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Simulating the spatial variability of nitrous oxide emission from cropped soils at the
within-field scale using the NOE model

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Abstract.

Estimating total N\textsubscript{2}O emission from agricultural soils is associated with considerable uncertainty due to the very large spatial variability of the fluxes. Thus characterizing the range of variations is of great interest. Modelling N\textsubscript{2}O fluxes remains challenging, especially at the within-field scale. The aim of this study was to test the ability of a simple process-based model, NOE (Nitrous Oxide Emission), to simulate N\textsubscript{2}O at scales finer than the field. Six field studies including 30 to 49 measurements of chamber N\textsubscript{2}O fluxes and ancillary variables were conducted in a barley/wheat field on hydromorphous soils. Three studies were made on surfaces of \(
\sim 10 \text{ m}^2
\) (defined as the local scale), and three studies along a 150-m transect (defined as the transect scale). First, the model was tested deterministically for predicting the flux spatial patterns, i.e., to try to reproduce the high flux points. Then the denitrification part of the model was tested stochastically for simulating the flux distributions by randomly generating input variables from the measured frequency distributions (Monte Carlo simulation). Measured fluxes were comprised between 0 and 1.5 mg N h\textsuperscript{-1} m\textsuperscript{-2}. The deterministic prediction of spatial patterns provided a good match with measurements in 1 of the 6 studied cases, in a transect study. Denitrification was assessed to be the main source of N\textsubscript{2}O in 5 of the 6 cases and the model satisfactorily simulated frequency distributions in 4
cases out of 5, 2 at the local scale and 2 at the transect scale. Thus this study suggests that simple process-based models such as NOE, combined to Monte Carlo methods, can be used to improve simulation of the skewed frequency distributions of $N_2O$ fluxes and provide valuable information about the range of spatial variations in $N_2O$ fluxes.

Keywords: greenhouse gas, soil fluxes, spatial variability, frequency distribution, Monte Carlo simulation.

1. Introduction

Fluxes of the greenhouse gas nitrous oxide ($N_2O$) from agricultural soils exhibit considerable spatial variability at all scales (Ambus and Christensen, 1994; Stehfest and Bouwman, 2006; van den Heuvel et al., 2009). At fine scale such as plot or within-plot scales (~10 m$^2$ to ~1000 m$^2$), $N_2O$ fluxes are characterized by the frequent occurrence of extreme values or “hotspots” (Parkin, 1987; van den Heuvel et al., 2009) which account for a significant part of the plot fluxes. $N_2O$ is produced by microbial processes in soils at the microscale (Parkin 1987) and the spatial variability results from these biological processes at local scale and from physicochemical processes acting at larger scale (region), due for example to climate, soil use and cropping practices. Studies have been conducted to represent the spatial variability at the region or country scale (Gabrielle et al., 2006, Lugato et al., 2010) with comprehensive agro-ecosystem models involving a large number of parameters requiring calibration (Lamers et al., 2007). Conversely the local scale variability and the hotspot occurrences have been much less accounted for into models (Groffman et al., 2009) and this remains a key challenge due to the difficulty to get high resolution spatial values of $N_2O$ flux drivers.

An explicit spatial determination of high flux areas at within field scale could be useful for fine scale management practices (precision agriculture). It could also help improving the modelling at larger scales. Regional or landscape-scale variability of $N_2O$ fluxes can include a significant part of the fine scale variability and thus the accuracy of model prediction at an
aggregated scale can depend on the quality of the simulations of variability at a finer scale (Pringle et al., 2008). Therefore it is very important to model correctly the fine-scale variability of N₂O fluxes.

There have been numerous spatial studies on the spatial variability of N₂O fluxes at fine scale based on measurements (e.g. Ambus and Christensen, 1994; Turner et al., 2008; Nishina et al., 2009) while to our knowledge few studies have been carried out to predict this spatial pattern at fine scale. Stacey et al. (2006) used regression kriging to improve process modelling based on flux measurements made on soil cores taken during a spatial campaign along a 1-km long transect and incubated in laboratory. The flux prediction was based on multiplicative models with rate limiting dimensionless functions of soil variables, which provide a simple tool for predicting N₂O fluxes (e.g. Hashimoto et al., 2011). The present study intends to test modelling at a finer scale (within-field scale), and to replicate spatial campaigns to assess the ability of model to account also for the temporal variations of spatial patterns.

Spatial studies based on measurements have led to the conclusion that “soil variables measured in bulk samples do not represent the integrated effect of the interaction of factors which control N₂O production at the soil microsites” (Velthof et al., 1996). This means that the deterministic prediction of local N₂O fluxes from these soil variables may in fact be very uncertain. Spatial variability of a soil variable can also be characterized by the frequency distribution. The latter gives information about the entire spectre of variation for a given variable instead of a specific value. N₂O flux distributions measured during spatial campaigns are generally skewed due to the patchy spatial pattern of N₂O fluxes produced by hotspots (Parkin 1987) and spatial studies have shown that the N₂O fluxes exhibit lognormal distribution (e.g. Turner et al., 2008; Konda et al., 2008). For such soil variables, using average of a few replicated measurements would provide a biased estimation of the mean value. As the flux distributions are varying over time, it is important to simulate the range of distributions associated with fluxes (Yates et al., 2006). Denitrification rate, which is
important in explaining the N\textsubscript{2}O fluxes, is an example of such soil variable exhibiting lognormal distributions. For the skewed distributions of the denitrification rate, Parkin and Robinson (1989) presented one study in which a stochastic simulation using a multiplicative model was preferable to a deterministic simulation. A similar approach may thus provide an efficient way to estimate the variability of N\textsubscript{2}O fluxes at fine scales.

The objectives of the present study were to measure the spatial variability of soil N\textsubscript{2}O fluxes at the within-field scale in a cropped field and to assess the capacity of a process-based multiplicative model, NOE (Nitrous Oxide Emission, Hénault et al., 2005), to predict this spatial variability. To deal with the objectives above, six measurement campaigns were carried out at two scales finer than the field (~10 m\textsuperscript{2} and a 150 m x 12 m transect) and the model was tested for 2 aims: (1) the ability to predict a single value of flux for a given location (deterministic prediction), and (2) the simulation of the flux distributions (stochastic simulation).

2.2. Material and methods

2.1 Experimental site

The study was carried out in a field on a privately owned farm in the Loir river valley, about 120 km south-west of Paris, France. This field is situated on poorly drained loamy soils similar to Gleyic Albeluvisol (IUSS-WRB, 2006). Previous N\textsubscript{2}O studies in this area clearly suggest that soil N\textsubscript{2}O fluxes are mainly due to the denitrification process (Hénault et al., 2005). The present study was conducted during the spring of 2011 and 2012, after fertilizer applications, because large N\textsubscript{2}O fluxes had already been measured in this region during the same period in previous years (Gu et al., 2011). The field had previously been under fallow, and was cropped since 2009. The crop rotation in 2010-2012 was winter wheat - winter barley - winter wheat. Tillage, the incorporation of straw residues, and sowing with winter barley took place on 3 October 2010. Nitrogen fertilizers were surface-applied on 17 February 2011 (65 kg N ha\textsuperscript{-1} ammonium nitrate pellets) and on 18 March 2011 (75 kg N ha\textsuperscript{-1} urea-ammonium nitrate solution). The crop was harvested on 10 July 2011. The next tillage,
incorporation of straw residues and sowing took place on 8 November 2011 and fertilizers were applied on 27 February 2012 (75 kg N ha\(^{-1}\) ammonium nitrate pellets) and 17 March 2012 (100 kg N ha\(^{-1}\) urea ammonium nitrate solution).

### 2.2. Quick sampling methodology

\(\text{N}_2\text{O}\) fluxes were measured by coupling an infrared quantum cascade laser (QCL) spectrometer to a “fast box”. This fast box is a mobile chamber, that does not require insertion in the soil, and that provides a rapid estimation of the fluxes when combined with an on-line analysis of gas concentration (Hensen et al., 2006; Flechard et al., 2007). The analyser was a laboratory-built instrument (known as SPIRIT) designed for the laser-based measurement of \(\text{N}_2\text{O}\) and \(\text{CH}_4\) in the 7.9 \(\mu\)m spectral range (Guimbaud et al., 2011, Gogo et al., 2011). This instrument has a special optical multipass cell (Robert, 2007) and is especially designed to work in the field. Its sensitivity at 0.7 Hz is less than 1 ppb for \(\text{N}_2\text{O}\).

The edges of the fast box are 7 cm in width with 4-cm high soft foam. The sensitivity and on-line response of the \(\text{N}_2\text{O}\) analysis make it possible to check that a good seal is obtained when the fast box is pressed on to the soil surface. The fast box is a 35 x 35 cm opaque PVC frame (18 L whole volume) and is used as a non-steady state closed chamber. Air is mixed with a low voltage fan to prevent air stratification in the chamber during the measurement. The accumulation time was typically 6 min, which is short enough to preclude any perturbation of fluxes due to an artificial temperature increase. Fluxes were calculated from the concentration increase inside the headspace, according to the HMR model (Pedersen et al., 2010), which provides a generalization of the exponential function of the model proposed by Hutchinson and Mosier (1981).

The main consideration when using a fast box is the possibility of poor sealing resulting in erroneous flux estimation. Sealing of the fast box could depend on the soil surface characteristics. A preliminary test was therefore conducted on-site to compare measurements obtained using a static chamber, with the frames inserted to 10 cm depth,
and the fast box. The soil surface was quite smooth during the growing season and the fast box was shown to provide reliable measurements (see supplementary material).

**Measurement campaigns:**

Campaigns were carried out at 2 scales: 3 times on square areas of about 10 m$^2$ (hereafter designated “S” campaigns and considered as “local scale”) and 3 times on a transect 150-m in length down the main slope of the field (hereafter referred to as “T” campaigns). In total in 6 campaigns were conducted over 2 years to cover different climatic conditions.

The three **S campaigns** were designed to provide an almost complete coverage of the ~10 m$^2$ areas and to precisely determine the frequency distributions of the flux and soil variables. Measurements were done on 01/04/2011 (S1), 14/03/2012 (S2) and 28/03/2012 (S3) on different 10-m$^2$ plots (Fig. 1). Fluxes were measured using 6 x 8 adjacent chamber deployments for S1 (covering a 2.56 x 3.36-m surface) and at 7 x 7 adjacent points for S2 and S3 (covering a 2.94 x 2.94-m surface). The fast box was carefully placed to ensure that the edges overlapped, i.e. the foam edge of the left side was placed exactly where the right edge had been placed during the previous flux measurement. Fluxes were never measured at a point where the box edge had been squeezed, so as to avoid possible effects of soil disturbance. This measuring technique made it possible to sample a large proportion (70%) of the whole surface area. Two locations on the footslope and one on the shoulder were sampled (Fig. 1).

The three **T campaigns** were carried out along a 150-m transect on 24/03/2011 (T1), 08/03/2012 (T2) and 21/03/2012 (T3). The transects were oriented along the main slope with a grid of 7 transversal lines (12-m long) with 4 replicate points (spaced 3, 6 and 3-m) and two extra-points (Fig. 1). The lines were placed 25-m apart perpendicular to the tractor wheel tracks. The exact same positions as T1 (2011), measured with a GPS system, were used in T2 (2012), then all points were moved 1 m downward in the footslope direction for T3 because soil samples had been taken from the previously sampled sites during T2.
The sampling duration of a campaign was typically 6 h, from 10:30 to 16:00 (local time), so 3-4 points were sampled twice, at the beginning and end of the experiment, to check that temporal variation of the fluxes were in any case much smaller than spatial variations.

2.3. Soil variables

Two sets of ancillary variables were measured during or just after the spatial campaigns. Firstly, the soil properties were measured by taking single soil samples from the 0-25-cm layer (corresponding to tillage depth) at each individual point on the transect, shortly after the T1 campaign. The samples were dried at room temperature, crushed and sieved to pass through a 2-mm mesh, and analysed for soil organic carbon and total N contents (dry combustion at 1000°C), soil texture (pipette method), and pH (1:5 soil:water ratio, v/v).

Secondly, the input variables for the NOE model (see subsection 2.4) were measured at each point inside the surface area sampled with the fast box, just after the flux measurement. This was repeated for each spatial sampling campaign, at both scales. Soil temperature at 10-cm depth was measured using a thermocouple (Type K, TC Direct, UK) inserted directly in the soil. Several soil samples were collected from the 0-25-cm soil layer at each flux measurement point. The first sample was used to measure gravimetric water content (GWC) and a composite of three soil replicates was prepared to determine mineral N contents.

Fresh soils were extracted with KCl solution (0.5 M) and NH$_4^+$ and NO$_3^-$ contents were determined using an automated discrete photometric analyzer (Aquakem 600, Thermo Fisher Scientific Inc., USA). Due to technical constraints, mineral nitrogen could only be measured at 8 points for S1 (4 zones of large flux and 4 of small flux).

Several bulk core replicates were taken to measure soil bulk density ($BD$). Samples were collected using a fixed-volume cylinder (500 cm$^3$) and then dried at 105 °C for 48 h. In 2011, 56 replicates were sampled along the transect (T1) and 15 replicates were taken at the footslope position (S1). In 2012, 15 replicates were taken at the top and bottom positions.

The mean $BD$ values for each sampling campaign were used to convert the GWC to Water
Filled Pore Space (WFPS), using a soil particle density of 2.65 g cm$^{-3}$ (Gu et al., 2011):

$$WFPS = GWC \cdot BD / (1 - BD / 2.65).$$

### 2.4. Data analysis and modelling

**Statistical analysis:**

The measurements were analyzed to characterize the spatial variability and to detect possible linear links between the variables. Normality tests were conducted on the direct data and the log-transformed data (Shapiro-Wilk, 5% level) because soil variables and N$_2$O fluxes are known to often exhibit lognormal distributions (Turner et al., 2008). If the distribution was considered as lognormal, the maximum likelihood method was applied to calculate the mean and standard deviation, which may differ considerably from the method of moments, and gives better results if the number of samples is sufficiently large (Parkin et al., 1988; Mathieu et al., 2006). The difference between the flux levels in each campaign was calculated by Mann-Whitney test at a significance level of 5%. Correlations between fluxes and soil variables were checked from the Pearson correlations.

**Model:**

N$_2$O production in soils is mainly due to two microbial processes: denitrification, the reduction of nitrate (NO$_3^-$) to N$_2$O and N$_2$, and nitrification, the oxidation of NH$_4^+$ to nitrite (NO$_2^-$) and NO$_3^-$ (Skiba and Smith, 2000). The NOE model (Hénault et al., 2005) had already been tested on several sites, including sites of similar soil types (Gu et al., 2014) but not to study the spatial variability at within-field scale. In this model, N$_2$O fluxes are predicted as a product of empirical functions (Hénault et al., 2005; see appendix for a complete description of functions). Two thresholds of WFPS are assumed (cf Fig. 2): $W_1$, the minimum WFPS at which denitrification can take place, and $W_2$, the maximum threshold at which nitrification can take place. $W_2$ was taken at 0.8 (Hénault et al., 2005) and $W_1$ at 0.689 (Lehuger et al., 2009; Gu et al., 2014). Above $W_1$, denitrification is assumed to further reduce N$_2$O at a fixed rate. The $r$ parameter is the fraction (between 0 and 1) of denitrification released as N$_2$O and thus...
characterizes the capacity of the soil to reduce $\text{N}_2\text{O}$ into $\text{N}_2$. A value close to 1 indicates a poor ability of the soil to reduce $\text{N}_2\text{O}$ to $\text{N}_2$ during the final step of denitrification.

NOE uses several soil parameters which can be measured following laboratory protocols: $D_p$, the potential denitrification rate (kg N ha$^{-1}$ d$^{-1}$), $z_n$, the potential nitrification rate (kg N ha$^{-1}$ d$^{-1}$), and $a$ and $b$, characterizing the response of nitrification to soil moisture (see appendix). The parameters $r$ and $D_p$ were determined from 16 samples collected at the shoulder and foot-slope positions, following the protocols proposed in Hénault and Germon (2000) and Hénault et al. (2001). The nitrification parameters $z_n$, $a$ and $b$ were based on measurements on the same soil type in a nearby region (Arrou site, Hénault et al., 2005) because the use of these parameters has also been validated by modelling $\text{N}_2\text{O}$ fluxes from soils of same type in the very close vicinity of the studied field (Gu et al., 2014). The spatial variability of the nitrification parameters has not been determined due to the low contribution of nitrification to $\text{N}_2\text{O}$ fluxes in this soil and to the very large time required for such measurements.

**Deterministic prediction:**

A deterministic model for each campaign based on soil properties at each site was tested by applying the model to individual sampling points, i.e. by using the measured soil WFPS and mineral nitrogen at an individual point for predicting the $\text{N}_2\text{O}$ flux at this point during the campaign. The agreement between predictions and measurements was tested by considering the Pearson's correlation between simulated and measured fluxes, and the root mean square error (RMSE).

**Stochastic simulation:**

Distribution simulations were performed when denitrification was identified as the main process source of $\text{N}_2\text{O}$, i.e. $\text{WFPS} > W_{r}$, as the spatial variability of the nitrification parameters has not been determined. The nitrification parameters were taken as constant and the denitrification part of NOE was used for estimating flux distributions by Monte Carlo (MC) algorithm rather than for predicting individual spatial fluxes. All calculations were made with MATLAB. A lognormal probability density function (pdf) was fitted by the maximum
likelihood method to the measured frequency distribution of the model parameter $D_p$ (denitrification potential rate). Values of $D_p$ were then randomly selected from this pdf.

Input variables exhibiting a lognormal distribution were first log-transformed. All variables were centred and reduced. Then the Cholesky decomposition method was applied to take into account measured correlations between input variables (Webster and Oliver, 2007). For this purpose, the covariance matrix of the transformed variables was calculated for each campaign and the Cholesky matrix was calculated. Sets of variables were randomly generated by multiplying the Cholesky matrix by a random vector following the normal law $N(0,1)$. Then, a back transformation of transformed variables was applied to generate values at the original scale.

These randomly generated variables were used as the driving variables of NOE for predicting a flux. The mean daily temperature was used in each case, because the flux measurements repeated at the beginning and end of each campaign showed that the range of temporal variation during the campaign was much smaller than the range of spatial variability, as previously reported by van den Heuvel et al. (2009). For each case simulation, 50000 runs were done to check the stability of the results. The simulated distributions were truncated at the 2.5 and 97.5% quantiles, to exclude unrealistic values due, for example, to extremely high or zero potential rates of denitrification. The simulated frequency distribution of the N$_2$O fluxes was compared with the measured one by applying a $\chi^2$ homogeneity test ($p < 0.05$). For this purpose, the fluxes were systematically attributed to classes such that the theoretical number of data in each class was always 5. The upper class, for which the theoretical number of data was less than 5, was grouped with the previous one.

3. Results

3.1 Measurements of N$_2$O fluxes and soil variables

The N$_2$O fluxes were significantly larger during the 2011 campaigns (T1, S1) than during the 2012 campaigns ($p < 0.05$ for transects and $p < 0.001$ for S surfaces). The largest difference
was measured between S1 and S3 (Fig. 3) and was almost one order of magnitude. The fluxes exhibited a large spatial variability and the minimum and maximum fluxes always differed by more than one order of magnitude even at the local scale (S). The frequency distributions for all the measurements were skewed and could be considered as lognormal (Table 1). The variation of frequency distributions over time was smaller at the S scale (CV from 68 to 96%) than at the T scale (CV from 82 to 311%). The largest CV was measured in T1 when a gradient of N₂O fluxes was observed along the main slope. The N₂O fluxes, VWC and NO₃⁻ contents correlated with elevation in T1 but not in T2 and T3 (p = 0.57 and 0.72 for T2 and T3, respectively).

The spatial variability of soil texture (Table 2) was similar to the variability previously reported at the field scale (e.g. Cambardella et al., 1994). No significant difference was found in the surface layer bulk density between locations. For T1, a significant correlation was observed between fluxes and WFPS \((p < 0.001, r = 0.78)\) and between fluxes and the NO₃⁻ content \((p < 0.001, r = 0.74)\). No significant correlation was found between N₂O fluxes and soil variables for the other campaigns. Finally, WFPS usually exhibited normal distributions, whereas the mineral nitrogen distributions were nearly always asymmetrical (Table 1 and Fig. 4).

### 3.3. Deterministic modelling of N₂O fluxes

The distribution of the \(D_p\) parameter could be considered as lognormal and calculation of the mean by the maximum likelihood method gave a value of 6.1 kg N ha\(^{-1}\) d\(^{-1}\). The value measured for the \(r\) parameter was 0.83, indicating the relatively poor capacity of this soil to reduce N₂O to N₂. In this study, the WFPS was above the presumed threshold of denitrification \(W_i\) in all campaigns except S3. Therefore, only a weak proportion of the flux was predicted to originate from nitrification i.e., 5% for S1; 13% for S2; 5% for T1; 5% for T2 and 10% for T3. For S3, the predicted proportion of N₂O produced by nitrification was 94% of the total flux.
When all the data were plotted together, predicted and measured N\(_2\)O fluxes were closely correlated (\(r = 0.73, p < 0.001\), Table 3 and Figure 5 a.). The agreement was good when the mean predicted flux versus the mean measured flux was considered for each campaign (Fig. 5 b. and Table 3). This means that the model could successfully predict variations over time.

When each campaign was considered separately, the agreement between the predictions and the measurements per treatment was generally poor: the RMSE were as large as or larger than the mean measured flux and there was no significant correlation between the predicted and measured fluxes (\(p > 0.1\) for S1, S2, S3, T2 and T3, Table 3). Nevertheless, a very good association between the predicted and measured data (\(p < 0.0001\), \(r = 0.88\), Fig. 5 a. and Table 3) together with reasonable accuracy (RMSE of 0.118 mg N m\(^{-2}\) h\(^{-1}\)), was obtained for T1.

### 3.4 Modelling the relative frequency distributions of N\(_2\)O fluxes.

The measured distribution of the \(D_p\) parameter was first fitted by a lognormal function to generate the pdf used for the MC simulations (Fig. 6). All asymmetrical distributions (Table 1) of soil input variables were log–transformed before applying the Cholesky method, regardless of whether the distribution was significantly different from a lognormal distribution, so as to render the distributions symmetrical.

The MC simulation was not applied to the S3 campaign because the main source of N\(_2\)O was probably nitrification due to low WFPS. When applied to the other campaigns, the simulated and measured flux distributions were not significantly different for the S1 and S2 campaigns at the local scale or for the T1 and T3 campaigns at the transect scale (\(\chi^2\) test, \(p > 0.05\), Table 4 and Fig. 7). For the T2 campaign, the mean flux produced by MC simulation was significantly smaller than the measured mean flux (\(\chi^2\) test, \(p < 0.001\), Table 4).

### 4. Discussion
The main aim of this study was to test the ability of a process-based model, NOE, to predict spatial variations in N₂O fluxes, by 1) predicting the individual N₂O fluxes at a fine scale (field or few m²) and 2) stochastically simulating the frequency distributions of fluxes measured during spatial campaigns.

4.1. Measured spatial variability of N₂O fluxes:
A quick flux measurement method involving a fast box was chosen for this study. It was extremely simple to use because it does not require special field preparation. Agreement between the measurements obtained by fast box and in static chambers was good (see supplementary material), which indicates that the fast-box method enabled to identify hotspots. Other authors have also recommended the fast box to minimize ecosystem disturbance due to long closure time (Flechard et al., 2007) and noted that, due to the rapid response of the QCL spectrometer, the number of measurements can be increased, and thus the opportunities for measuring the spatial variability of N₂O fluxes. In the present study, the measured variability was consistent with the spatial variability of fine-scale studies described in the literature. Indeed, the flux distributions in these studies were often considered as lognormal (Ambus and Christensen 1994, Ball et al 1997, Röver et al 1999, Turner et al 2008, Konda et al., 2008, Nishina et al., 2009) and the CV generally ranged from ~50% to 300 % (e.g. Velthof et al., 1996, Ambus and Christensen, 1994, Turner et al., 2008).

4.2. Overall quality of N₂O flux predictions:
Although models are generally used to predict temporal variations in N₂O fluxes, they often provide better predictions of cumulated fluxes over a season or year, than of daily variations (Lehuger et al., 2009; Beheydt et al., 2007). For example, Jarecki et al. (2008) reported a correlation coefficient of 0.37 between measured and predicted fluxes with the DAYCENT model, and Beheydt et al. (2007) reported RMSE values of between 0.7 and 1.4 mg N m⁻² h⁻¹ for maximum N₂O flux values of about 3.3 mg N m⁻² h⁻¹ with the DNDC model in long-term field experiments. Hergoualc'h et al. (2009) used two rate-limiting models (NOE and NGAS) to predict the temporal dynamics of N₂O fluxes on Costa-Rican coffee plantations and...
reported that the correlation coefficient between measured and predicted fluxes was 0.57 with a daily time step and 0.94 with a seasonal time step. The \( RMSE \) in this study was below 0.04 mg N m\(^{-2}\) h\(^{-1}\) for maximum N\(_2\)O flux values of about 1 mg N m\(^{-2}\) h\(^{-1}\). In our study, the only campaign in which we observed a good match between measured and predicted fluxes was T1, with a correlation coefficient of 0.88 and an \( RMSE \) of 0.188 mg N m\(^{-2}\) h\(^{-1}\) for a measured range of about 0 to 1.35 mg N m\(^{-2}\) h\(^{-1}\) (Tables 1 and 3). Thus the \( RMSE \) was smaller than the \( RMSE \) reported by Beheydt et al. (2007) but larger than that reported by Hergoualc’h et al. (2009). However the temporal variability between campaigns can be determined from the predicted mean flux at each date (6 points, cf Fig. 5.b.) and the resulting \( RMSE \) is then 0.058 mg N m\(^{-2}\) h\(^{-1}\) (Table 3), which is within the range of the \( RMSE \) values reported by Hergoualc’h et al. (2009).

Very few studies aimed at the spatial prediction of individual N\(_2\)O fluxes, especially at a fine spatial scale. Milne et al. (2005) and Stacey et al. (2006) used the same flux database from cores sampled along a 1-km transect on the same day. Both studies were intended for the assessment and optimization of models, and multiplicative models based on rate-limiting functions, i.e. based on similar principles to NOE, were tested. A correlation coefficient \( r = 0.67 \) to 0.7 (Milne et al., 2005) and an \( RMSE \) between 36 and 52 \( \mu \)g N kg\(^{-1}\) d\(^{-1}\) were reported for N\(_2\)O fluxes ranging from 0 to about 300 \( \mu \)g N kg\(^{-1}\) d\(^{-1}\) (Stacey et al., 2006). If it is assumed that, in our study, N\(_2\)O was only produced in the top 25 cm of soil, then the \( RMSE \) for the T1 campaign was 2.10 \( \mu \)g N kg\(^{-1}\) d\(^{-1}\) for N\(_2\)O fluxes ranging from 0 to 24 \( \mu \)g N kg\(^{-1}\) d\(^{-1}\).

The performance of the NOE model was therefore quite similar to that reported in the above studies, but only for the T1 campaign. This emphasizes the need to evaluate models spatially at several dates.

When used deterministically, the NOE model reproduced the T1 campaign well, but poorly predicted the individual N\(_2\)O fluxes in the other T (T2-T3) and the three S campaigns. A clear correlation between N\(_2\)O fluxes, WFPS, NO\(_3\)^- contents and field elevation was only observed for the T1 campaign. In this case, the distribution of nutrients and water along the transect...
was probably controlled by topography-induced transfer, which in turn controlled the N₂O fluxes. Similar effects have been reported for denitrification by Pennock et al. (1992) and for N₂O fluxes by Nishina et al., (2009) and Vilain et al. (2010). This effect may only be occasional because conditions during the early spring of 2012 were very dry and the field slope is gentle (1.6%), which would explain why an effect was not measured in T2 and T3. The good prediction of individual N₂O fluxes for the T1 campaign can be explained by the good correlation of both the N₂O fluxes and model input variables at the same elevation. The MC simulation of flux distribution could be tested under conditions favorable for denitrification, i.e. T1, T2, T3, S1 and S2, but not S3 when nitrification was probably dominant. The simulated and observed flux distributions were not significantly different, except for the T2 campaign. We hypothesize that the T2 results were influenced by the associated meteorological conditions. The T1, T3 and S2 campaigns were carried out under sunny conditions after at least 3 dry days. Only S1 was conducted in wet soil, after a minor rain event (8.2 mm within 3 days), and there was probably very little evaporation as the relative humidity remained at 95% throughout the day. In contrast, the T2 campaign was carried out on the first sunny day after 5 days of rain (12 mm from 2-7 March 2013) following a dry period. It has often been reported that peak N₂O production is triggered by soil rewetting (Kim et al., 2012). Thus, one possible explanation may be that the model cannot reproduce correctly N₂O fluxes during the transitory period following rewetting, although no conclusion can be drawn from this single campaign. Although a satisfactory agreement between the predicted and measured fluxes was only obtained for T1, the measured distributions could be reproduced in 4 cases out of 5: two out of three at the scale of ~10 m² (S1 and S2) and 2 at the transect scale (T1 and T3). This suggests that the interactions between control variables are adequately represented by the model. The deterministic prediction at very local scale fails because soil variable measurements are not representative of the volume where N₂O is produced. But the correct representation of the denitrification
process by the model enables to estimate the flux distributions from the soil variable
distributions.

4.3. Interest of simulating distributions:

As the frequency distributions of flux change over time, it is important to test the ability of a
model to reproduce the range of measured distributions (Yates et al., 2006). Even if the
location of largest N$_2$O fluxes, and thus the spatial pattern of N$_2$O fluxes, cannot be correctly
predicted, the frequency distribution can provide information about the range of variations in
N$_2$O flux.

Flux distributions were simulated from the measured distributions of their controlling factors.
Assessments of the flux range can be used to determine an appropriate number of soil
measurements. A resampling method, for example, was used to estimate the number of
measurements (n) which would have been required to simulate an estimated mean flux
within ±10% of the true mean at the 95% uncertainty level, under the conditions measured
during campaigns where denitrification was found to be dominant. The distributions fitted to
the measured WFPS and NO$_3$ content distributions were assumed to be the true
distributions and the N$_2$O flux distribution resulting from applications of the NOE model was
assumed to be the true N$_2$O flux distribution. The n samples were randomly selected within
these distributions. These data were then used as input for the NOE model and the mean
N$_2$O flux was estimated by maximum likelihood method and compared to the mean of the
real flux distribution. The number of measurements required to obtain a 10% level of
uncertainty was 65, 100, 210, 205 and 390 for S1, S2, T1, T2 and T3, respectively. This is
still of interest because in many cases, it is simpler to ensure extensive coverage of the soil
variables rather than of the N$_2$O fluxes. These large numbers of measurements also need to
be compared with the number of N$_2$O flux measurements required to obtain the same
uncertainty for the mean flux reported in other spatial studies. For example, Folorunso and
Rolston (1984) claimed that between 156 and 4117 measurements would be required to
obtain a sample mean within ±10% of the true mean of the ln-transformed flux, and that this
result could not be used to determine the non-transformed flux. However the quantification of
fluxes at a given scale depends on information about the mean non-transformed flux.
Practically, even if it is not possible to provide such a large number of measurements, this
study emphasizes the need to focus spatial sampling effort on peak periods of N₂O fluxes
due to the transitory character of these fluxes. Accumulation chambers remain the most
widely used technique for such measurements due to their simplicity. So a correct simulation
of the flux distribution during the periods of large fluxes would enable improving the
estimation of total flux without bias due to low sampling coverage. A further step into the
modelling of spatial variability of fluxes would then be to provide parameterization for the
simulation of the distribution of soil variables with an agro-ecosystem model, before using
these simulated distributions as input of the NOE model. This would in turn be useful to take
into account the local spatial variability and measurement uncertainty in model up-scaling
(Whelan and Gandolfi, 2002).
The general agreement of our measurements with previous studies suggests that our case
can provide a good example of the spatial variability in N₂O fluxes from croplands. Although
the method needs to be further investigated with different soil types and different crops, the
findings imply that it could be useful for simulating flux distributions at other sites with similar
ranges of WFPS and soil mineral nitrogen content.

5. Conclusion
N₂O fluxes, like many soil properties, display a very large spatial variability and it is important
to quantify the range of this variation in the form of a confidence interval or even better by
describing the frequency distributions of such variations, even in modelling studies. The aim
of this study was to test the feasibility of predicting spatial variations in N₂O fluxes from
cropped soils by applying the simple process-based model NOE. It is generally recognized
that, at such fine scale, linking hotspots to soil properties or predicting individual fluxes is
difficult, which certainly explains why the simulation did not match the measured fluxes in all
but one campaign. For this transect campaign, a spatial flux pattern was observed, probably
linked to a strong gradient of soil water content along the slight slope of the field due to the climatic conditions. It is thus important to evaluate spatial simulations at different dates.

The stochastic simulation of distributions with the denitrification part of the NOE model was then tested as spatial information on nitrification parameters were not available. Input variables were randomly generated taking into account the measured distributions of the input variables and possible correlations between them. For one campaign, the dominant microbial process producing N$_2$O was probably nitrification due to low WFPS. The stochastic simulation was tested for the other 5 campaigns and satisfactorily simulated N$_2$O fluxes in 4 of these 5 cases, two at the local scale (~10m$^2$) and two at the transect scale. The reason of failing for the 5$^{th}$ case has to be further investigated. Nevertheless this suggests that the NOE model provides an adequate simulation of N$_2$O flux distribution within this range of WFPS. Simple process-based models of fluxes, such as NOE, could thus serve as useful tools for simulating flux distributions and describing the range of variations in N$_2$O fluxes at the within-field scale.

**Acknowledgments**

We gratefully acknowledge A. Ayzac, G. Giot, C. Pasquier, C. Lelay and P. Courtemanche for their technical assistance during field measurements. This work was supported by the Région CENTRE, the Fonds Européen de Développement Régional (FEDER) and INRA through the SPATIOFLUX Project, and also by the Labex Voltaire (ANR-10-LABX-100-01).

**Appendix: Equations in NOE**

Denitrification functions:

$F_N$ and $F_W$ are the effects of soil NO$_3^-$ content ([NO$_3^-$], mg N kg$^{-1}$) and water-filled pore space (WFPS) respectively.

$$F_W(WFPS) = \left( \frac{WFPS - W_l}{1 - W_l} \right)^{1.74}$$

(1)
\[ F_N = \frac{[NO_3^-]}{km_1 + [NO_3^-]} \]  

where \( km_1 \) denotes the half-saturation constant (mg N kg\(^{-1}\)). \( km_1 \) is calculated at each gravimetric soil water content (GWC), corresponding to 22 mg N kg\(^{-1}\) at GWC=27\% (Hénault and Germon, 2000).

Nitrification functions:

\[ N_{NH_4} = \frac{[NH_4^+]}{km_2 + [NH_4^+]} \]  

where \( km_2 \) denotes the half-saturation constant (mg N kg\(^{-1}\)). \( km_2 \) is calculated at each GWC, corresponding to 2.6 mg N kg\(^{-1}\) at GWC=27\% (Hénault et al. 2005).

\[ N_W(WFPS) = a \cdot GWC + b = a \cdot WFPS \cdot \left( \frac{1}{BD} - \frac{1}{2.65} \right) + b \]  

The response function of temperature (\( T \) in °C) is common to both processes:

\[ F_T(T) = N_T(T) = \begin{cases} 
\exp \left( \frac{(T - 11) \ln(89) - 9 \ln(2)}{10} \right) & \text{if } T < 11^\circ \\
\exp \left( \frac{(T - 20) \ln(2.1)}{10} \right) & \text{if } T \geq 11^\circ 
\end{cases} \]  

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Figures:

Figure 1: Study plot. The black dots show sampling points on the T1 and T2 transects (150 m x 12 m). The grey squares indicate the places where the 3 x 3 m² surfaces were sampled in the dense surface sampling experiments.

Figure 2: Basic principle of the NOE model. See text for details.

Figure 3: N₂O fluxes measured at spatial (S) (left) and at transect (T) scales (right). Horizontal axes indicate distance (m).

Figure 4: Measured frequency distributions of WFPS (left), NO₃⁻ content (middle) and NH₄⁺ content (right). Blue line shows the normal or lognormal fitted pdf.

Figure 5 a. Predicted fluxes versus measured fluxes for the deterministic simulation. b. Mean predicted fluxes versus mean measured fluxes for each campaign for the deterministic simulation. The dashed black line is the linear fit of the deterministic results. The thick black line indicates the 1 to 1 line.

Figure 6: Frequency distribution of the potential denitrification parameter Dp. Blue line shows the lognormal fitted pdf.

Figure 7: Measured frequency distributions of N₂O fluxes (left) and simulated distributions (right). Blue line shows the lognormal fitted pdf.
Table 1: Summary statistics of measured variables. For the distributions, n indicates normality, ln lognormality and x indicates that both possibilities were rejected. F(N₂O) is the N₂O flux in mg N m⁻² h⁻¹, WFPS the water filled pore space, NO₃⁻ and NH₄⁺ the NO₃⁻ and NH₄⁺ content in mg N kg⁻¹ soil.

Table 2: Soil properties along the transect. Units are g kg⁻¹ except for C/N ratio and pH.

Table 3: Summary of deterministic simulation results. Mean fluxes are given in mg N m⁻² h⁻¹.

Table 4: Summary of results from the distribution simulation. Mean fluxes are given in mg N m⁻² h⁻¹. Bold characters indicate that the χ² test shows no significant differences between the measured and simulated distributions.
Figure 1:

![Image of a map with soil samples labeled S1, S2, and S3, showing nitrous oxide emission data.](image-url)

Legend:
- **S1**: Soil sample 1
- **S2**: Soil sample 2
- **S3**: Soil sample 3

**X-axis**: 0, 10, 20 meters

**Y-axis**: Nitrous oxide concentration (ppm)

**Legend**:
- **Black dot**: Nitrous oxide receptor
- **Square**: Sampling point
Figure 2

\[ W_{FPS} < W_i \]

\[ F_{N_{i,O}} = N_R \]

\[ W_{FPS} < W_2 \]

\[ F_{N_{i,O}} = r \cdot (D_R + N_R) \]

\[ F_{N_{i,O}} = r \cdot D_R \]

Where:

\[ N_R = z_N \cdot N_T(T) \cdot N_{NH_4} \cdot N_{WPS}(WFPS) \]

Nitrification rate

\[ D_R = D_p \cdot F_T(T) \cdot F_{NO_3} \cdot F_W(WFPS) \]

Denitrification rate
Figure 3

1. \( N_2O \) flux (mg N h\(^{-1}\) m\(^{-2}\))

2. \( NO \) flux (mg N h\(^{-1}\) m\(^{-2}\))

3. \( N_2O \) flux (mg N h\(^{-1}\) m\(^{-2}\))

4. \( NO \) flux (mg N h\(^{-1}\) m\(^{-2}\))

5. \( N_2O \) flux (mg N h\(^{-1}\) m\(^{-2}\))

6. \( NO \) flux (mg N h\(^{-1}\) m\(^{-2}\))
Figure 4

Relative frequency of soil properties across different sites (S1, S2, S3, T1, T2, T3).

- Top row: Relative frequency of wFPS (%) for S1 and S2.
- Middle row: Relative frequency of NO$_3$ (mg N kg$^{-1}$) for S1 and S2.
- Bottom row: Relative frequency of NH$_4$ (mg N kg$^{-1}$) for S1 and S2.

Note: The y-axis represents the relative frequency, and the x-axis represents the soil property concentration.
Figure 5

a. 

![Graph showing predicted vs. measured flux with data points for T1, T2, T3, S1, S2, S3]

b. 

![Graph showing simulated vs. measured flux with error bars for T1, T2, T3, S1, S2, S3]
Figure 6

![Graph showing relative frequency versus denitrification potential parameter (kg N ha\(^{-1}\)).]
Figure 7

![Figure 7](image-url)
Table 1

### a. Table 1

<table>
<thead>
<tr>
<th>variables</th>
<th>n</th>
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<th>range</th>
<th>CV</th>
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<td>0.413</td>
<td>0.104-1.421</td>
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<td>ln</td>
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<td>0.015-0.238</td>
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<td>71.2-82.1</td>
<td>3%</td>
<td>n</td>
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<td>ln</td>
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### b. Table 1

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Table 3

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<td>S3</td>
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<table>
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<td><strong>T and S</strong></td>
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<td>&lt;<strong>0.001</strong></td>
<td><strong>0.168</strong></td>
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Mean fluxes of each campaign:
- **Determinist**
  - r: 0.97, p: 0.002, RMSE: 0.058
- **Stochastic**
  - r: 0.98, p: 0.002, RMSE: 0.033
### Table 4

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<thead>
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<td>T3</td>
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