Self potential signals preceding variations of fumarole activity at Merapi volcano, Central Java.

S. Byrdina^{a,*}, C. Rücker^b, M. Zimmer^c, S. Friedel^d, U. Serfling^e

^a*ISTerre, Université de Savoie, Equipe Géophysique des Volcans, IRD R219, CNRS, UMR 5559, F-73376 Bourget du Lac, France*

^b*Technische Universität Berlin, Institut für Angewandte Geowissenschaften, Ackerstr. 76, D-13355 Berlin*

^c*Helmholtz-Centre Potsdam GFZ German Research Center for Geosciences, Telegrafenberg, 14473 Potsdam, Germany*

^d*COMSOL Multiphysics GmbH, Technoparkstr. 1, 8005 Zürich, Switzerland*

^e*GGL Geophysik und Geotechnik Leipzig GmbH, Bautzner Str. 67, 04347 Leipzig*

Abstract

This paper analyzes simultaneous self-potential and gas temperature variations recorded at Merapi volcano in spring 2001, the dry season shortly after the volcanic crisis 2001. Temporal variations of fumarole gas temperature show characteristic quasi periodic signals at scales 1-8 hours and amplitudes up to ten degrees. We propose a simple graphical technique combining a wavelet scalogram and a cross-correlation analysis to demonstrate that the variations of gas temperature are systematically preceded by self-potential variations at the same scales. The influence of meteorological variations on these correlated signals can be ruled out. Rather, we suggest them to be related to the magma degassing in the upper conduits of the volcano. We discuss a semi-qualitative model to explain this correlation and the observed phase shift of about two hours.

Keywords: self-potential monitoring, hydrothermal system, gas monitoring, Merapi

1. Introduction

Merapi is one of the most active volcanoes in Indonesia, located on the Java Arc (Figure 1), where the Indo-Australian Plate is subducted beneath the Java Trench. Its characteristic activity consists of sequences of growth and gravitational collapse of a viscous andesitic dome (Voight et al., 2000) producing pyroclastic flows. In addition to this regular activity, Voight et al. (2000) describe

*Corresponding author

Email addresses: svetlana.byrdina@univ-savoie.fr (S. Byrdina), carsten.ruecker@tu-berlin.de (C. Rücker), martin.zimmer@gfz-potsdam.de (M. Zimmer), sven.friedel@comsol.com (S. Friedel), serfling@ggl-gmbh.de (U. Serfling)

several major eruptions with $VEI > 2$ since 1768, like the explosion in 1822 which created a circular crater with 600 m diameter; the 1872 explosion completely destroyed the dome and created an oval crater 500 m deep; the eruption in 1930 with dome destruction and pyroclastic flows traveling up to 12 km. The time interval studied in the current paper was preceded by few months by a partial dome collapse, occurred in early 2001. This minor event was typical for the activity of Merapi volcano in twentieth century. Two months before the first dome collapse an increase in frequency of volcano-tectonic and multi-phase earthquakes was observed, thereafter numerous pyroclastic flows were encountered which accompanied the growth of the new lava dome. The new dome reached a total volume of about $1.4 \times 10^6 \text{ m}^3$ before it partially collapsed in two stages on January 28 and February 10.

The latest to date explosive crisis which happened in October-November 2010 was probably the most violent eruption since 1872. During this eruption with $VEI \approx 4$, a new summit crater with a diameter of 400 m was created, released $\approx 0.44 \text{ Tg}$ of SO_2 , caused evacuation in a 20 km radius from the volcano and more than 350 fatalities (Surono et al., 2011). This dangerous eruption behavior with possible influence of external factors like rainfall or tectonic activity (e.g. Voight et al., 2000; Friedel et al., 2004; Harris and Ripepe, 2007; Surono et al., 2011) motivates further studies aimed to improve multi-parameter monitoring techniques.

Traditional Merapi monitoring techniques include seismology, deformation, in-situ sampling of gas emissions, and petrology (e.g. Surono et al., 2011, and references there) by the Indonesian Center of Volcanology and Geological Hazard Mitigation and its observatory and technology center in Yogyakarta, BPPTK. Continuous monitoring of geochemical parameters at the summit of Merapi was conducted during few weeks in 1998 and in 2000, when an automatic gas monitoring unit comprising gas chromatograph, an alpha scintillometer and temperature sensor was installed at Solfatara field Woro (Zimmer and Erzinger, 2003). The authors observed cyclic variations in the chemical composition of the gas associated with variations of its temperature. The gas temperature was found to increase when the concentration of the CO_2 increased and the concentration of H_2O decreased (Figure 2).

The self-potential method is often used to characterize the extension of hydrothermal system, complimentary to geochemical data (Lénat et al., 2000; Finizola et al., 2004; Revil et al., 2008; Byrdina et al., 2009). The major contributions of self-potential are created by the flow of the

pore water dragging an excess of electrical charges existing in the vicinity of the mineral/water interface, the so-called streaming potential (e.g. Nourbehecht, 1963; Ishido and Mizutani, 1981; Revil et al., 1999, 2003; Crespy et al., 2008). At Merapi volcano, a continuous monitoring of self-potential and ground temperatures was conducted from August, 2000 to July, 2001, in order to retrieve information on subsurface water flow variations related to the volcanic activity (Friedel et al., 2004). A clear correlation between self-potential, and seismic signals in ultra low frequency band was observed before the volcanic crisis in the early 2001, mostly during the rain season in November 2000 - January 2001 (Byrdina et al., 2003). Because of the strong influence of rainfall on self-potential and temperature, only repetitive or high-amplitude signals could be studied during the rain season. The present work deals with analysis of gas flow characteristics in Woro fumarole in dry season and during the period of relative quiescence following the 2001 volcanic crisis. The aim of the present work is to detect the common gas temperature and the self-potential signals reflecting the variations in magmatic degassing during an inter-eruptive period.

2. Experiment and Instruments

A continuous monitoring station for electrical field and ground temperatures was installed in August 2000, in 200 m distance from the dome and several meters away from the fumarolic vents of Woro (Figure 1 b). The station included three electrode pairs, two in North-South direction with lengths of 50 and 75 m and one in East-West direction of 50 m length. We called them in the following the SP dipoles U_{21} , U_{43} , and U_{65} . Two electrodes, E_2 and E_5 , were placed in a direct vicinity of fumarole vents, E_5 was only few meters away from the fumarole temperature sensor GC. We used non-polarizable Ag/AgCl electrodes designed by the Geophysical Instrument Pool Potsdam. Voltage differences were sampled at 20 sps with a resolution of $0.2 \mu\text{V}$. Each electrode was equipped with a PT1000 temperature sensor at the depth of installation 0.7-0.8 m. The temperature data were sampled at 4 sps with a resolution of 0.1°C using a Guralp CMG 24 digitizer with GPS clock synchronization. We refer to Friedel et al. (2004) for a more detailed description of the setup. In the following, analogous to the notation of Friedel et al. (2004), the self-potential data are referred to as $U_{21} = U_2 - U_1$, the potential difference measured between the electrodes E_2 and E_1 etc. Similarly, the difference of the ground temperature at the electrode positions (called in the following electrode temperature difference) $T_{21} = T_2 - T_1$ etc. Ground temperatures varied

between 40 and 70 °C except for sensor T_4 whose maximal temperature reached 100 °C. In order to obtain the same sampling as for gas temperature, all data were down-sampled to 1 sample per minute using median filtering. The median was preferred to simple moving averages or low-pass filters in the frequency domain because of its robustness against outliers.

The fumarole gas temperature sensor, a Ni-Cr/Ni thermocouple at 30 cm depth, replaced a gas chromatograph installed in 1998 at a location indicated as GC in Figure 1 c (for more details see Zimmer and Erzinger, 2003). During the main dome collapse of February 10, 2001, the station was partially destroyed and was be reactivated 2 months later starting on April 6, 2001.

3. Data analysis

The classical measure of the correlation between two time series with a time shift between them is given by a cross-correlation function. Its Fourier transform, the cross power spectral density, gives the frequency range of correlation. This analysis is best suited for stationary signals with good signal-to-noise ratio, otherwise the maximum of the cross-correlation function is not pronounced enough to identify a correlation between the time series (Figure 3 a, b).

To find the correlation of intermittent and noisy signals, we propose a technique based on wavelet analysis and cross correlation analysis which allows to detect both the time scale with maximal signal correlation and a possible time-shift. The idea is to use the time-frequency representation offered by the wavelet analysis; and to use as an advantage a compact support of the wavelet basis in order to focus the cross-correlation analysis on the significant time scales of the signal.

3.1. Wavelet transform. Time-frequency representation.

The complex wavelet transforms the signal $x(t)$ using the dilated and time shifted versions of a basis function called basis wavelet ψ Mallat (1999):

$$W(a, b) = a^{-1/2} \int_{-\infty}^{\infty} x(t) \psi^* \left(\frac{t-b}{a} \right) dt \quad (1)$$

where the wavelet coefficients $W(a,b)$ give the transformed signal as a function of the translation parameter b , and the dilatation parameter a (scale). We used the Morlet wavelet which is a complex sinus wave with a Gaussian envelope

$$\psi(t) = \pi^{-1/4} e^{i\omega_0 t} e^{-t^2/2}. \quad (2)$$

We used logarithmically equidistant values for a (dyadic grid). In this notation, the time is unitless. This wavelet was used to plot the time-frequency wavelet spectrum – the scalogram given by $|W(a, b)|^2$. The Fourier transform of the Morlet wavelet is a Gaussian with positive frequencies for $\omega_0 \geq 5$ (we used $\omega_0 = 5$): The scale - frequency relationship of the Morlet wavelet is given by

$$\omega = \frac{\omega_0}{a} \quad (3)$$

The wavelet coefficients at every scale are the Hilbert transformed original data (analytic signal) bandpass filtered by the Gaussian envelope with center frequency ω given by equation 3.

3.2. Linear cross-correlation function of the wavelet coefficients

The next step is the calculation of the linear cross-correlation function $P(X, Y)$ where the data X and Y are replaced by their complex wavelet coefficients $Wx = W_x(a, b)$ and $Wy = W_y(a, b)$

$$P_{Wxy}(a, b) = \frac{\sum_i^{N-b} (Wx_{i+b} - \overline{Wx}) (Wy_i - \overline{Wy})}{\sqrt{\left(\sum_i^N (Wx_i - \overline{Wx})^2\right)} \sqrt{\left(\sum_i^N (Wy_i - \overline{Wy})^2\right)}} \quad (4)$$

for each scale a and for reasonable time shifts b . The cross-correlation function of the wavelet coefficients $P_{Wx, Wy}(a, b)$ is then plotted as a function of scale a and time delay b between both time series. If the value of $P_{Wx, Wy}(a, b)$ is close to unity at a scale a_d and at a time shift b_d , there is a correlation between signals with dominant frequency corresponding to the scale a_d and a time delay b_d . Figure 3 shows an example of synthetic time series containing intermittent signals superimposed with random noise. The cross-correlation plot of wavelet coefficients in Figure 3 c possesses a clear maximum. Its ordinate indicates the scales at which the data contain correlated signals, and its abscissa indicates the time shift between them.

4. Data basis and Observations

Figure 4 shows gas temperature data, self-potential and ground temperature data after the end of the rain season and re-installation of the sensor in April and till June 2001. Ground temperatures T_4 and T_6 are not presented here. Sensor T_4 was placed in a permeable erosive channel with much higher temperatures (up to 100° C) and larger temporal variations than the other temperature sensors, and sensor T_6 was damaged all through the period of observation.

Though no rain data in this time interval are available, we suggest that no rainfall happened between Julian days 110 and 137 (from April 19th to May 16th). As detailed by Friedel et al. (2004), both self-potential and electrode temperature difference data at this station respond similarly to the rainfall with typical high amplitudes (up to 300° C in gas temperature and 50 mV in self-potential data), sharp onset and exponential decay; moreover, a high linear correlation between the self-potential and electrode temperatures is usually observed during the rainfall. The absence of such correlated self-potential and electrode temperature signals, as well as the small amplitudes of variations in all observables suggest that no rainfall happened in this time interval, which was therefore chosen for a closer study. Amplitude spectra of the time series presented in Figure 4 can be seen in Figure 5. Daily and semi-diurnal variations dominate the ground temperature and self-potential spectra but are less spectacular in the spectrum of gas temperature where a large part of the signal energy is distributed between 2 and 8 hour periods. Interestingly, the self potential spectra also contain some signal energy at these periods, in contrast to ground temperature data.

To explore the correlation between self-potential and gas temperature, cross-correlation plots of wavelet coefficients were calculated as described in section 3; they are shown in Figure 6 a, b and c. The scale range of correlation between 1 and 8 hours corresponds roughly to the typical signal durations observed by Zimmer and Erzinger (2003) in gas concentration and gas temperature data. These periods are hardly visible in the Fourier spectra of the gas temperature in Figure 5 a. The broad maximum of the correlation is located at scales 1.5-8 hours and a time shift of 130 min at all three dipoles; self-potential signals precede gas temperature variations. Interestingly, contrary to the rain season (see discussion in Friedel et al., 2004), no correlation at all is found between gas temperature and ground temperature (d,e), and no correlation is observed between the self-potential and ground temperature difference (f). The time frequency representation in Figure 7 a, b shows striking similarity between the variations of gas temperature and self-potential. Wavelet coefficients at one scale (2.2 hours) are displayed in c. Gas temperature variations (red curve) are clearly delayed with respect to the self-potential at both dipoles shown with blue and black lines.

Figure 8 plots fumarole temperature data versus self-potential U_{21} . Both gas and self-potential data were high-pass filtered with 2.9 h corner period. This choice of the corner period allows to exclude the 6- and 3 h harmonics of the barometric pressure variations. Furthermore, gas temperature data were time shifted with respect to the self-potential in order to align the correlating

152 signals.

153 5. Discussion

154 We observed a correlation between the cyclic variations in gas temperature and self-potential
155 which we attribute to the variations of the magma degassing for the following reasons. Firstly,
156 we can exclude meteorological influence. As discussed by Friedel et al. (2004), rainfall induced
157 SP signals can be recognized even without reference precipitation data because they have a very
158 typical shape, extremely large amplitudes and correlate positively with the ground temperature
159 data (with the linear correlation coefficient up to $R^2 = 9.8$!). Quasi-periodic signals observed in
160 self-potential and gas temperature data can not be attributed to atmospheric pressure neither, as
161 typical signal durations vary from 1 to 8 hours and do not generally coincide with the harmonics
162 of barometric pressure.

163 Secondly, the isotopic studies of Toutain et al. (2009) reveal the magmatic origin of CO₂ in
164 fumarole Woro. Clear correlation gas concentrations and temperature analyzed by Zimmer and
165 Erzinger (2003) and presented in Figure 2 suggest that these regularly oscillations of gas parameters
166 are directly related to magma degassing and are generated by regular oscillations of pressure, which
167 generate also the related self-potential variations. The whole area is characterized by intense
168 diffuse degassing, with carbon dioxide concentrations as high as 500 000 ppm in September 2002,
169 as reported by Toutain et al. (2009). Nevertheless, the ground temperatures at the electrode
170 locations did not record any temperature changes, related to variations in gas temperature. These
171 observations indicate that self-potential oscillations are generated by a mechanism other than
172 diffuse soil degassing or pure temperature effects at the electrode locations. In addition, oscillations
173 in gas temperature are preceded by self-potential signals with a time shift of more than two hours
174 indicating a relatively deep source of self-potential. Interestingly, these common oscillations of
175 self-potential and gas temperature have signatures very different from earlier observations related
176 to the rain season preceding the eruption in February 2001 (Byrdina et al., 2003; Richter et al.,
177 2004). These authors observed that ultra-long period (ULP) seismic events were systematically
178 accompanied by variations of both fumarole temperature (Richter et al., 2004) and self-potential
179 (Byrdina et al., 2003) without any significant time shift between them. Returning to oscillations
180 of self-potential and gas temperature during the dry season, we suppose them to be generated

by a deeper source than the source of ULP seismicity because of a larger time shift between the self-potential and gas temperature. In this case, the time shift between gas temperature and self-potential might contain information about the properties of the magmatic conduits or about the depth where the pressure pulses are originated.

For example, Cigolini et al. (2007) report radon emissions at Stromboli volcano related to Palermo earthquake of September 6th, 2002. The regional seismicity was found to be correlated with radon emissions and the rate of erupted magma volume. The time delay of radon emissions with respect to seismicity was interpreted by viscoelastic properties of the magma chamber. Furthermore, Olmos et al. (2007) observed a time delay of SO₂ emissions with respect to real time seismic amplitude measurements at Santa Ana volcano.

Physical models related to cyclic behavior of volcanic degassing in andesitic magmas are usually based on nonlinearities caused by the variable viscosity of magma. In these models, viscosity of magma depends on volatile content, temperature or pressure, and strongly decreases as the degassing rate increases (e.g. Melnik and Sparks, 1999; Lensky et al., 2008). An example is the stick-slip model of supersaturated magma degassing developed by Lensky et al. (2008). The gas diffuses into the magma, which cannot expand because of the presence of a sticking plug resulting in a build-up of pressure. When the pressure exceeds some critical value, the strength of the plug, the stick-slip motion occurs and the pressure is relieved. The magma sticks again when the pressure falls below the value of dynamic friction. Although the available data are not sufficient to attempt a numerical modeling, we can try to understand the information contained in the time shift between the gas temperature and the electric signals. In the logic of the stick-slip model we expect the electric potential to be generated during the phase where the pressure drop is maximal. The time shift would give the travel time of the gas from the source of pressure (e.g. the base of the plug) to the surface which would bring some constraints on the depth of the source of pressure as we will show in the following. The flow of a compressible ideal gas ($Pu = \text{constant}$) in the porous conduit is described by a modification of Darcy equation (e.g. Scheidegger, 1974):

$$u = \frac{k}{\mu} \cdot \frac{P_d^2 - P_s^2}{L \cdot P_s} \quad (5)$$

where u is the gas flux velocity in z-direction [m/s], k is the permeability in [m⁻²], μ is the dynamic viscosity of the gas in [Pa s]. P_d and P_s are the pressures at the source and at the surface in Pa, indices stay for "depth" and "surface". L is the depth of the fumarole origin which can be expressed

as $L = u \cdot \delta t$ where δt is the time delay of the gas in relation with self-potential.

Now we estimate the average gas pressure at the pressure source (Figure 9). The relationship between the gas pressure at magma temperature $T_d = 1000^\circ\text{C}$ and the gas pressure at the surface, at the temperature of $T_s = 450^\circ\text{C}$, follows from state equation of ideal gas:

$$\left(\frac{P_d}{P_s}\right)^{(\gamma-1)/\gamma} = \frac{T_d}{T_s}, \quad (6)$$

where γ is the ratio of specific heats at constant pressure and constant volume $c_p/c_v \approx 1.3$. We obtain from equation (6) the $P_d = 2\text{ MPa}$ considering the atmospheric pressure at the surface.

Returning now to equation (5), we take $k = 10^{-11}\text{ m}^2$ for the unknown conduit permeability and $\mu = 2 \cdot 10^{-5}\text{ Pa}\cdot\text{s}$ for the dynamic viscosity of the water vapor at 400°C (e.g. Mende and Simon, 1969), and obtain finally the estimation of darcy velocity $u \approx 0.04\text{ m/s}$ and the depth of $\approx 300\text{ m}$.

It is premature to take uncritically any estimations on the basis of self-potential data from one single location. The present study gives a direct evidence that the pressure variations in the magma conduit create measurable self-potential variations. However, in order to obtain quantitative information on the pressure source from self-potential monitoring data, it is advantageous to know the geometry of the flow system from previous structural self-potential studies (e.g. Aizawa et al., 2009). In addition, it is necessary to use several monitoring stations in order to characterize the attenuation of the self-potential transients with distance and to obtain a reliable estimate on the time delay between the self-potential and gas temperature variations.

6. Conclusion

Gas fumarole data and self-potential data collected at Solfatara Woro show correlating events at scales 1-8 h with a time shift of approximately 130 min. The correlation was observed at all three dipoles during a time interval of 40 days. The influence of different meteorological factors on both data sets could be excluded because 1) temperatures at electrode positions showed no correlation neither with self-potential nor with gas temperatures, 2) the typical signal durations do not coincide with the harmonics of atmospheric pressure, 3) the absence of response signals characteristic for rainfall in both self-potential and gas temperature data suggest that the correlation between self-potential and gas temperature can not be attributed to the rainfall. 4) geochemical data indicate the magmatic origin of several fumarolic gas components (Toutain et al., 2009).

Therefore, the correlated self-potential and gas temperature signals reflect directly the quasi-periodic variations in magma degassing. The dominant generation mechanism of electric signals is probably the electrokinetic and thermoelectric effects of gas flow. With higher spatial density of self-potential dipoles it could be possible to localize the source of the multi-parameter signals using the information about the amplitude of the self-potential signals as function of the distance and time delay between the correlated signals.

7. Acknowledgments

The work was partially supported by DFG Ja 590/6. We thank the personnel at BPPTK, Jogjakarta. We thank Jean Vandemeulebrouck, Eric Delcher and André Revil for interesting discussions improving the paper. We thank J.F. Lénat and an anonymous reviewer for their constructive contributions to our manuscript. The non-polarizable electrodes were borrowed at the Geophysical Instrument Pool Potsdam (GIPP) of the German Research Centre for Geosciences (GeoForschungszentrum Potsdam, GFZ). We used Latex, JabRef, and InkSpace open source software.

References

- Aizawa, K., Ogawa, Y., Ishido, T., 2009. Groundwater flow and hydrothermal systems within volcanic edifices: Delineation by electric self-potential and magnetotellurics. *J. Geophys. Res.* 114, B01208.
- Byrdina, S., Friedel, S., Wassermann, J., Zloticki, J., 2003. Self-potential variations associated with ultra-long-period seismic signals at Merapi volcano. *Geophys. Res. Lett.* 30 (22), 2156.
- Byrdina, S., Revil, A., Contraires, S., Pant, S., Gautam, U., Koirala, B., Shrestha, P., Tiwari, D., Sapkota, S., Perrier, F., 2009. Dipolar self-potential anomaly associated with carbon dioxide and radon flux at Syabru-Bensi hot springs in central Nepal. *J. Geophys. Res.* 114, B10101.
- Camus, G., Gourgaud, A., Mossand-Berthommier, P., Vincent, P., 2000. Merapi (Central Java, Indonesia) An outline of the structural and magmatological evolution, with a special emphasis to the major pyroclastic events. *J. Volcanol. Geoth. Res.* 100 (1-4), 139–163.
- Cigolini, C., Laiolo, M., Coppola, D., 2007. Earthquake-volcano interactions detected from radon degassing at Stromboli (Italy). *Earth Planet. Sci. Lett.* 257, 511525.
- Crespy, A., Revil, A., Linde, N., Byrdina, S., Jardani, A., Boleve, A., Henry, P., 2008. Detection and localization of hydromechanical disturbances in a sandbox using the self-potential method. *J. Geophys. Res.* 113, B01205.
- Finizola, A., Lénat, J.-F., Macedo, O., Ramos, D., Thouret, J., Sortino, F., 2004. Fluid circulation and structural discontinuities inside Misti volcano (Peru) inferred from self-potential measurements. *J. Volcanol. Geoth. Res.* 135, 343–360.

274 Friedel, S., Byrdina, S., Jacobs, F., Zimmer, M., 2004. Self-potential and ground temperature at Merapi volcano
 275 prior to its crisis in the rainy season of 2000-2001. *J. Volcanol. Geoth. Res.* 134 (3), 149 – 168.
 276 Harris, A., Ripepe, 2007. Regional earthquake as a trigger for enhanced volcanic activity: Evidence from MODIS
 277 thermal data. *Geophys. Res. Lett.* 34 (2), L02304.
 278 Ishido, T., Mizutani, H., 1981. Experimental and theoretical basis of elektrokinetic phenomena in rock-water systems
 279 and its applications to geophysics. *J. Geophys. Res.* 86, 1763–1775.
 280 Lénat, J. F., Fitterman, D., Jackson, D., Labazuy, P., 2000. Geoelectrical structure of the central zone of Piton de la
 281 Fournaise volcano (La Réunion). *Bull. Volcanol.* 62, 75–89.
 282 Lensky, N. G., Sparks, R., Navon, O., Lyakhovsky, V., 2008. Cyclic activity at Soufriere Hills Volcano, Montserrat:
 283 degassing-induced pressurization and stick-slip extrusion. *Geol. Soc. Spec. Pub.* 307, 169–188.
 284 Mallat, S., 1999. A wavelet tour of signal processing, 2nd Edition. Academic Press.
 285 Melnik, O., Sparks, R., 1999. Non-linear dynamics of lava dome extrusion. *Nature* 402, 37–41.
 286 Mende, D., Simon, G., 1969. Physik - Gleichungen und Tabellen. VEB Fachbuchverlag Leipzig.
 287 Nourbehecht, B., 1963. Irreversible thermodynamic effects in inhomogeneous media and their application in certain
 288 geoelectric problems. Ph.D. thesis, M. I. T., Cambridge.
 289 Olmos, R., Barrancos, J., Rivera, C., Barahona, F., López, D. L., Henriquez, B., Hernández, A., Benitez, E.,
 290 Hernández, P. A., Pérez, N. M., Galle, B., 2007. Anomalous Emissions of SO₂ During the Recent Eruption of
 291 Santa Ana Volcano, El Salvador, Central America. *Pure Appl. Geophys.* 164, 24892506.
 292 Revil, A., Finizola, A., Piscitelli, A., Rizzo, E., Ricci, T., Crespy, A., Angeletti, B., Balasco, M., Barde-Cabusson,
 293 S., Bennati, L., Bolve, A., Byrdina, S., N., N. C., Gangi, F. D., Morin, J., Perrone, A., Rossi, M., Roulleau, E.,
 294 Suski, B., 2008. Inner structure of La Fossa di Vulcano (Vulcano Island, southern Tyrrhenian Sea, Italy) revealed
 295 by high resolution electric resistivity tomography coupled with self-potential, temperature, and soil CO₂ diffuse
 296 degassing measurements. *J. Geophys. Res.* 113, B07207.
 297 Revil, A., Pezard, P. A., Glover, P. W. J., 1999. Streaming potential in porous media 1. Theory of the zeta potential.
 298 *J. Geophys. Res.* 104, 20021–20031.
 299 Revil, A., Saracco, G., Labazuy, P., 2003. The volcano-electric effect. *J. Geophys. Res.* 108 (B5), 2251.
 300 Richter, G., Wassermann, J., Zimmer, M., , Ohrnberger, M., 2004. Correlation of seismic activity and fumarole
 301 temperature at the Mt. Merapi volcano (Indonesia) in 2000. *J. Volcanol. Geoth. Res.* 135, 331–342.
 302 Scheidegger, A. E., 1974. The physics of flow through porous media, 3rd Edition. University of Toronto. Press,
 303 Toronto.
 304 Surono, S., Jousset, P., Pallister, J., Boichu, M., Buongiorno, M. F., Budisantoso, A., Costa, F., Andreastuti, S.,
 305 Prata, F., Schneider, D., Clarisse, L., Humaida, H., Sumarti, S., Bignami, C., Griswold, J., Carn, S., Oppenheimer,
 306 C., 2011. The 2010 explosive eruption of Java's Merapi volcano a "100-year" event. submitted to *J. Volcanol.*
 307 *Geotherm. Res.*
 308 Toutain, J., Sortino, F., Baubron, J., Richon, P., Surono, S., Sumatri, S., A.Nonell, 2009. Structure and CO₂ budget
 309 of Merapi volcano during inter-eruptive periods. *Bull. Volcanol.* 71, 815–826.
 310 Voight, B., Constantine, E. K., Siswovidjojo, S., Torley, R., 2000. Historical eruptions of Merapi volcano, Central
 311 Java. *J. Volcanol. Geoth. Res.* 100 (1-4), 69–138.

312 Zimmer, M., Erzinger, J., 2003. Continuous H₂O, CO₂, ²²²Rn and temperature measurements on Merapi Volcano,
313 Indonesia. J. Volcanol. Geoth. Res. 125 (1-2), 25 – 38, Understanding volcanoes through multiparameter measure-
314 ments and their interpretation: In memory of Bruno Martinelli.

Figure 1: a) Simplified map of Java with location of Merapi volcano and Java trench. b) Summit area of Merapi after Camus et al. (2000), with main lava flows until 2000, crater rims, active dome, and Woro fumarole field. c) Location of our monitoring station at Woro with self-potential dipoles and gas temperature sensor. Gray circles indicate fumaroles (modified from Byrdina et al. (2003)).

Figure 2: An example of a) gas concentration recorded in 1998 and b) temperature variations recorded in 2000 at Woro solfatara field of Merapi volcano (after Zimmer et al, 2004).

Figure 3: a) Two synthetic data sets X and Y (black lines) were created by superimposing random noise with two identical features A and B with time shift 20 and 15 hours. b) Cross-correlation function does not show any clear maxima. c) Cross-correlation of wavelet coefficients of X and Y separates the scales of correlation and gives the time shifts between both signals.

Figure 4: Time series of fumarolic temperature, self-potential and ground temperature. See Figure 1 for location of the sensors. Data from the time period between day 110 and 137 of year 2001 without any perturbations were taken for a further study.

Figure 5: Energy spectral density of the time series presented in Figure 4 in the time period between day 110 and 137 of year 2001.

Figure 6: The cross-correlation of wavelet coefficients for a) T_{fum} and U_{21} , b) T_{fum} and U_{43} , c) T_{fum} and U_{65} , d) T_{fum} and T_{21} , e) T_{fum} and T_4 , f) T_{21} and U_{21} . High values of $W(T_{fum}, U)$ are encountered at scales 1-8 hours indicating a correlation between the fumarole gas temperature and SP. A time shift between the correlated signals is approximately 130 minutes, the self-potential variations precede the corresponding variations of fumarole temperature. Interestingly, there is no correlation between the gas and the ground temperature (d, e); there is no correlation between the electrode temperature difference and the self-potential (f).

Figure 7: Time-frequency representation of gas temperature (a) and self-potential dipole U_{21} (b). Time in Julian days is represented in X and scales in Y axes. c) Wavelet coefficients at scale of maximal correlation (≈ 2.2 hours) for the gas temperature, self-potential at two dipoles, and for electrode temperature difference $T_2 - T_1$.

Figure 8: Gas temperature data versus self-potential U_{21} at period range from 2 min to 170 min. Both kinds of time series were high-pass filtered, gas temperature data were time shifted to align the correlated signals.

Figure 9: Parameters entering equations 5 and 6 which govern the flow of a compressible fluid in the fumarole conduit (see text).