equations**

- Equality of both wave vectors
  \[ k_{ia} = \frac{\omega_{ia}}{c_s} = \]
  \[ \frac{\omega_{qt}}{c} \left( 1 + \frac{\omega_p^2 / \omega_{qt}^2}{\omega_{ce} \cos \beta / \omega_{qt} - 1 + i \nu / \omega_{qt}} \right)^{1/2} \]

- The resulting wave is a quasi-transverse whistler mode, the ray path of which is nearly parallel to magnetic field lines

- The self saturation of the ion-acoustic instability yields the ELF modulation of the current sheets acting as antennas.

**Permitted SR Bandwidth**

- The ES-EM coupling mechanism in the SR source region is only possible within a range of oblique resonance constrained by the width of the dip angle \( \beta \) between \( B_0 \) and the current sheet.
Secondary Magnetic Field induced in the Atmosphere

The current-induced magnetic field in the atmosphere is derived from Biot-Savart law

$$dH = \frac{I}{4\pi} \frac{dl \sin(\alpha)}{d^2} u; \quad \text{with } u = dl \times d,$$

$$B_0(Z_p) = \frac{\mu_0 I}{4\pi} \int_{0}^{180^\circ} \sin(\alpha) \rho \, d\theta \, u,$$

- $J \sim 30 \text{ nA/m}^2 \quad \Rightarrow \quad I = YD \bar{J}_x \approx 2100 \text{ A.}$
- ELF modulation: (Kuo et al. GRL, 1999).

$$\bar{I}(\omega,t) = I \left[1 + \sum_{\omega} \delta_\omega (\exp(\pm i \omega t)) \right]$$

~ 0.25 nT at the Surface

(after Béghin, Icarus, 2015)
Induced DC-ELF Magnetic Field Strength in the Atmosphere

- With a saturation modulation rate $\Delta B/B_0$ of 0.41 Hz$^{-1/2}$, the value of $B_0$ at 100 km ($\sim 0.13$ nT) is found consistent with the EM strength of the SR signal.
- The vertical ELF modulated field lines are anticipated to induce Eddy-Foucault currents in the buried ocean.
- From MHD assessment of $B_0$ field force balance, most parts of the altitude profile are found force-free, except between 850-1000 km where a relaxation of about 3.5 nT amplitude could account for a few tens of minutes decay of a retentive “fossil” field such as observed during the T32 flyby. 
Summary

• After the confirmed absence of any detectable lightning activity in Titan’s atmosphere, the only conceivable generation mechanism of Titan’s Schumann Resonances comes from sets of ionopause current sheets induced by Saturn’s magnetosphere interaction.

• A day-light/ram-side atmospheric profile model applicable to Huygens descent is constrained by the Modal Equations of the observed 2nd SR Eigenmode.

• The same method allows to constrain the thickness and the average permittivity of the icy crust, and to reveal the presence of a liquid water ocean buried from 60 to 80 km below the surface.

• The model accounts for the observation of the 2nd mode only, because the meridional orientation of Saturn’s magnetic field at the Titan’s interface during bi-polar conditions.

• The strength of secondary magnetic field induced in the atmosphere by the current sheets is decreasing from a few nT at 1000 km down to about 0.3 nT at 200 km altitude, extending far beneath the surface and the buried ocean.

• The fleeting remanence of this magnetic field after Titan would have left the Saturn’s magnetosphere could explain the existence of a “fossil” field observed in such a case.


