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Abstract. The competitive binding of rare earth elements (REE) to humic acid (HA) and carbonates was studied experimentally at various pH and alkalinity values by combining Ultrafiltration and Inductively Coupled Plasma Mass Spectrometry techniques. The results show that the REE species occur as binary humate or carbonate complexes but not as ternary REE-carbonate-humate as previously proposed. The results also reveal the strong pH and alkalinity dependence of the competition as well as the existence of a systematic fractionation across the REE series. Specifically, carbonate complexation is at a maximum at pH 10 and increase with increasing alkalinity and with the atomic number of the REE (LuCO$_3$ >> LaCO$_3$). Modelling of the data using Model VI and recently published stability constants for complexation of REE by humic acid well reproduced the experimental data, confirming the ability of Model VI to accurately determine REE speciation in natural waters. This modelling also confirms the reliability of recently published stability constants. This work shed more light not only on the competition between carbonates and HA for REE complexation but also on the reliability of WHAM 6 and Model VI for calculating the speciation of REE with organic matter in alkaline organic rich-water.

Key words: Rare earth elements, humic acid, carbonates, binding, speciation, ultrafiltration
1. Introduction

The hydrochemical behavior of Rare Earth Elements (REE) is strongly influenced by their solution speciation [1, 2]. Due to the complexation of REE by a large variety of ligands, only a small fraction of each REE occurs as free hydrated ions (Ln$^{3+}$ - Ln as lanthanide) in circumneutral waters. In circumneutral waters, REE are mostly bound to humic substances (HM) such as fulvic acids (FA) and humic acids (HA) [3-5]. By contrast, in alkaline waters with high carbonates concentrations, REE complexation is generally dominated by carbonate complexes as LnCO$_3^+$ and Ln(CO$_3$)$_2^-$ [2, 5]. However, competition reactions between carbonates and organic matter for REE complexation have not yet been experimentally constrained. At present, accurate models of REE chemistry in natural waters are only dependent on experimentally determined (i) REE carbonates complexation constants [6-12] and (ii) REE humic substances constants [13-15]. However, since there is no experimental data about the competition between carbonates and organic matter for REE complexation, an important piece of information is missing.

Previous studies [5, 16-18] based on speciation calculation of some REE (e.g., La$^{3+}$, Eu$^{3+}$, Lu$^{3+}$) concluded that organic complexes dominate for intermediate pH range (from pH 4 to 8) whereas carbonate complexes (Ln(CO$_3$)$_2^-$) are the predominant species at alkaline pH (> 8). However, as discussed by these authors themselves, speciation calculations may underestimate the LnHM complexes, especially at alkaline pH (> 8). They suggest that this could have significant effects on ternary inorganic-colloid-HM-Ln interactions [17, 19, 20]. They also suggested that Ln speciation would be dominated by interactions with humic material. The lack of experimental data regarding LnHM interactions at neutral-to-alkaline pH leads to extrapolation and the speciation results obtained for alkaline waters should be regarded with caution [18]. Takahashi et al. [21] calculated speciation of Ce$^{3+}$, Eu$^{3+}$ and Lu$^{3+}$ in solution in the presence of humic acid. Hydroxide carbonates and humate complexes were considered. Unlike the studies above, their results suggest that LnHA complexes should be predominant in a wide
pH range (from pH 3 to 10.5), and even more at higher HA concentrations. \( \text{Ln} (\text{CO}_3)^{2-} \) should be dominant at pH higher than 10.5. These observations are further illustrated by a new study considering Model VI fitted complexation constants between REE and HA. Model VI calculated high proportions of light REE (LREE) complexed with organic matter under alkaline pH conditions [15]. Comparison of REE speciation model calculations, taking into account organic ligands, shows strong differences between each model regarding the competition between humic substances and carbonates for REE complexation.

In order to assess humic acid and carbonates competition for REE at alkaline pH, batch equilibration experiments with REE, Aldrich HA and carbonates were performed simultaneously for the 14 naturally occurring REE. This new dataset was obtained using an experimental method which combines an ultrafiltration technique and Inductively Coupled Plasma Mass Spectrometry. These experiments were designed to elucidate the pH range where REE-humate complexes would be dominant in natural organic-rich waters for various alkalinity concentrations and test whether significant formation of ternary complexes can take place in such conditions. Moreover, Humic Ion Binding Model VI included in WHAM 6 - a model that does not considered ternary surface complexes - was used to model the binding of lanthanides to humic substances [22]. This study should also evidence the ability of the newly determined HA-REE binding constants [15] to accurately predict the speciation of REE in alkaline waters.

2. Materials and Methods

2.1. Experimental Binding of Rare Earth Elements by Humic Acid and Carbonates

All chemicals used were of analytical grade, and all the experimental solutions were prepared with doubly deionized water (MilliQ system, Millipore™). Complexes were prepared in polyethylene containers previously soaked in 10 % Ultrapure \( \text{HNO}_3 \) for 48 h at 60 °C, then rinsed.
with MilliQ water for 24 h at 60 °C to remove all possible REE contamination sources. Synthetic REE solutions were prepared from nitrate REE standards (10 ppm, Accu Trace™ Reference Standard). All experiments were carried out at room temperature, i.e. 20 °C ± 2.

2.1.1. Humic acid

Purified humate, referred to below as HA (humic acid), was obtained from Aldrich™ humic acid (Aldrich™, H1, 675-2) following the protocol described by Vermeer et al. [23]. HA sample was freeze-dried and stored in a glass container at room temperature. HA obtained was ash free and in its protonated form, with the following elemental composition (in weight percent): C = 55.8 %, O = 38.9 %, H = 4.6 %, N = 0.6 %. REE concentrations in HA were below the detection limit of ICP-MS method (i.e. below 1 ppt). HA has a mean molecular weight of 23 kDa [23]. Prior to use, the freeze-dried humate was resuspended overnight in an 0.001 mol L⁻¹ NaCl electrolyte solution at pH = 10, to ensure complete dissolution of the sample [24, 25].

2.1.2. Experimental set-up

REE complexation with HA and carbonates was investigated using a standard batch equilibration technique. 100 mL of solutions were prepared with 50 ppb of each REE (e.g., 360 nmol L⁻¹ La to 286 nmol L⁻¹ Lu), 5 mg L⁻¹ of HA and various concentration of NaHCO₃ (from 10⁻³ to 10⁻² mol L⁻¹) in a 10⁻³ mol L⁻¹ NaCl-solution. Prior to addition of NaHCO₃, the pH of the solution was approximately 4. The initial hydroxide concentration was negligible and concentration of LnOH²⁺ was therefore minimal. After addition of NaHCO₃, pH was adjusted to the tested pH range, from 6 to 11 by adding NaOH (4 mol L⁻¹). The pH was measured with a combined Radiometer Red Rod electrode. The electrode was calibrated with WTW™ standard solutions (pH 4, 7 and 10). The accuracy of the pH measurement was ±
0.05 pH unit. Experimental solutions were stirred for 48 h (the equilibrium time was
determined from preliminary kinetic experiments) to allow equilibration and partitioning of REE
between the aqueous solution and the humate suspension. Aliquots of 10 mL were sampled
twice: at the beginning of the experiment; and after 48 h at equilibrium state. REE complexed by
the HA were separated from the remaining inorganic REE by ultrafiltration. Ultrafiltrations were
carried out by centrifugating the 10 mL solution samples through 15 mL centrifugal tubes
equipped with permeable membranes of 5 kDa pore size (Millipore Amicon Ultra-15). All
centrifugal filter devices used were washed and rinsed with 0.1 mol L⁻¹ HCl and MilliQ water
two times before use in order to minimize contamination. Centrifugations were performed using
a Jouan G4.12 centrifuge with swinging bucket rotor at 3000 g for 30 minutes. This allowed the
REE-HA complexes to be quantitatively separated from inorganic REE species. The selectivity
of the 5 kDa membrane regards to the REE-HA complexes was verified by monitoring the
Dissolved Organic Carbon (DOC) contents of the ultrafiltrates. Results show that the latter were
systematically lower or equal to blank values (below 0.1 ppm). Possible adsorption of inorganic
REE species onto the membrane or onto cell walls was also monitored. Inorganic REE solutions
of given REE concentration were ultrafiltrated several times. Results showed that between 98.91
(for Ho) and 99.98 % (for Yb) of the REE present in solution were recovered in the ultrafiltrates,
demonstrating that none REE were adsorbed either on the membranes or on the walls of the cell
devices.

Amount of REE complexed with HA correspond to the difference between the initial REE
concentration and the remaining REE concentration into the < 5 kDa ultrafiltrates. REE
concentrations were determined by using an Agilent Technologies™ HP4500 ICP-MS instrument.
Quantitative analyses were performed using a conventional external calibration procedure. Three
external standard solutions with REE concentrations similar to the analyzed samples were
prepared from a multi-REE standard solution (Accu Trace™ Reference, 10 mg L⁻¹, USA). Indium
was added to all samples as an internal standard at a concentration of 0.87 μmol L⁻¹ (100 ppb) to
correct for instrumental drift and possible matrix effects. Indium was also added to the external
standard solutions. Calibration curves were calculated from measured REE/indium intensity
ratios. The instrumental error on REE analysis in our laboratory as established from repeated
analyses of multi-REE standard solution (Accu Trace™ Reference, USA) and of the SLRS-4
water standard is below ± 2 % [4, 25]. Chemical blanks of individual REE were all lower than
detection limit (1 ppt), which is negligible since they are three to four orders of magnitude lower
than the concentrations measured in the synthetic solutions used for the complexation
experiments. DOC concentrations were determined using a Shimadzu 5000 TOC analyzer. The
accuracy of DOC concentration measurements is estimated at ± 5 % as determined by repeated
analyses of freshly prepared standard solutions (potassium biphtalate). Carbonates concentrations
were determined by potentiometric titrations (HCl 0.1 mol L⁻¹), with Gran method analysis. The
uncertainty is better than 5 %.

In order to check that no retention of REE or carbonates occurs inside the membrane
during ultrafiltration, mass balance calculations were performed. The initial concentration of
each element is compared with the sum of each element concentration in the ultrafiltrate and in
the retentate. In the presented experiments, mass balanced calculations show that > 98 % of the
REE and > 95 % of the carbonates and DOC were recovered. Moreover, in order to verify that no
precipitation occurs, samples were filtrated at 0.2 µm before ultrafiltration. Concentrations of
REE, HA and carbonates were systematically identical within analytical uncertainties in the 0.2
µm filtrates and the raw samples.

2.2. WHAM 6 and Humic Ion Binding Model VI

WHAM 6 (version 6.0.10), incorporating Humic Ion Binding Model VI (Model VI), was
used to calculate REE speciation in the batch experiments. Model VI has been described in detail
by Tipping [22]. The model is a discrete binding site model in which binding is modified by
electrostatic interactions. There is an empirical relation between the net humic charge and an electrostatic interaction factor. The discrete binding sites are represented by two types of sites (types A and B), and within each type of site there are four different sites present in equal amounts. The two types of sites are described by intrinsic proton binding constants (pK\textsubscript{A} and pK\textsubscript{B}) and spreads of the values (\(\Delta pK_A\) and \(\Delta pK_B\)) within each type of sites. There are \(n_A\) (mol g\(^{-1}\)) A-type sites (associated with carboxylic type groups) and \(n_B = n_A/2\) (mol g\(^{-1}\)) B-type of sites (often associated with phenolic type groups). Metal binding occurs at single proton binding sites or by bidentate complexation between pairs of sites depending on a proximity factor that defines whether pairs of proton binding groups are close enough to form bidentate sites. Type A and Type B sites have separate intrinsic binding constants (log \(K_MA\) and log \(K_MB\)), together associated with a parameter, \(\Delta LK_1\), defining the spreads of values around the medians. A further parameter, \(\Delta LK_2\), takes into account a small number of stronger sites. By considering results from many datasets, a universal average value of \(\Delta LK_1\) is obtained, and a correlation established between log \(K_MB\) and log \(K_MA\) [22]. Then, a single adjustable parameter (log \(K_MA\)) is necessary to fully describe metal binding. Generic parameters for HA are presented in Table 1. WHAM 6 databases were modified and included new log \(K_MA\) for REE complexation with humic acid [15] and well-accepted, infinite dilution (25°C) stability constants for REE carbonates complexes [11].

3. Experimental Results

Experimental data are reported for three REE (La, Eu and Lu) in Table 2 and illustrated in Fig. 1. Competition between HA and carbonates for REE complexation is examined by considering the mass fraction inorganic REE species as a function of pH. The complementary fraction is made up of REE organic complexes. Based on speciation calculations of the inorganic fraction using WHAM 6, REE were shown to consist mostly of carbonate complexes. In these experimental conditions (see section 2.1), hydroxide and free species are only present at very low
concentrations (as regards to speciation calculations < 0.2 % and < 3.8 % of the inorganic fraction for La, respectively). Two REE-carbonate complexation reactions are considered in Fig. 1 and described by the following equations:

\[
\text{Ln}^{3+} + \text{CO}_3^{2-} \rightleftharpoons \text{LnCO}_3^+ \quad [1]
\]

\[
\text{Ln}^{3+} + 2 \text{CO}_3^{2-} \rightleftharpoons \text{Ln(CO}_3)_2^- \quad [2]
\]

whereas humic complexation are described by the following equation:

\[
\text{Ln}^{3+} + \text{HA}^- \rightleftharpoons \text{LnHA}^{2+} \quad [3]
\]

As shown in Figure 1, \(\text{LnCO}_3^+\) and \(\text{Ln(CO}_3)_2^-\) concentrations depend strongly on the pH- and the carbonate content. \(\text{LnCO}_3^+\) concentrations decrease with pH increase whereas \(\text{Ln(CO}_3)_2^-\) concentrations increase while pH increases. Moreover, \(\text{Ln(CO}_3)_2^-\) and \(\text{LnCO}_3^+\) concentrations increase with the solution alkalinity. The slight "bump" in the pH range 8-8.5 corresponds to the competitive reaction between mono- (Eq. [1]) and di- (Eq. [2]) carbonato-complexation reactions. This "bump" is more significant for LREE than for heavy REE (HREE), a result consistent with the difference in complexation constants of LREE- and HREE-carbonate complexes [11]. Thus, a fractionation is apparent between LREE and HREE regarding their complexation to carbonate. Let’s consider for example a pH 10 value of alkalinity \(10^{-2}\) mol L\(^{-1}\) and the results observed under these conditions. Only 15 % of La is bound to carbonate whereas 30 % of Eu and up to 60 % of Lu are bound to carbonate. Moreover, carbonate concentrations were systematically identical in the ultrafiltrates and in the initial batches (within the uncertainty of the measures). Calculation considering that 1:1:2 ternary complexes could be formed were performed and further demonstrate that no carbonate was bound to HA in our experiments (Ln concentrations are several order of magnitude higher than maximum \(\text{CO}_3^{2-}\) concentration variation between ultrafiltrates and initial batches). Consequently, no additional interactions
between metal (Ln\(^{3+}\)), ligand \((\text{CO}_3^{2-})\) and surface (HA) occurred demonstrating that ternary surface complexes did not develop.

4. Discussion

4.1. Lack of evidence of ternary complexe formation

A common question when dealing with metal (M) speciation in systems containing humic substances (HS) such as HA and inorganic ligands (L) such as carbonate is, whether or not, ternary complexe (M-HA-L\(_m\) with m corresponding to the ligand stoechiometry), can form.

Information about ternary complex formation in the literature is scarce, especially concerning REE. Even if such a mechanism was suggested for REE (e.g., [17]), only a few experimental studies brought direct evidence for possible formation of such complexes [19, 20]. Dierckx et al. [19] provided evidence for mixed-ligand complex formation of Eu\(^{3+}\) with humic acid and inorganic ligands (i.e., \(\text{CO}_3^{2-}\)). However, the interpretation of Dierckx et al. [19] left some open questions, as they observed formation of either M-HA or M-HA-L\(_2\) complexes formed across the whole range of L concentrations, without observing the formation of M-HA-L\(_1\) complexes. These observations are unusual with respect to common experiences found with inorganic ligands and oxide-based surfaces (e.g., [26]). Moreover, Glaus et al. [27, 28] have shown that the formation of mixed-ligand-humic complexes is rather weak as compared to the formation of simple ligand-complexes with inorganic ligands. Ternary-humic complexes appear thus less important than predicted by the data of Dierckx et al. [19].

A possible explanation for the absence of ternary complex formation in the present work might be the electrostatic repulsion between the negatively charged HA and Ln-CO\(_3\). Due to the polyelectrolyte character of HA, this repulsion is stronger than that occurring between low-molecular weights ligands. Schindler [26] reported that ternary complexes with SiO\(_2\) and TiO\(_2\)
surfaces are rather weak. Both surfaces are negatively charged at the pH of Schindler's experiments and can therefore be considered as analogues to HS. Ternary surface complexes are thus not as important as previously stated and do not need to be considered in REE speciation calculation in systems dominated by organic and alkaline water.

4.2. Competition between humic acid and carbonates for REE complexation

In order to further constrain the competition between humic acid and carbonates for REE complexation, calculation using Model VI in WHAM 6 were performed. Calculations were conducted using Model VI in which a new determined log $K_{MA}$ dataset for HA-REE complexation was integrated [15]. These log $K_{MA}$ values were estimated from REE complexation by HA experiments without any competing effect. The log $K_{MA}$ values range from 2.58 ± 0.16 (for La) to 2.65 ± 0.15 (for Eu); these latter being slightly higher than the one estimated by Lead et al. [18] (2.36 ± 0.13). These calculations only considered trivalent REE species. Speciation calculations are illustrated on Figs. 1.2a, b and c for La, Eu and Lu, respectively, for the three experimental conditions (i.e. increasing alkalinity and pH). In particular, Model VI reproduced quite well the observed dependence of the proportion of carbonate complexes with pH and alkalinity. However, the observed experimental "bump" is not modelled by Model VI. This is due to the fact that only Ln complexation with two $\text{CO}_3^{2-}$ is predicted whereas Ln complexation with a single $\text{CO}_3^{2-}$ is overwhelmed by competition with HA (Fig. 1.2). Comparison between experimental and calculated values evidences that Model VI slightly underpredicts (0 to 11 %) REE complexation by carbonate (Figs. 1.2a, b and c). Root mean square error (rmse) values represent the sum of the squares of the difference between observed and calculated values. As indicated by the rmse systematically below 0.06 (Fig. 1.2), fits can be considered of good quality, even if rmse values increase when competition between HA and carbonates is more developed.
(i.e., for alkalinity of $10^{-2}$ mol L$^{-1}$). Overall, it is clear that LREE to Middle REE (MREE) are strongly bound to HA whereas HREE are more shared between HA and carbonate fractions.

More in detail, pH is a crucial parameter affecting binding, since it regulates competition between HA and carbonates. Carbonate complexation mostly affects REE speciation in alkaline waters (pH above 8.5). These observations validate both the use of Model VI [22] and of the log $K_{MA}$ (REE-HA) dataset determined by Pourret et al. [15] to confidently predict REE speciation in natural alkaline waters. As stated by Tipping [22], an important issue in increasing WHAM and Model VI capacity to perform chemical speciation calculations for field situations is whether significant formation of ternary complexes takes place. Simulations on some trace metals may have indeed significantly underestimated the extent of metal binding as compared to observation especially when binding occurs through the formation of ternary complexes [29]. As evidenced by experimental results, none ternary surface complexation occurs between REE, HA and carbonate. WHAM 6 is thus applicable to calculate REE speciation in natural water even if it does not take into account ternary surface complexation. This study combined with a previous one [30] now covers a wide range of natural conditions and shows that WHAM and Model VI are reliable in calculating the speciation of REE with organic matter in acidic and circumneutral DOC-rich ground- and river waters [30] and in alkaline organic rich-water (this study). These results suggest that dissolved organic complexes of the REE are more important than carbonates complexes for LREE to MREE and as important for HREE in World Rivers. As previously suggested by Tang and Johannesson [5], the role played by organic material to complex REE increases our understanding of REE cycling in the hydrosphere. This also questions the fact that carbonate complexes could dominate the REE cycle in circumneutral pH-low carbonate concentrations fresh waters.

5. Conclusions
Experimental studies of HA and carbonate competition for REE complexation were carried out for the 14 naturally REE simultaneously. Experimental method combines an ultrafiltration technique and ICP-MS to determine REE concentrations in the different pools. Competition between HA and carbonates for REE complexation is pH- and carbonate concentration-dependent. There is no evidence of any ternary surface complex as previously proposed (e.g., [19]). These experiments elucidate the pH range where humate complexes could be the dominant species of REE(III) in natural organic-rich waters, for various alkalinity concentrations. Carbonates are the only REE predominant species for HREE at higher alkalinity concentrations, above pH 8.5. A fractionation develops between LREE and HREE relative to REE complexation to carbonates, especially at higher alkalinity. Modelling calculations were performed with Model VI [22]. Calculations were consistent with experimental result, namely the pH- and carbonate concentration-dependence. The results show the influence of the competitive reactions between carbonates and HA for REE complexation at alkaline pH. All these observations allow validating the log K_{MA} (REE-HA) dataset [15] that can be, therefore, used with confidence to predict REE speciation in natural alkaline waters. They also evidence the reliability of WHAM 6 and Model VI in calculating the speciation of REE with organic matter in alkaline organic rich-water, as ternary surface complexes do not need to be modelled. Overall, the results of this study suggest that further considerations about organic matter should be taken into account especially at alkaline pH in organic-rich waters.
Acknowledgements

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References


Tables and Figures Captions

Table 1. Model VI parameters for humic acid [22].

Table 2. Proportion of Ln species in the ultrafiltrate.

Fig. 1. Proportion of inorganic species for (a) La, (b) Eu and (c) Lu (experimental concentrations: 50 ppb of each REE, 5 mg L\(^{-1}\) of HA and alkalinity of 10\(^{-2}\) mol L\(^{-1}\)). Squares represent experimental data points (proportion of species in the ultrafiltrate), whereas solid lines represent modelled total inorganic species, dash lines modelled LnCO\(_3^+\) and dot lines modelled Ln(CO\(_3\))\(_2^-\) (see text for details).

Fig. 2. Comparison between Model VI calculations and experiments. Proportion of lanthanides bound to carbonates as a function of pH for various alkalinities: (a) La, (b) Eu and (c) Lu.
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Table 1.
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<td>10.81</td>
<td>10.5</td>
<td>12.01</td>
<td>23.98</td>
<td>51.16</td>
</tr>
</tbody>
</table>

Table 2.
La(CO$_3$)$_2^-$ + LaCO$_3$ + La(CO$_3$)$_2^-$

EuCO$_3$ + Eu(CO$_3$)$_2^-$

LuCO$_3$ + Lu(CO$_3$)$_2^-$

Fig. 1
Fig. 2.